

# Local defect properties and their signatures in electrical probes of GaN defect spin dynamics

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University of Iowa

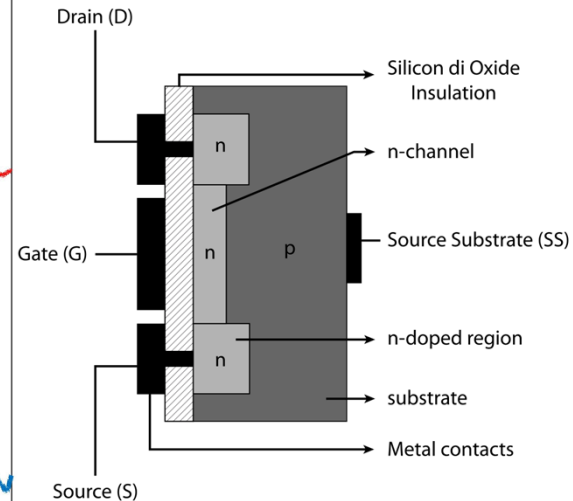
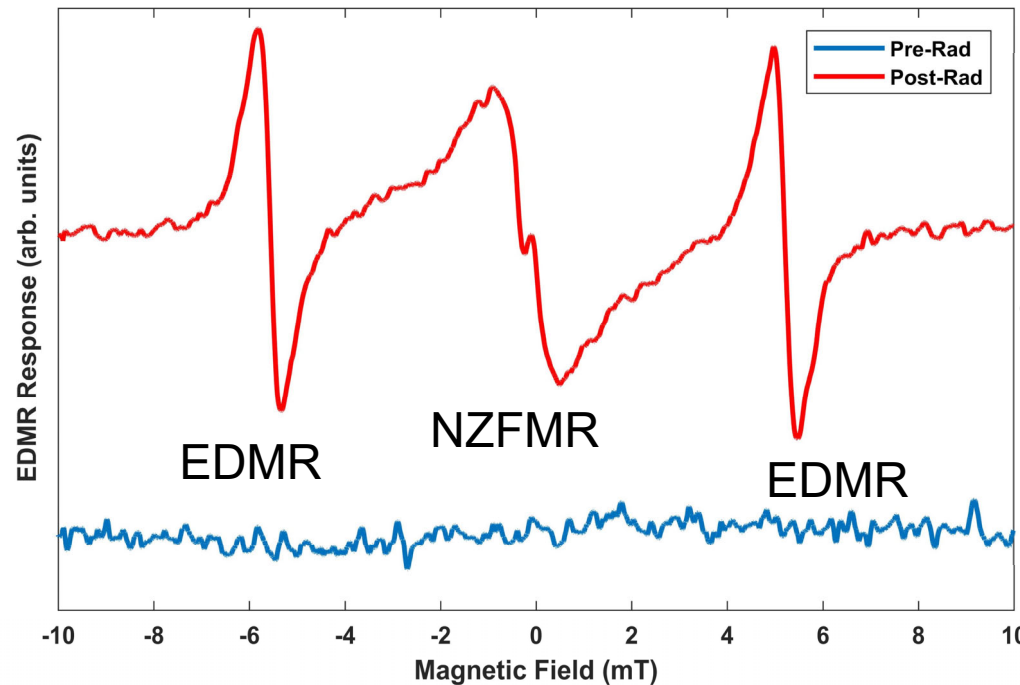
David Fehr  
Joseph Sink (here)

Measurements: Lenahan  
Devices: Chu  
Additional theoretical discussion: Tuttle



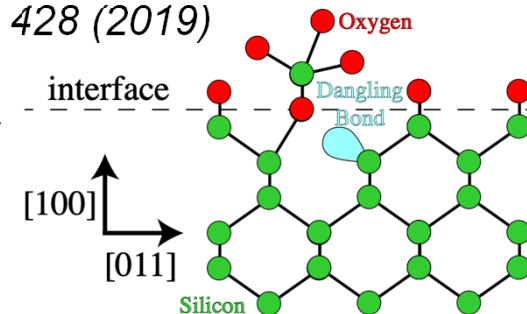
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# gate leakage through irradiated nonmagnetic Si/SiO<sub>2</sub> junctions



*IEEE TNS 66, 428 (2019)*

RF frequency 151 MHz, source and drain 0.33 V, gate 0.3 V  
near-interface trap ( $P_b$ , which has hyperfine interactions)

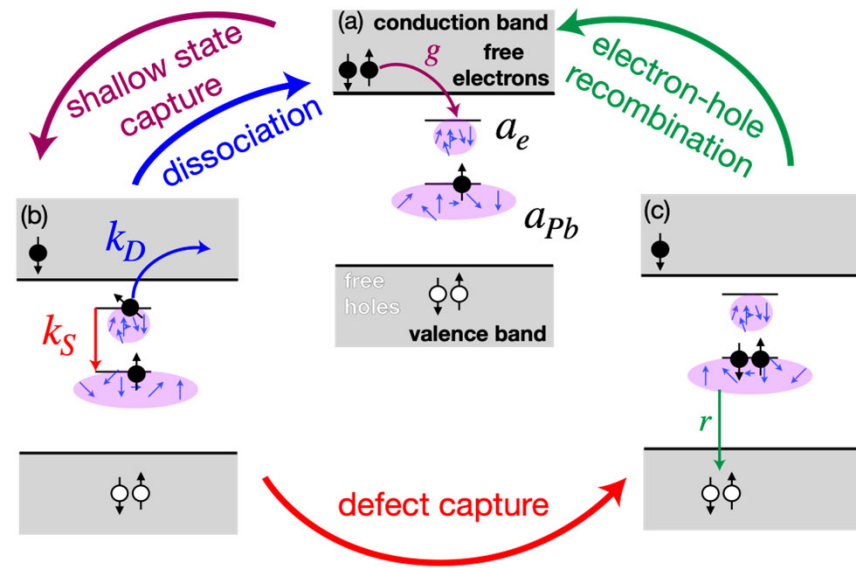
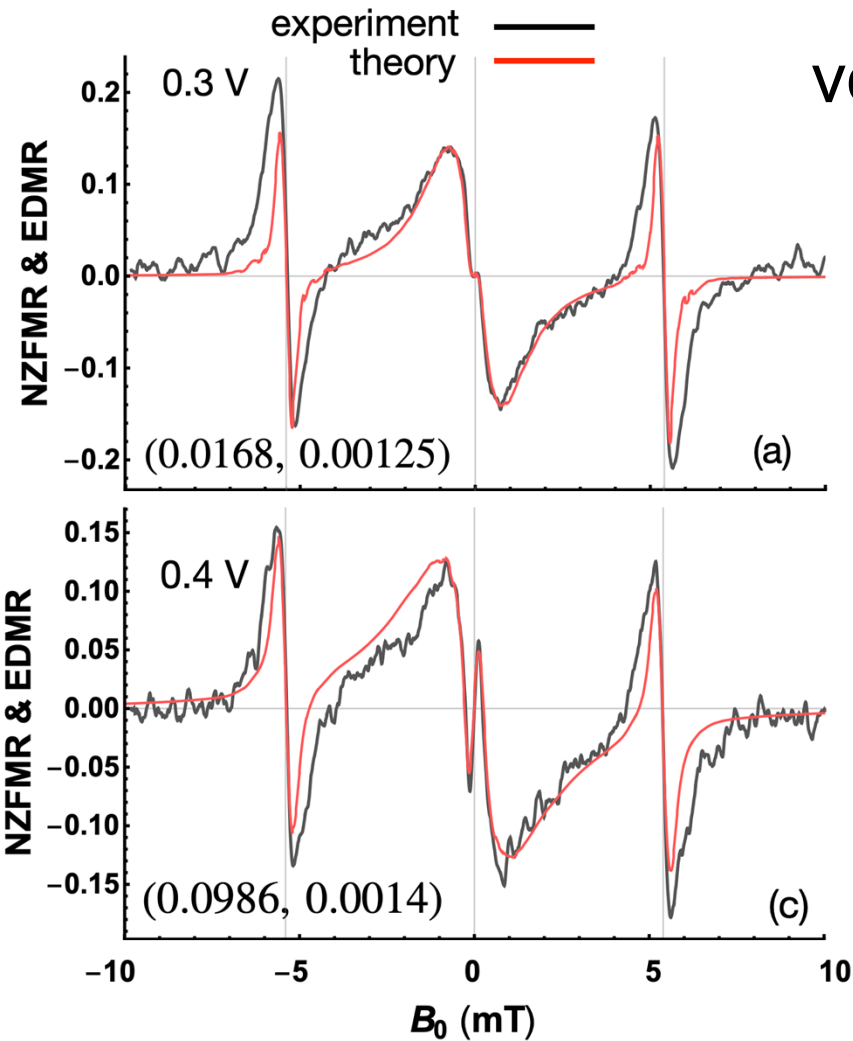


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# voltage dependence reveals rates

APL 123, 251603 (2023)  
arXiv:2008.08121

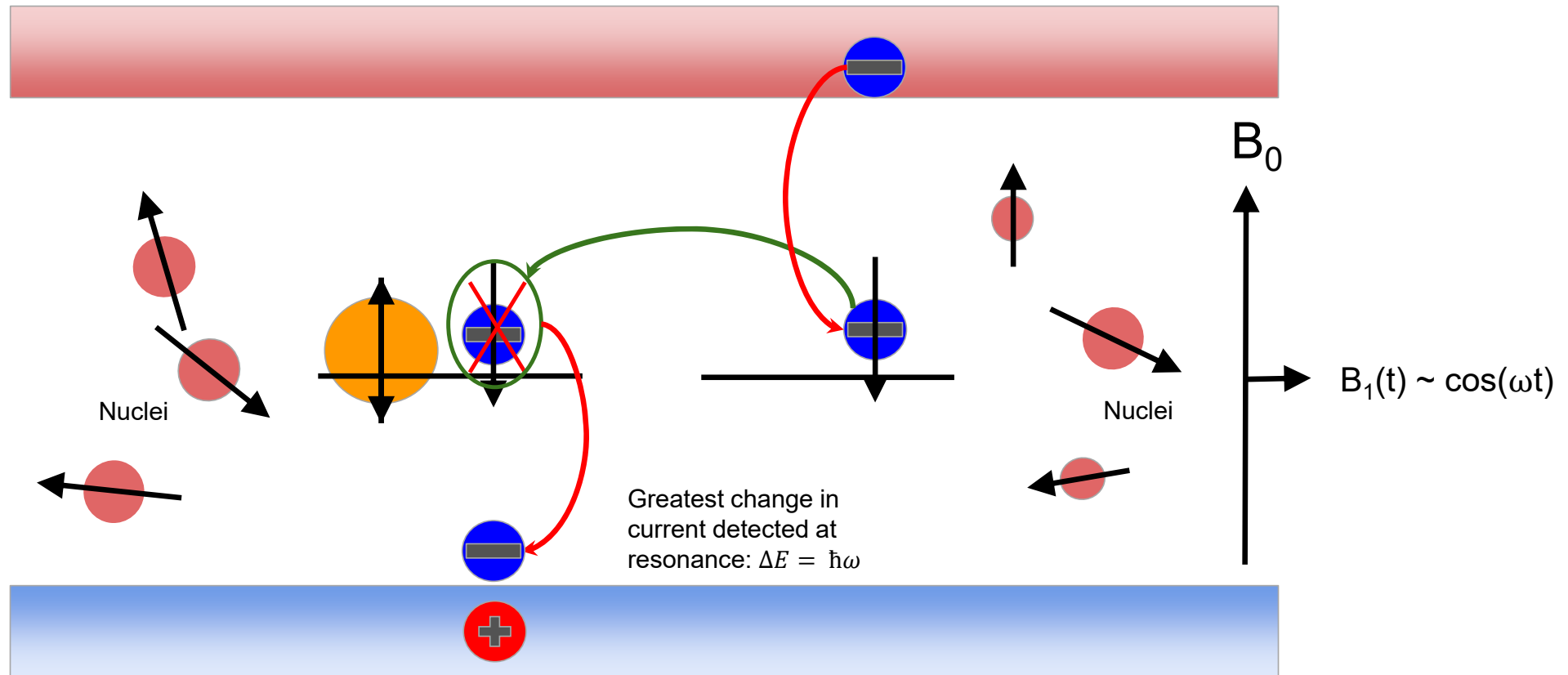
*features  
depend on  
rates as well as  
hyperfine fields*



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[illegible]

# Electrically Detected Magnetic Resonance (EDMR)



# Simulation of EDMR and NZFMR - Lindblad Equations

$\vec{S}_d$  = Spin of deep level defect       $\vec{S}_e$  = Spin of electron at shallow level

$$\hat{H} = g\mu_B \underbrace{\left(\vec{B}_0 + \vec{B}_1\right)}_{\text{Zeeman and Microwave B Fields}} \cdot \left(\vec{S}_d + \vec{S}_e\right) + \vec{S}_d \cdot \underbrace{\sum \overleftrightarrow{A}_i \cdot \vec{I}_i}_{\text{Deep level nuclear bath}} + \vec{S}_e \cdot \underbrace{\sum \overleftrightarrow{A}_j \cdot \vec{I}_j}_{\text{Shallow level nuclear bath}}$$

$$\partial_t \hat{\rho}(t) = -\underbrace{\frac{i}{\hbar} \left[ \hat{H}(t), \hat{\rho}(t) \right]}_{\text{Schrödinger Equation (coherent evolution)}} + \underbrace{\sum_i k_i \left( \hat{L}_i \hat{\rho}(t) \hat{L}_i^\dagger - \frac{1}{2} \left\{ \hat{L}_i^\dagger \hat{L}_i, \hat{\rho}(t) \right\} \right)}_{\text{Hopping of Transport Electron and Quantum Noise}}$$



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## Comparing Simulation to Experiment (Signal)

$$I(B_0) \propto \text{Tr}[\hat{P}_S \hat{\rho}_{ss}] = \rho_S$$

$$\text{Signal}(B_0) \equiv \partial_{B_0} I(B_0)$$

Magnetic field derivative of singlet spin population in the steady-state is proportional to the experimental signal measured by Lenahan group

## Computational Difficulties of Nuclear Baths in GaN

$^{69}\text{Ga}$  (60% n.a.),  $^{71}\text{Ga}$  (40% n.a.) have 4 states/nuclei ( $I=3/2$ )

Nitrogen vacancy nuclear bath involves  $\geq 4^4 = \mathbf{256}$  quantum states

$^{14}\text{N}$  (100% n.a.) have 3 states/nuclei ( $I=1$ )

Gallium Vacancy nuclear bath involves  $\geq 3^4 = \mathbf{81}$  quantum states

Number of matrix equations scales with nuclear bath - **approximations needed**



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# V(N) NZFMR Fit to Commercial Device Data

Classical nuclear hyperfine averaging theory  
for both isotopes of Gallium:

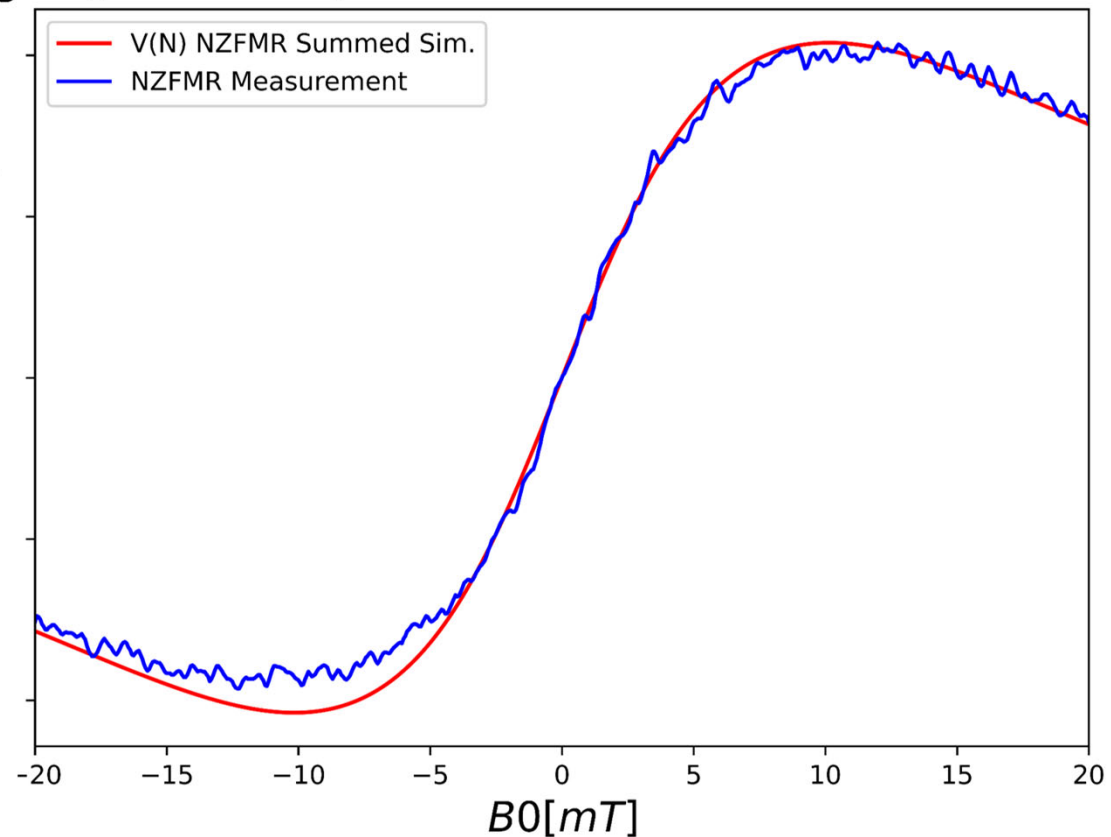
$$\text{Signal}(B_0) = 0.6 \times \text{Signal}_{69Ga}(B_0) + 0.4 \times \text{Signal}_{71Ga}(B_0)$$

$$A_{\perp,eff} = A_{zz,eff} = 28 \text{ MHz}$$

Hyperfine coupling calculations will be  
described towards end of presentation

Defect coherence time:  $T_2 = 20 \text{ ns}$  (fit)

Signal[Arb. Units]

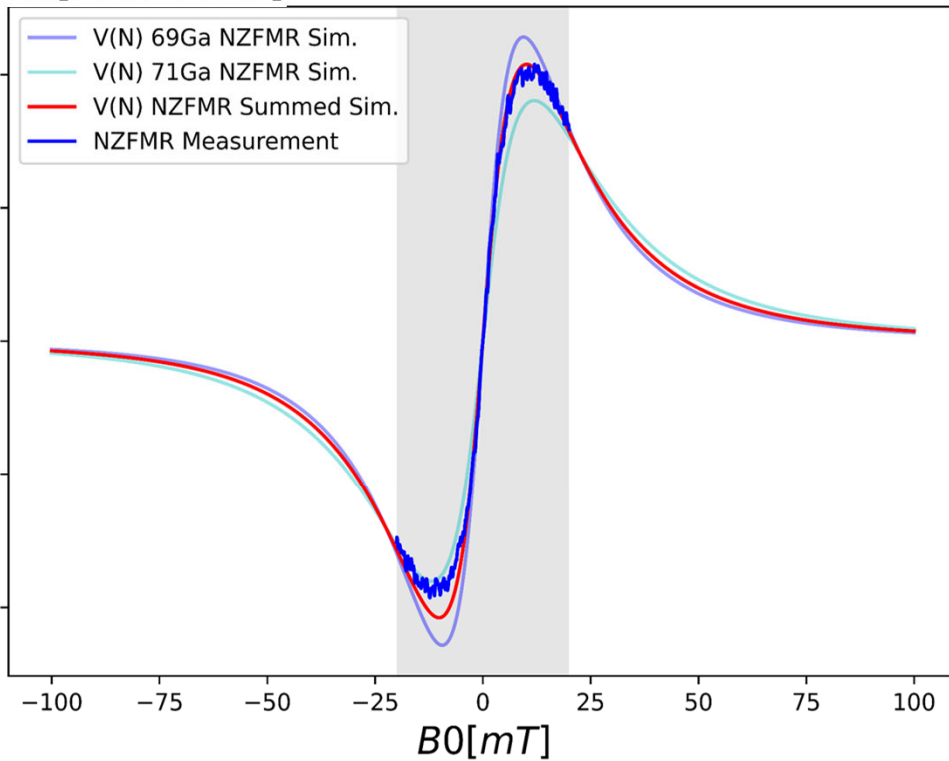


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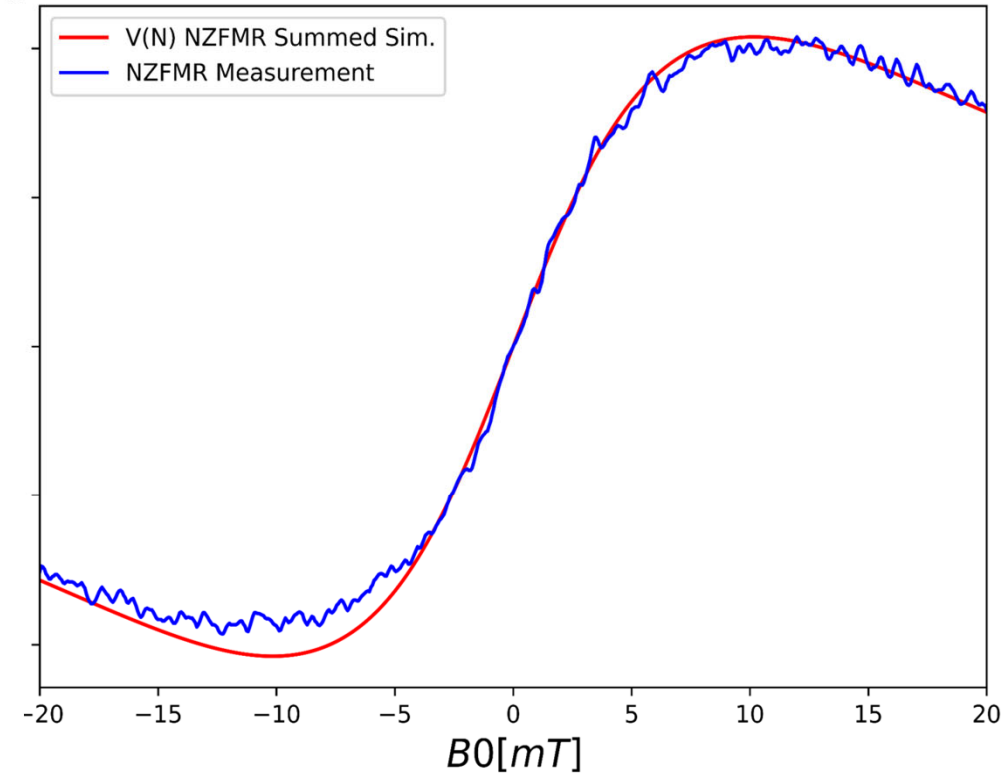


# V(N) NZFMR Fit to Commercial Device Data

Signal[Arb. Units]



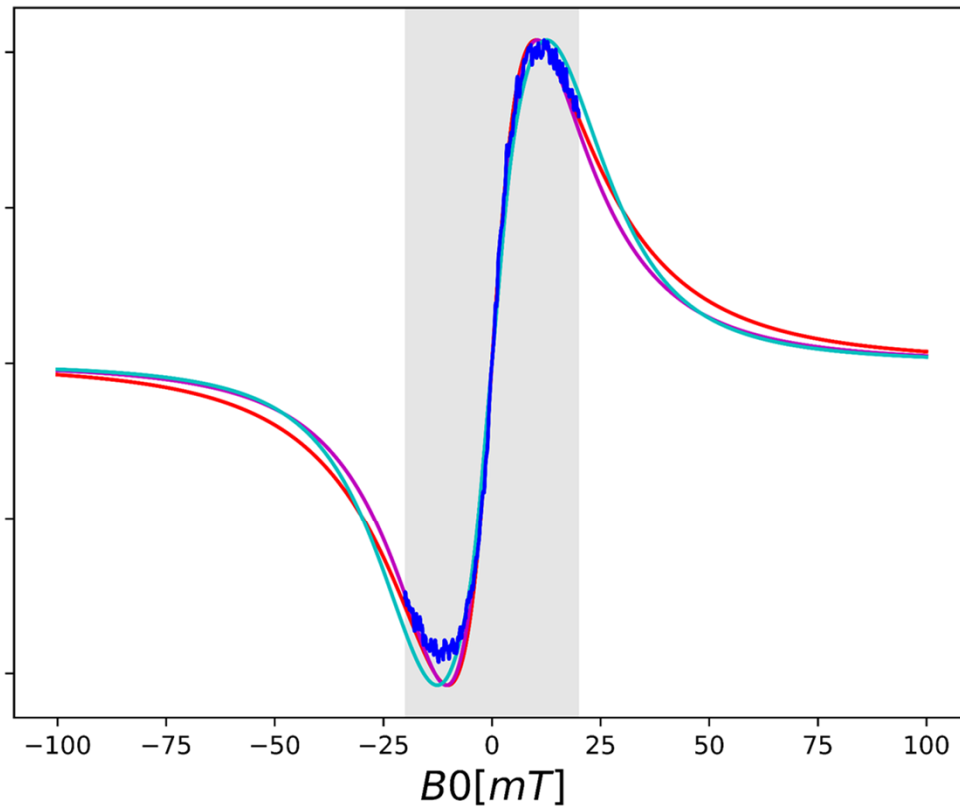
Signal[Arb. Units]



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# V(N) NZFMR Fit - Constraining Hyperfine Values

Signal[Arb. Units]



- V(N) NZFMR Sim.  $A = 3$  MHz,  $T_2 = 0.5$  ns
- V(N) NZFMR Sim.  $A = 28$  MHz,  $T_2 = 20$  ns
- V(N) NZFMR Sim.  $A = 110$  MHz,  $T_2 = \infty$
- V(N) NZFMR Data

Simulation constrains upper bound of hyperfine coupling in data:

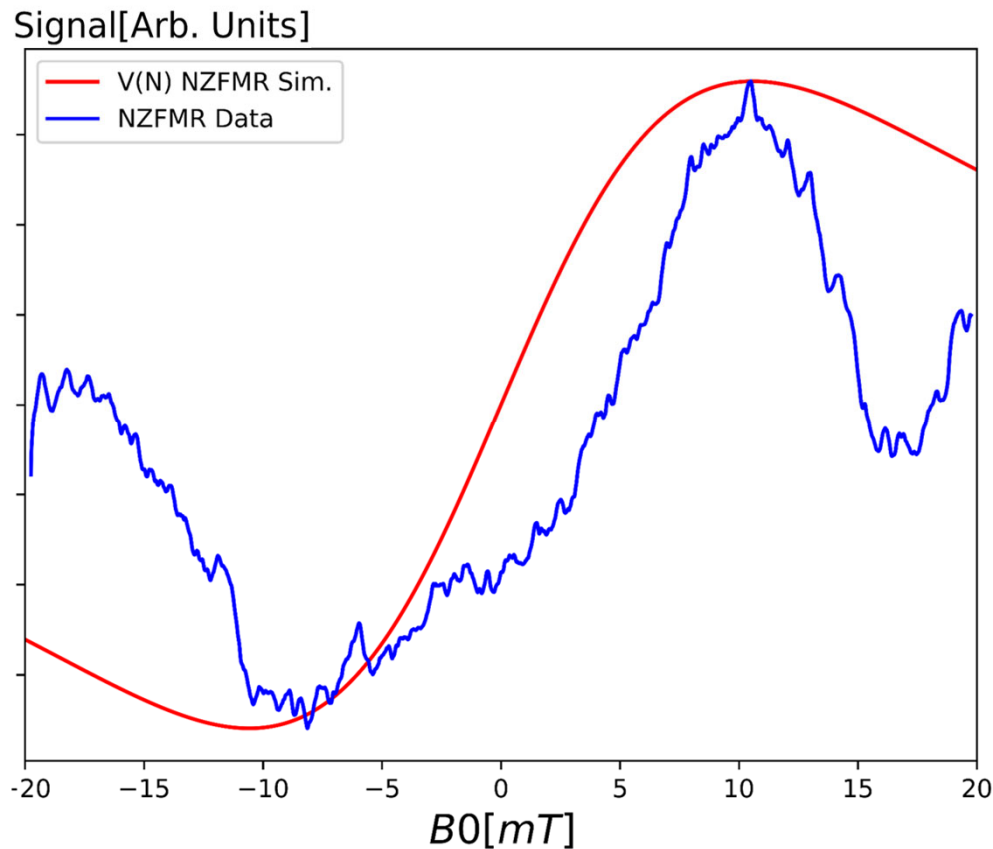
$$A_{\perp,eff} = A_{zz,eff} \leq \sim 100 \text{ MHz}$$

This constraint is consistent with our calculation of the hyperfine coupling of V(N) (28 MHz)



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# V(N) NZFMR Fit to Penn State Device Data



NZFMR simulation based on V(N) is not consistent with the NZFMR measurement on this device.

Other defects playing a role?



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# V(Ga) EDMR Fit to Penn State Device Data

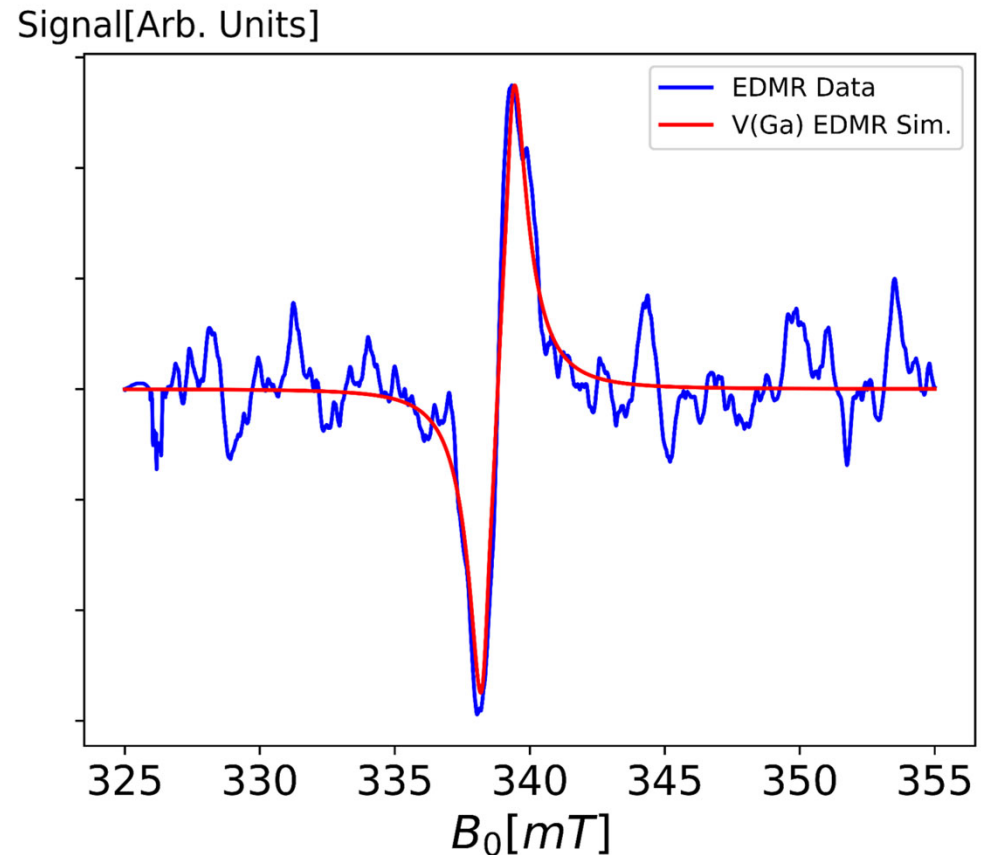
EDMR signal is dominated by the  $A_{zz}$  component of nitrogen on axial site:

$$A_{zz}^a = -10.7 \text{ MHz}$$

Contribution from basal nitrogens is negligible:  $A_{zz}^b = 0.17 \text{ MHz}$

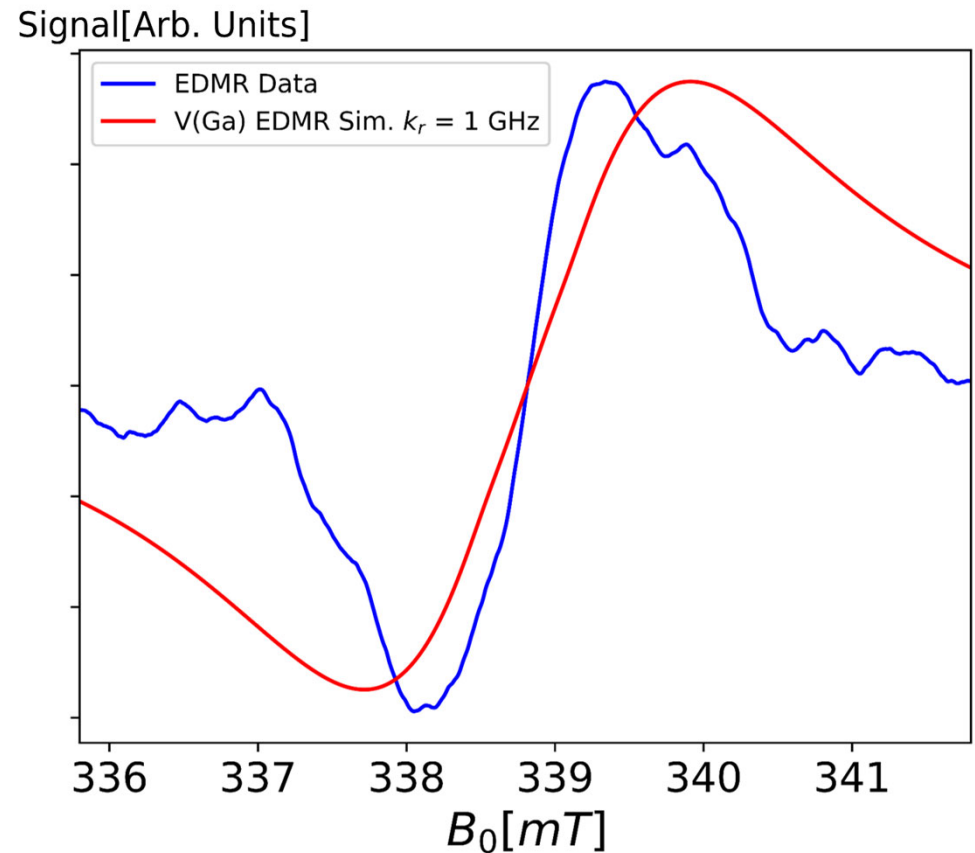
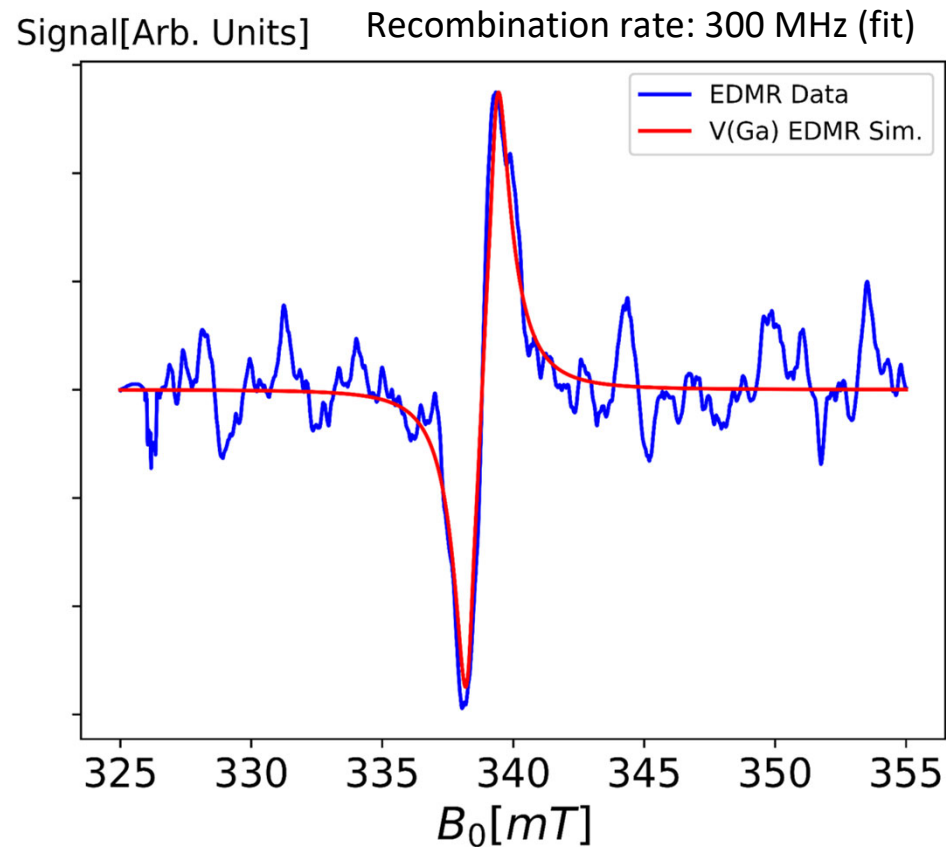
Hyperfine couplings calculated using tight-binding Green's functions as described later

Recombination rate: 300 MHz (fit)



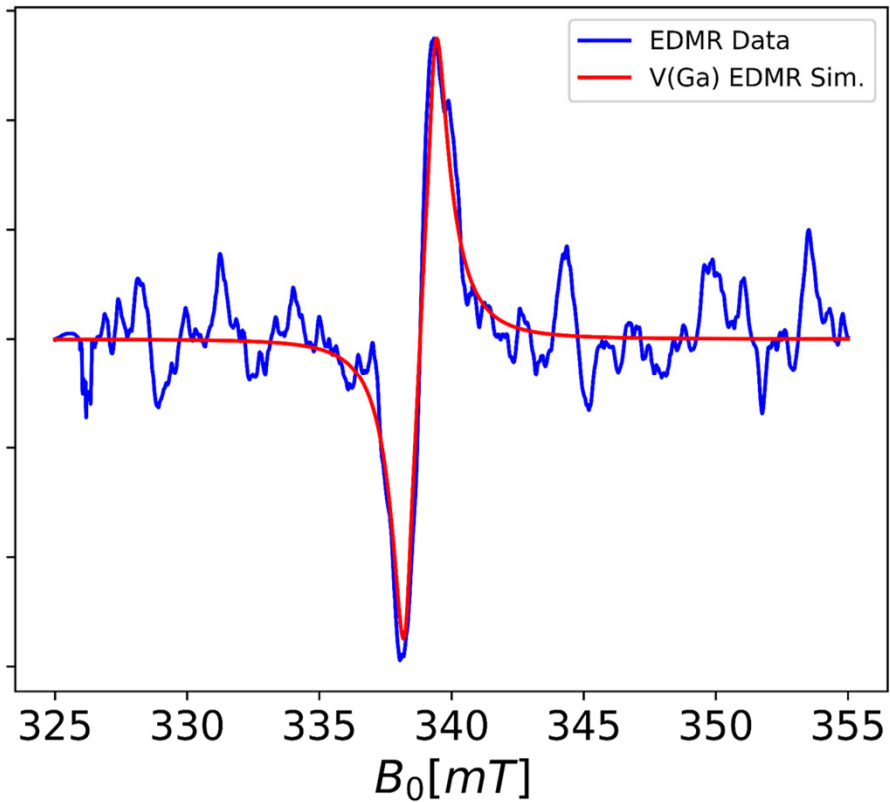
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# V(Ga) EDMR Fit – Vary Recombination Rate

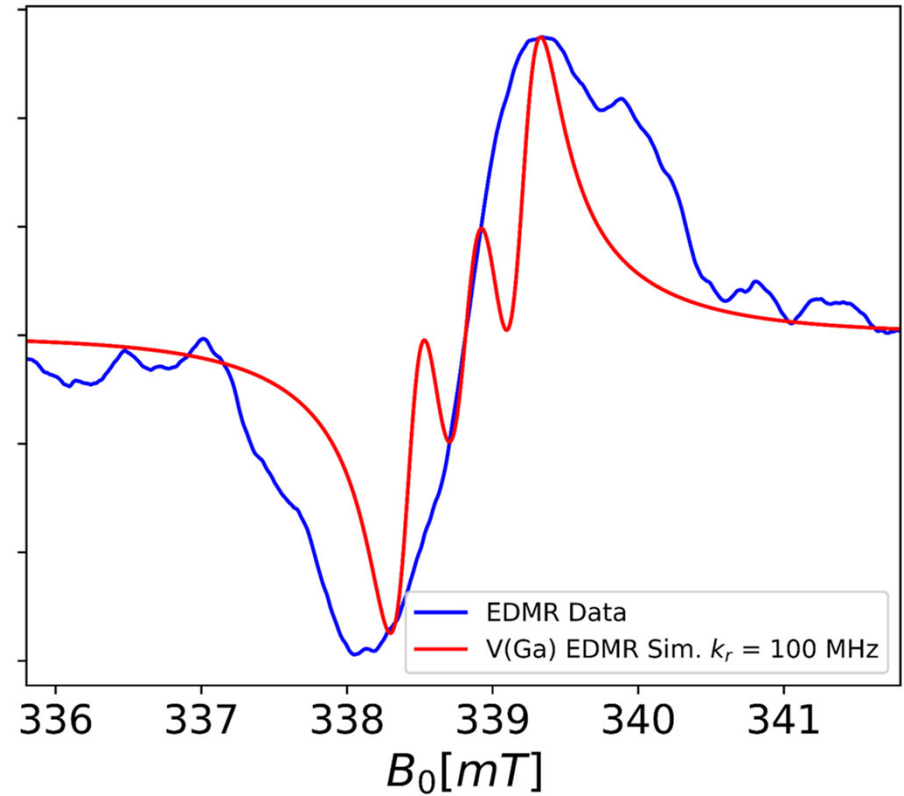


# V(Ga) EDMR Fit – Vary Recombination Rate

Signal[Arb. Units]



Signal[Arb. Units]



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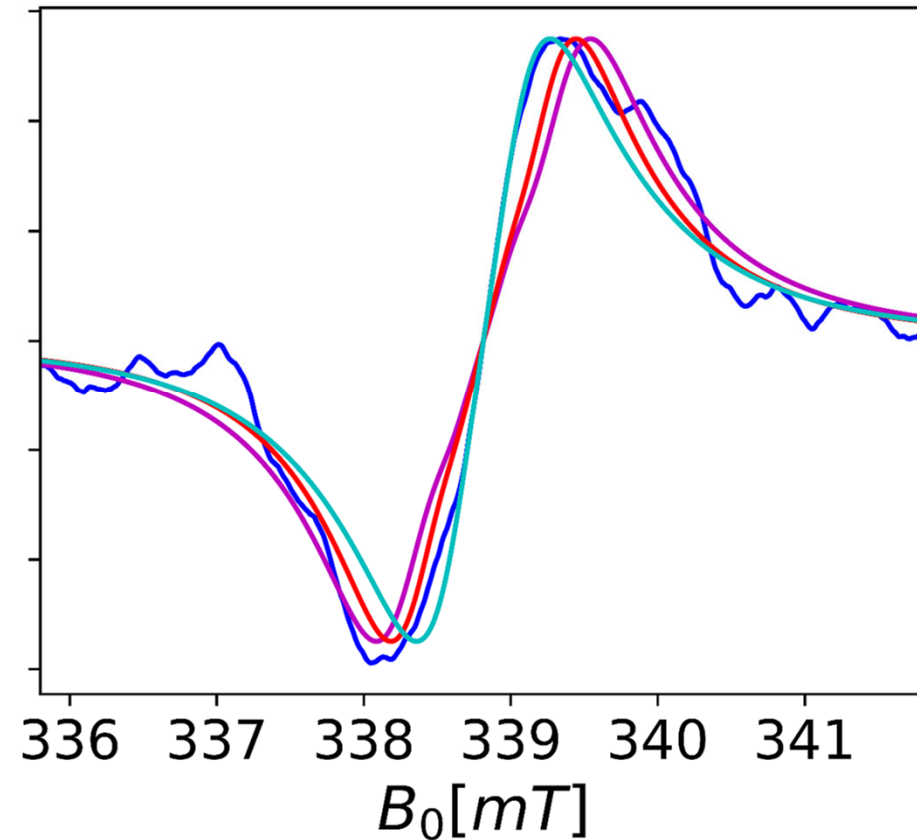
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# V(Ga) EDMR Fit – Vary Axial Hyperfine

Signal[Arb. Units]



- EDMR Data
- V(Ga) EDMR Sim.  $A_{zz} = -13$  MHz,  $k_r = 330$  MHz
- V(Ga) EDMR Sim.  $A_{zz} = -10.7$  MHz,  $k_r = 300$  MHz
- V(Ga) EDMR Sim.  $A_{zz} = -4$  MHz,  $k_r = 350$  MHz

Simulation constrains upper bound of hyperfine coupling in data:

$$|A_{zz}^a| \leq 13 \text{ MHz}$$

This constraint is consistent with our calculation of the axial hyperfine coupling of V(Ga) (-10.7 MHz)



# Tight-Binding Green's Functions

Defects in bulk can be efficiently solved via the Dyson Eqn[1,2,3],

$$\hat{G} = (1 - \hat{g}\hat{V}')^{-1}\hat{g}$$

## 1) Homogeneous

$$\hat{g}(\delta\mathbf{R}; \omega) = \int_{BZ} d^3k [\omega - \hat{H}(\mathbf{k})]^{-1} e^{ik \cdot \delta\mathbf{R}}$$

## 2) Inhomogeneous

$$\hat{M}_{nn} = (1 - \hat{g}_{nn}\hat{V}'_{nn})^{-1}$$

$$\hat{G}_{nn} = \hat{M}_{nn}\hat{g}_{nn}$$

$$\hat{G}_{ff} = \hat{g}_{ff} + \hat{g}_{fn}\hat{V}'_{nn}\hat{M}_{nn}\hat{g}_{nf}$$

with,

$$\hat{V}' = \begin{pmatrix} \hat{V}'_{nn} & 0 \\ 0 & 0 \end{pmatrix}$$

## 3 Observables

$$\eta(\mathbf{R}, \omega) = \frac{-1}{\pi} \text{Im}[\text{Tr}[\hat{G}(\mathbf{R}, \mathbf{R}; \omega)]]$$

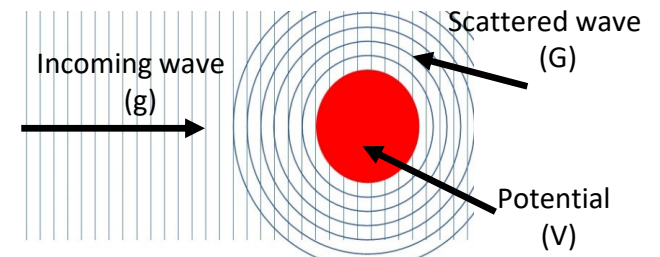
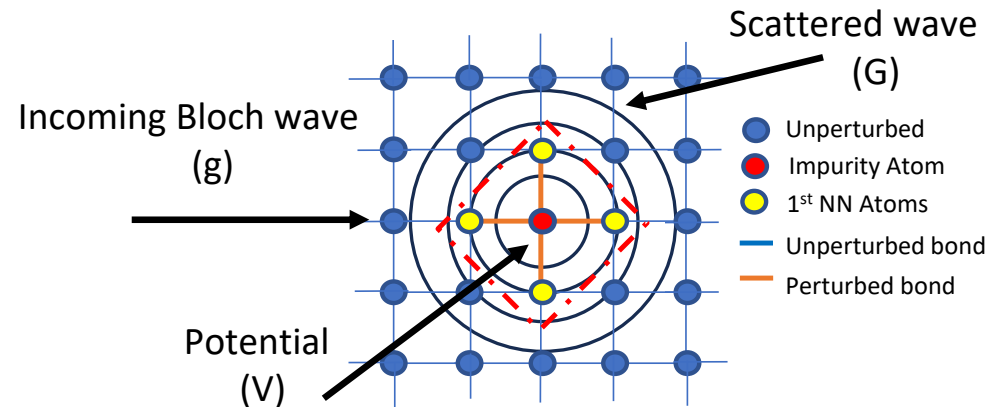
$$\langle \hat{A}_{iso} \rangle_{\omega} = \frac{-1}{\pi} \frac{8\pi}{3} A_0 |\psi_s(0)|^2 \hat{G}_{s,s}(\omega)$$

$$\langle \hat{A}_{ij} \rangle_{\omega} = \frac{-1}{\pi} \text{Im} [\text{Tr}[\hat{G}(\omega) A_0 \hat{r}^{-3} \hat{Q}_{ij}]]$$

with,

$$\hat{Q}_{ij} = 3\hat{r}_i\hat{r}_j - \delta_{ij}$$

$$A_0 = \frac{g_s g_N \mu_0 \mu_B}{4\pi \langle S_z \rangle}$$



[1]Koster/Slater PR 95, 1167 1954

[2]Hjalmarson et al. PRL. 44, 810 1980

[3]Tang/Flatté PRL 92, 047201 2004

[4]A. Koh and D. Miller, Atom. and Nuc. Data 33, 235 (1985)



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# Nitrogen Vacancy

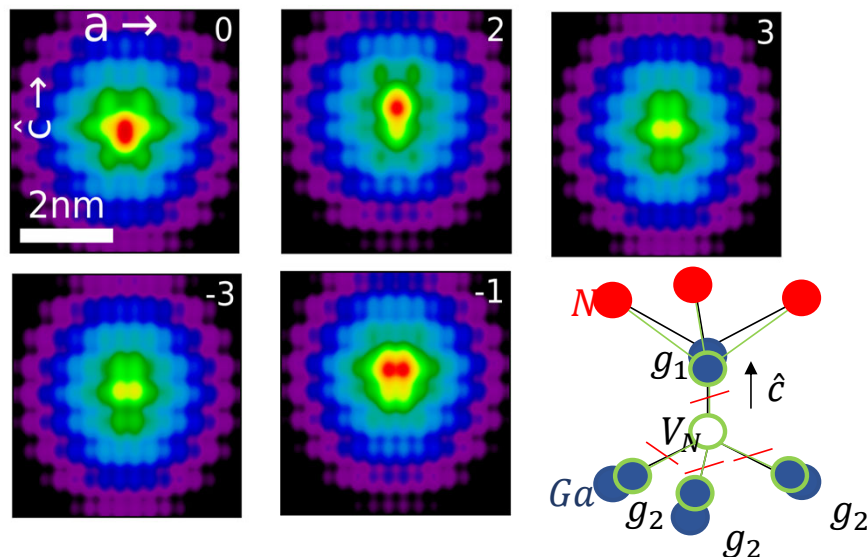
The  $V_N$  donor (31meV) is modelled using a ( $C_{3v}$  symmetric) potential,

$$\hat{V}' = \hat{E}_{Onsite} + \hat{V}_{NN}^{Strain} - \hat{V}_{NN}^{Bulk}$$

Where,

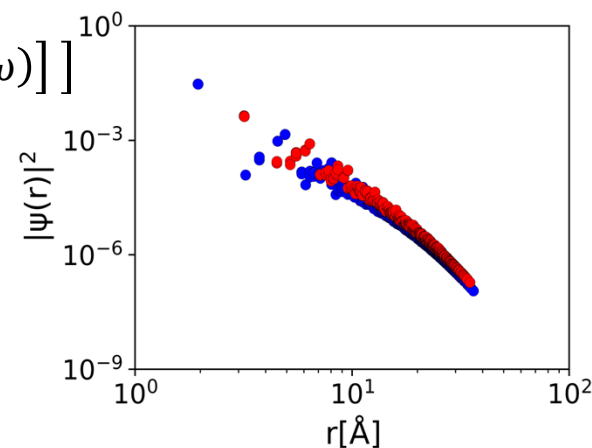
- $-\hat{V}_{NN}^{Bulk}$  creates four dangling Ga bonds as well as a non-interacting atomic nitrogen
- $\hat{E}_{Onsite}$  pushes the atomic nitrogen states up in energy, making them inaccessible
- $\hat{V}_{NN}^{Strain}$  allows the Ga to relax inward

The Nitrogen Vacancy wave function is highly isotropic and spread out over many atoms



## Local Density of States

$$\eta(\mathbf{R}, \omega) = \frac{-1}{\pi} \text{Im}[\text{Tr}[\hat{G}(\mathbf{R}, \mathbf{R}; \omega)]]$$



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# Nitrogen Vacancy Hyperfine

The  $V_N$  ( $C_{3v}$  symmetric) donor we model has s-like orbital character

We compute the strain dependent isotropic (Fermi Contact) hyperfine at  $\mathbf{R}_i$  as,

$$\langle \hat{A}_{iso} \rangle_{\omega}^i = \frac{-1}{\pi} \frac{8\pi}{3} A_0 |\psi_s(0)|^2 G_{ss}(\mathbf{R}_i, \mathbf{R}_i, \omega)$$

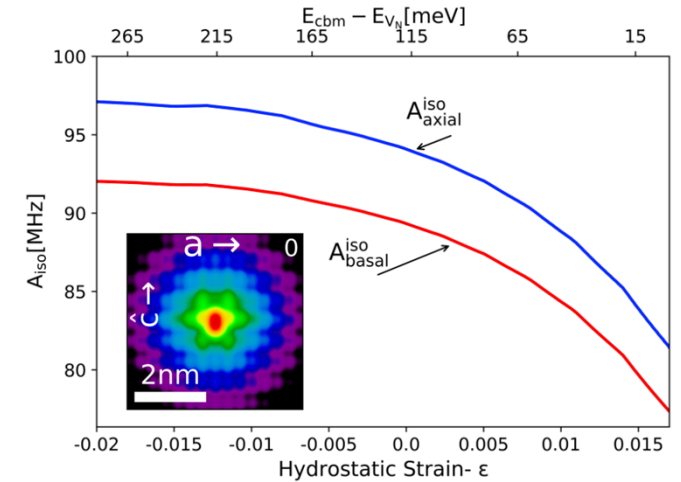
Defect Calculation

$G_{ss}(\mathbf{R}_i, \mathbf{R}_i, \omega) \Rightarrow \psi_s$  of wave function to LDOS for atom i

Atomic Constants[1]

$$A_0 = \frac{g_s g_N \mu_0 \mu_B}{4\pi \langle S_z \rangle}$$

$|\psi_s(0)|^2 \Rightarrow$  Fermi Contact Amp. from  $\psi_s$  at nucleus



[L,J,K,L]	$r_0[\text{\AA}]$	$A_{iso}[\text{MHz}]$
<b>1NN Axial - Gallium</b>		
[0, 0, 0, 1]	1.9540	80.6125
<b>1NN Basal - Gallium</b>		
[0, $\bar{1}$ , $\bar{1}$ , 3], [ $\bar{1}$ , 0, $\bar{1}$ , 3], [0, 0, $\bar{1}$ , 3]	1.9487	84.8936
<b>2NN - Nitrogen</b>		
$[\bar{1}$ , 0, 0, 2], [0, 0, $\bar{1}$ , 2], [0, $\bar{1}$ , 0, 2]	3.1798	2.1615
$[\bar{1}$ , 0, $\bar{1}$ , 2], [0, 0, 0, 2], [0, $\bar{1}$ , $\bar{1}$ , 2]		
[0, $\bar{1}$ , 0, 0], [ $\bar{1}$ , 0, 0, 0], [ $\bar{1}$ , 1, 0, 0]	3.1890	2.1684
[0, 1, 0, 0], [1, 0, 0, 0], [1, $\bar{1}$ , 0, 0]		

[1]A. Koh and D. Miller, Atom. and Nuc. Data 33, 235 (1985)



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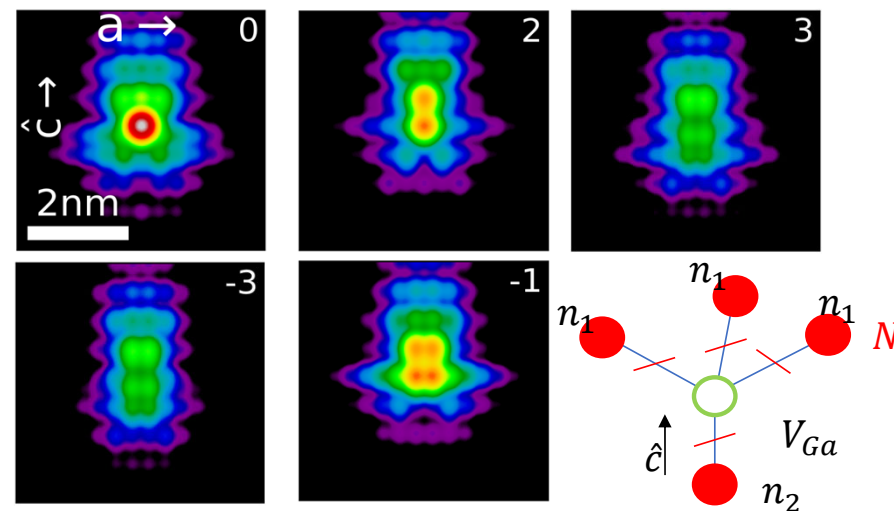
# Gallium Vacancy

The  $V_{Ga}$  Acceptor (238meV) is modelled using the ( $C_{3v}$  symmetric) potential,

$$\hat{V}' = \hat{E}_{Onsite} - \hat{V}_{NN}^{Bulk}$$

Where,

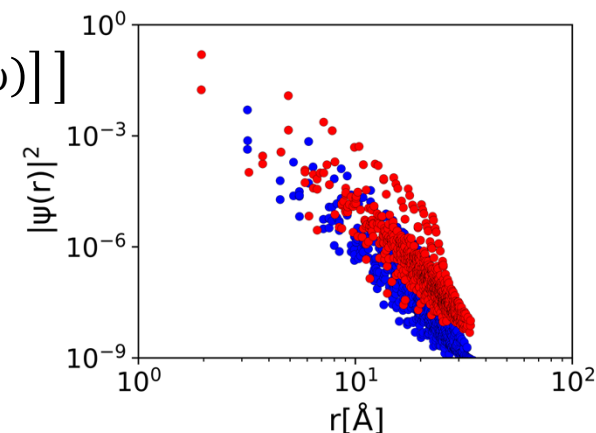
- $-\hat{V}_{NN}^{Bulk}$  creates four dangling N bonds and one free atomic gallium
- $\hat{E}_{Onsite}$  pushes the atomic nitrogen states up in energy, making them inaccessible



## Local Density of States

$$\eta(\mathbf{R}, \omega) = \frac{-1}{\pi} \text{Im}[\text{Tr}[\hat{G}(\mathbf{R}, \mathbf{R}; \omega)]]$$

The gallium vacancy wave function is highly anisotropic with a spatial decay with a much shorter range than the nitrogen vacancy.



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# Gallium Vacancy Hyperfine

The  $V_{Ga}$  ( $C_{3v}$  symmetric) acceptor we model has p-like orbital character.

We compute the anisotropic orbital hyperfine at  $\mathbf{R}_i$  as,

$$\langle \hat{A}_{ij} \rangle_{\omega}^q = \frac{-1}{\pi} \text{Im} \left[ \sum_{\beta\beta'} G_{\beta\beta'}(\mathbf{R}_q, \mathbf{R}_q, \omega) A_0^{\beta} \langle r^{-3} \rangle_{\beta} Q_{\beta\beta'} \right]$$

Defect Calculation

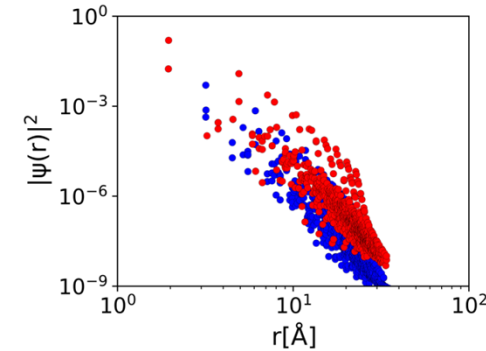
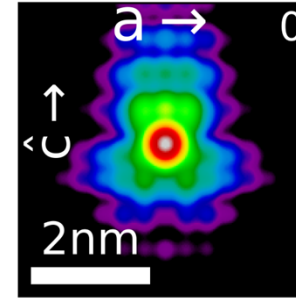
$G_{\beta\beta'}(\mathbf{R}_q, \mathbf{R}_q, \omega) \Rightarrow \psi_s$  of wave function to LDOS for atom q

Tabulated Constants

$\hat{Q}_{ij} = 3\hat{r}_i\hat{r}_j - \delta_{ij} \Rightarrow$  Quadrupole moment tensor

$$A_0 = \frac{g_s g_N \mu_0 \mu_B}{4\pi \langle S_z \rangle} [1]$$

$\langle r^{-3} \rangle_{\beta} \Rightarrow$  Expectation of radial decay of orbital- $\beta$  [1]



[L,J,K,L]	$r_0[\text{\AA}]$	$A_{qq}[\text{MHz}]$	$[u_x, u_y, u_z]_q$
<b>1NN Axial - Nitrogen</b>			
[0, 0, 0, 0]	1.9540	-6.4265	[ 0.8610, 0.5086, 0.0000]
		-6.4265	[ 0.5086, -0.8610, 0.0000]
		23.7987	[-0.0000, -0.0000, 1.0000]
<b>1NN Basal - Nitrogen</b>			
[0, 0, 0, 2]	1.9487	-0.7025	[-1.0000, -0.0002, -0.0005]
		-0.7020	[-0.0006, 0.2956, 0.9553]
		2.6639	[ 0.0000, -0.9553, 0.2956]
[ $\bar{1}$ , 0, 0, 2]	1.9487	-0.7012	[-0.5000, 0.8660, 0.0002]
		-0.7007	[-0.2559, -0.1479, 0.9553]
		2.6591	[-0.8273, -0.4777, -0.2956]
[0, $\bar{1}$ , 0, 2]	1.9487	-0.7025	[ 0.5000, 0.8660, -0.0002]
		-0.7020	[ 0.2561, -0.1477, 0.9553]
		2.6639	[-0.8273, 0.4777, 0.2956]

[1] A. Koh and D. Miller, Atomic and Nuclear Physics, 33, 235 (1981)



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# Summary

Magnetic field effects on transport through junctions containing defects with spin provides insight into

- (1) hyperfine structure of the defect
- (2) electronic spin character of the defect
- (3) transport rates including recombination rates, generation, dissociation

Correlations between EDMR and NZFMR provides insight into any radiation-induced defects

- NZFMR and EDMR simulations validated for GaN devices, including those from Penn State
- Microscopic wave function extent and hyperfine fields for vacancies calculated
- Width and mixing features are fingerprints for recombination pathways

Next steps

- Analyze more device measurements, including those from radiation damage
- Complete hyperfine simulations with simulations of N and Ga antisites and interstitials



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# Theory of Classical Nuclear Hyperfine Averaging

1. Nuclear bath approximations

$$\overleftrightarrow{\mathbf{A}} = \begin{pmatrix} A_{xx} & A_{xy} & A_{xz} \\ A_{xy} & A_{yy} & A_{yz} \\ A_{xz} & A_{yz} & A_{zz} \end{pmatrix} \approx \begin{pmatrix} A_{\perp} & 0 & 0 \\ 0 & A_{\perp} & 0 \\ 0 & 0 & A_{zz} \end{pmatrix} \quad \overleftrightarrow{\mathbf{A}}_i = \overleftrightarrow{\mathbf{A}}_{i'} = \overleftrightarrow{\mathbf{A}}_{eff}$$

1. Replace the nuclear bath with a discrete set of classical B-fields and respective weights calculated from  $\overleftrightarrow{\mathbf{A}}_{eff}$

$$\sum \overleftrightarrow{\mathbf{A}}_i \cdot \vec{I}_i \rightarrow \left\{ \vec{B}_i (A_{\perp}, A_{zz}), w_i \right\} \quad \hat{H} \rightarrow \left\{ \hat{H}_i (\vec{B}_i) \right\}$$

1. Calculate a weighted signal:

$$\text{Signal}(B_0) = \sum w_i \times \text{Signal}(B_0, \vec{B}_i)_i$$



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# Calculation of Classical Magnetic Fields

Simplified hyperfine tensor allows Hamiltonian to be written in block-diagonal form:

$$\hat{H} = \begin{pmatrix} \hat{H}_1 & 0 & 0 \\ 0 & \ddots & 0 \\ 0 & 0 & \hat{H}_N \end{pmatrix} \quad \overleftrightarrow{A}_{eff} = \begin{pmatrix} A_{\perp} & 0 & 0 \\ 0 & A_{\perp} & 0 \\ 0 & 0 & A_{zz} \end{pmatrix}$$

The hyperfine interaction in each sub-block is mapped onto a classical field:

$$\hat{H}_i = \vec{I} \cdot \overleftrightarrow{A}_{eff} \cdot \vec{S} \equiv g\mu_B \vec{B}_i \cdot \vec{S} \quad \vec{B}_i = \frac{1}{g\mu_B} \langle \propto A_{\perp}, 0, \propto A_{zz} \rangle$$

Proportionality constants depend on nuclear spin value



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# Calculation of Classical Magnetic Fields (Many Nuclei)

Identical hyperfine tensors allow for nuclear spin angular momenta to be added:

$$\overleftrightarrow{A}_i = \overleftrightarrow{A}_{i'} = \overleftrightarrow{A}_{eff} \quad \sum \overleftrightarrow{A}_i \cdot \vec{I}_i = \overleftrightarrow{A}_{eff} \cdot \vec{I}_{total}$$

For four nearest-neighbor nuclei,  $I_{total}$  takes a range of values with multiplicities  $\Omega$

Gallium vacancy:

$I_{total}$	4	3	2	1	0
$\Omega$	1	3	6	6	3

Nitrogen Vacancy:

$I_{total}$	6	5	4	3	2	1	0
$\Omega$	1	3	6	10	11	9	4



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# Calculation of Classical Magnetic Fields (Many Nuclei)

Each possibility of  $I_{total}$  corresponds to  $2 \times I_{total}$  classical magnetic fields

Distribution of classical field components is a function of  $I_{total}$

$$B_x(I_{total}) = \frac{2A_{\perp}}{g\mu_B} \times \left\{ \text{matrix elements of } \hat{I}_{total,x} \right\}$$

$$B_y(I_{total}) = 0$$

$$B_z(I_{total}) = \frac{A_{zz}}{g\mu_B} \times \left\{ \text{matrix elements of } \hat{I}_{total-1/2,z} \right\}$$

$$w_i = \frac{\Omega_i}{\text{Total \# of Fields}} \quad \text{Signal}(B_0) = \sum w_i \times \text{Signal}(B_0, \vec{B}_i)_i$$

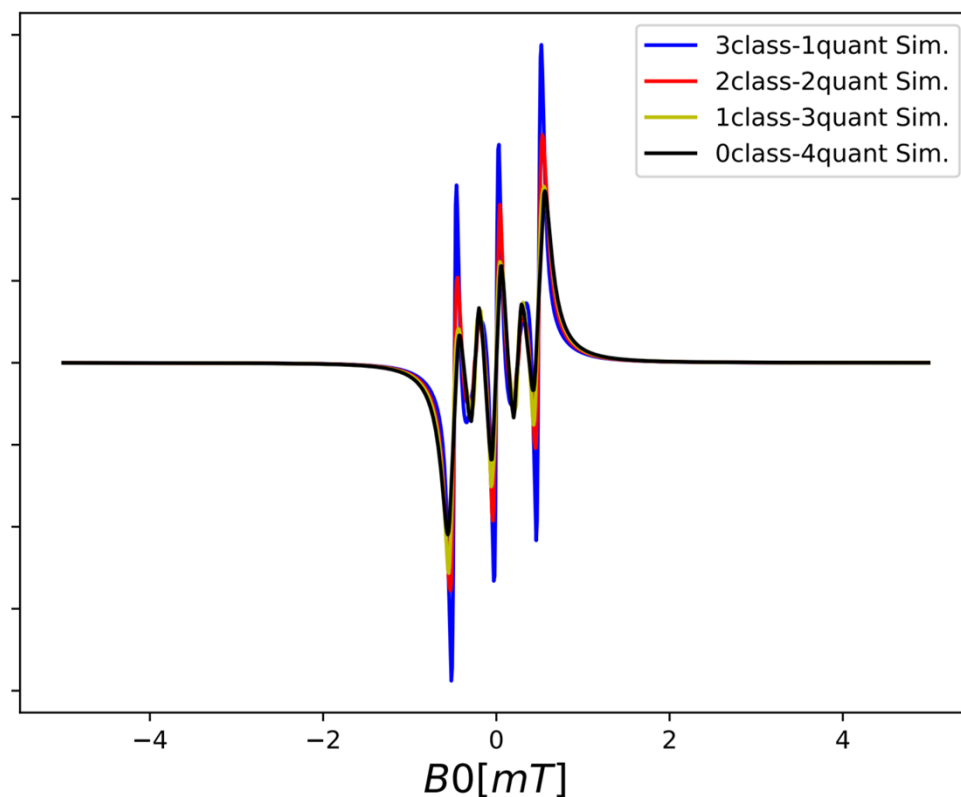


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# V(Ga) NZFMR - Varying “Quantumness”

Our tight-binding Green’s functions hyperfine calculations predict significantly different hyperfine couplings for axial vs. basal nitrogens to V(Ga).

(Right) classical nuclear hyperfine averaging on 0-3 basal nitrogens (**axial nitrogen is left fully quantum for all**):



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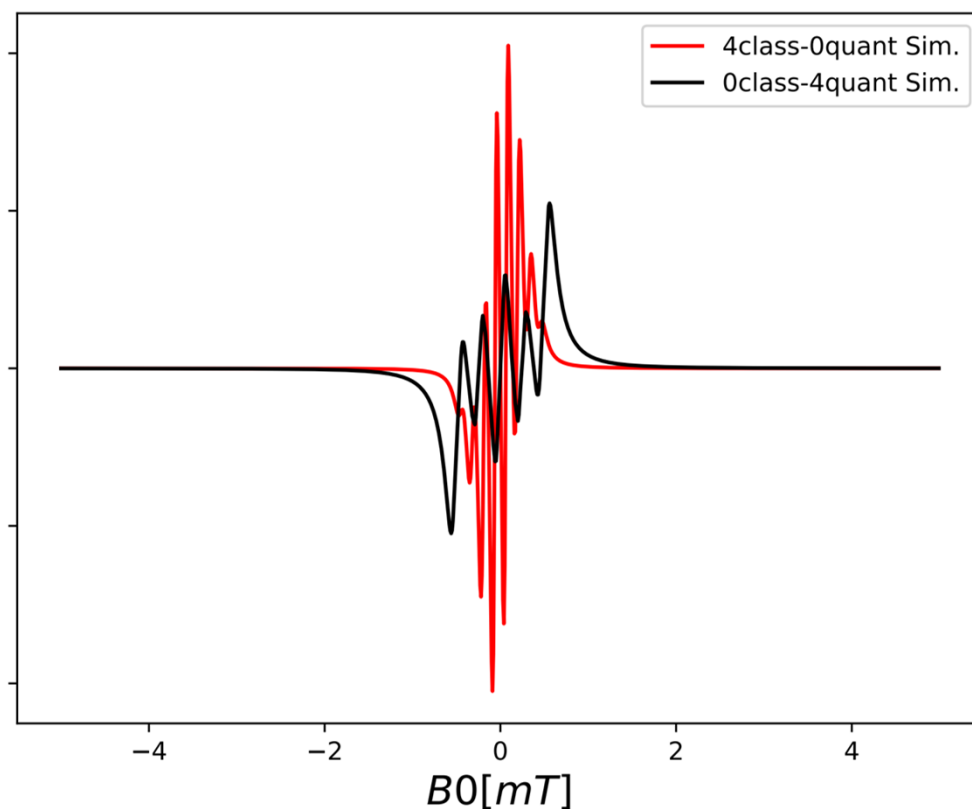


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# V(Ga) NZFMR - Varying “Quantumness”

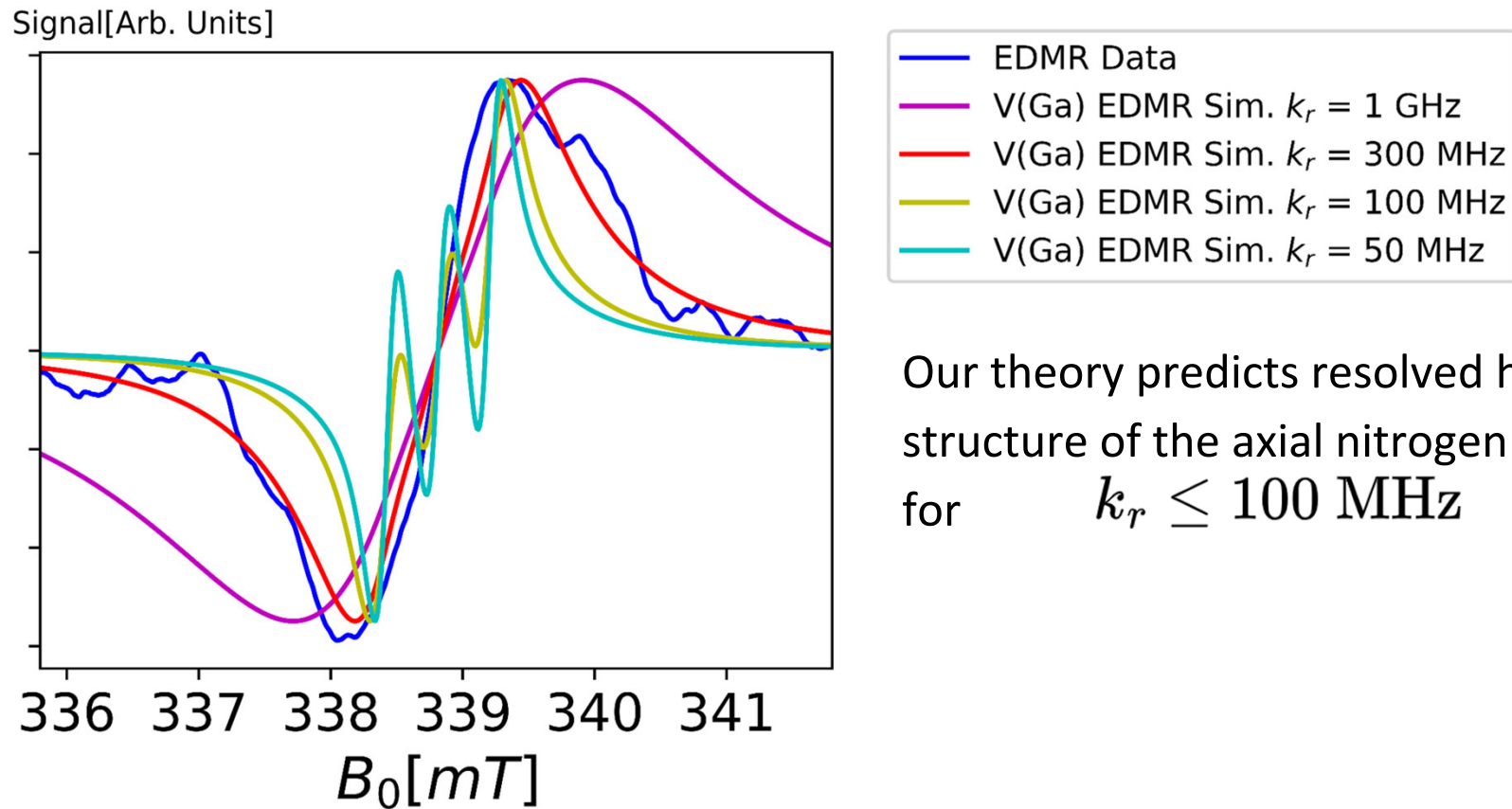
Our tight-binding Green’s functions hyperfine calculations predict significantly different hyperfine couplings for axial vs. basal nitrogens to V(Ga).

(Right) comparison to fully quantum simulation when the **axial nitrogen nuclear spin is also treated classically**:



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# V(Ga) EDMR - Varying Recombination Rate



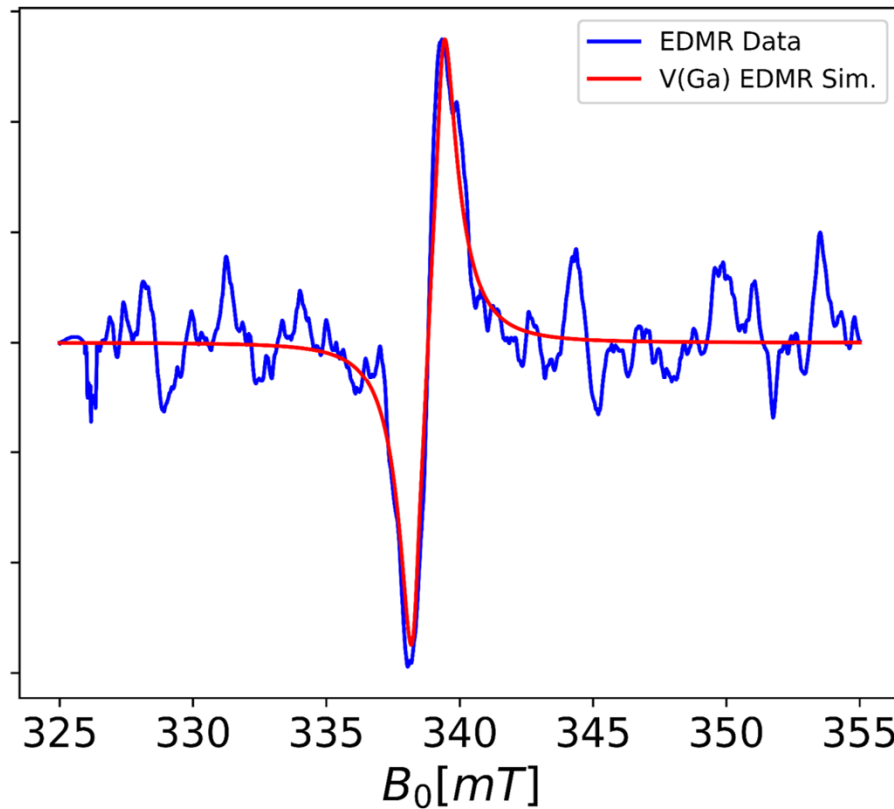
Our theory predicts resolved hyperfine structure of the axial nitrogen nuclear spin for  $k_r \leq 100$  MHz



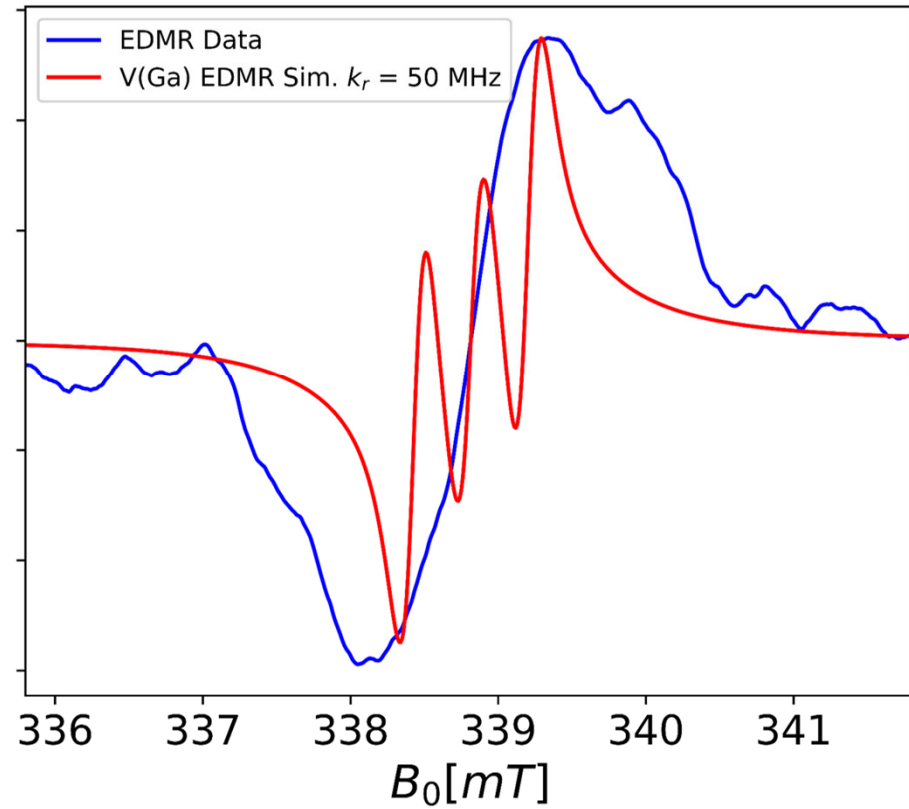
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# V(Ga) EDMR - Varying Recombination Rate

Signal[Arb. Units]

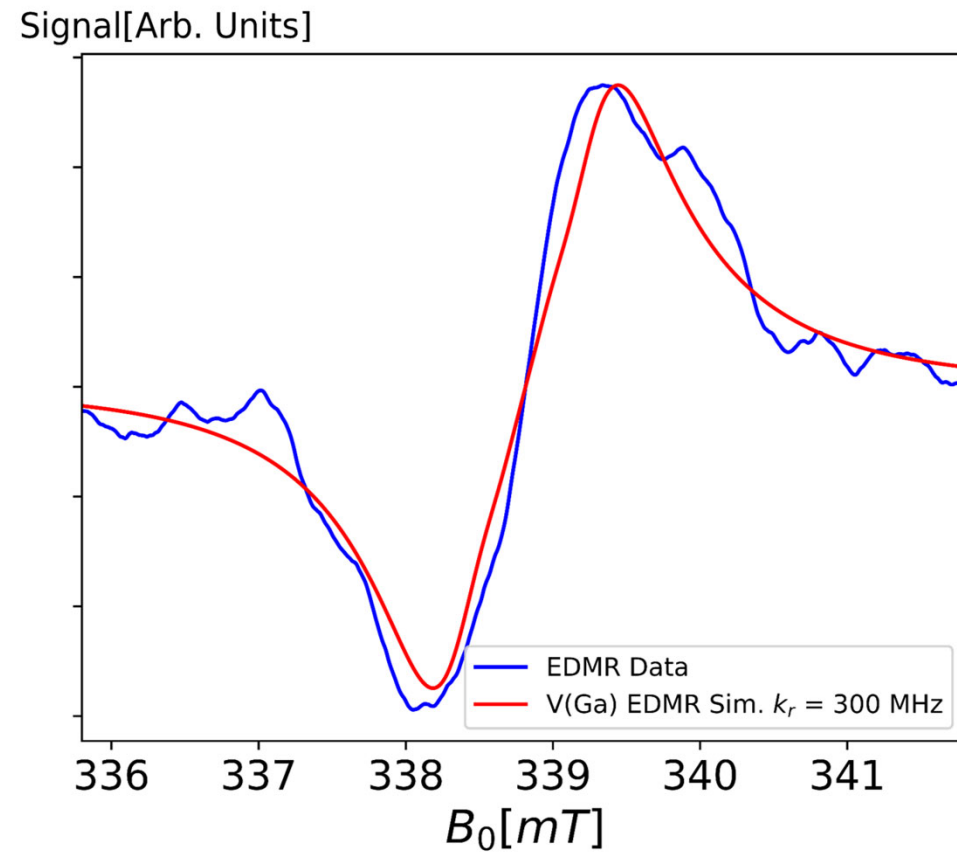
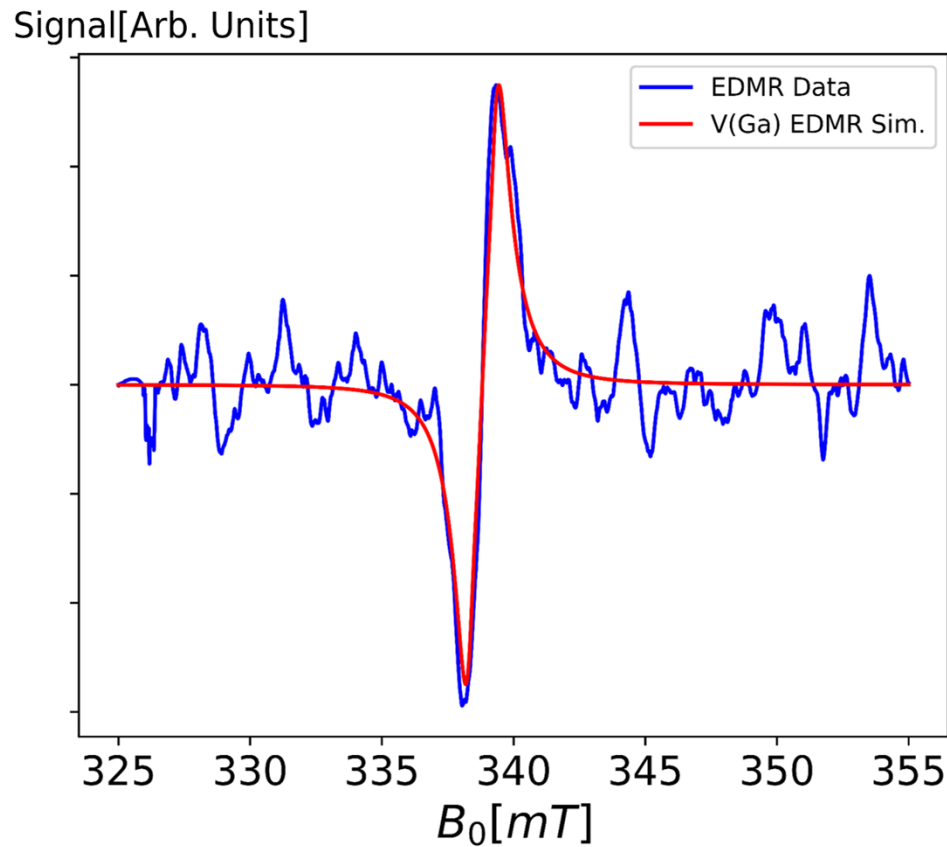


Signal[Arb. Units]



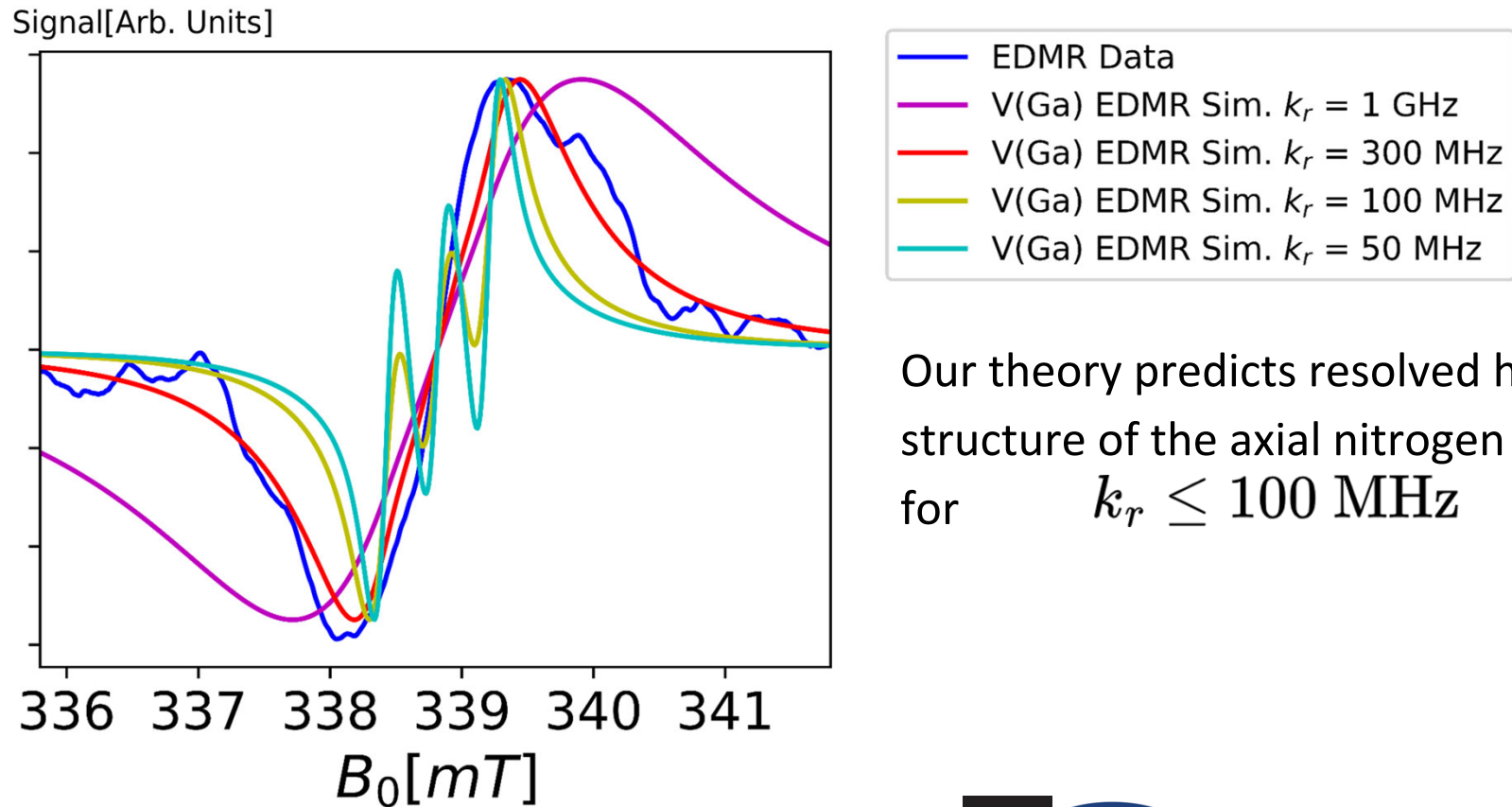
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Our theory predicts resolved hyperfine structure of the axial nitrogen nuclear spin for  $k_r \leq 100$  MHz



IOWA

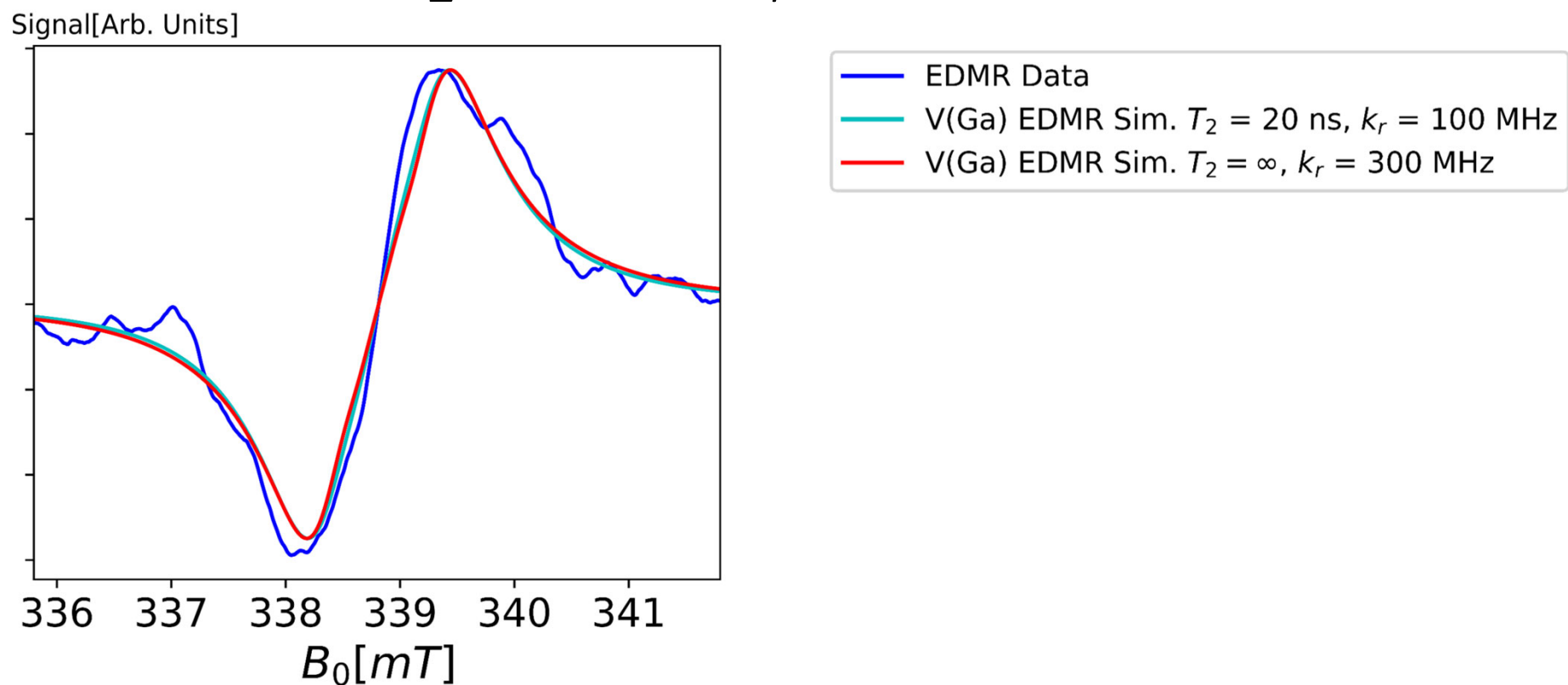
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# V(Ga) EDMR $T_2$ versus $k_r$



# Tight-Binding Green's Functions

Want solution to

$$[\hat{H}_{Bulk} + \hat{V}']\psi = E\psi$$

This can be solved efficiently as a scattering problem[1-3]

**Dyson Eq.:**  $\hat{G} = (1 - \hat{g}\hat{V}')^{-1}\hat{g}$

where,

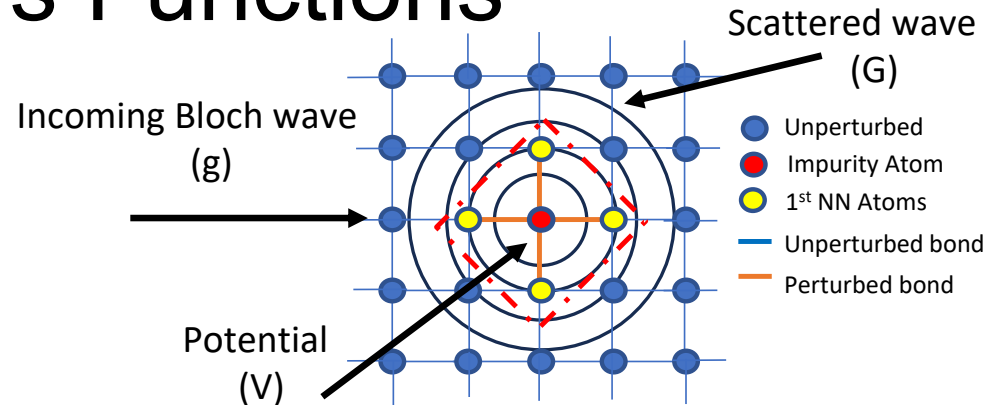
$$\hat{g}(\delta\mathbf{R}; \omega) = \int_{BZ} d^3k [\omega - \hat{H}(\mathbf{k})]^{-1} e^{i\mathbf{k} \cdot \delta\mathbf{R}}$$

Observables

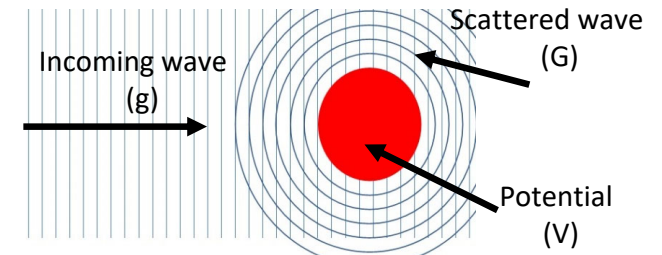
LDOS  $\eta(\mathbf{R}, \omega) = \frac{-1}{\pi} \text{Im}[\text{Tr}[\hat{G}(\mathbf{R}, \mathbf{R}; \omega)]]$

Isotropic Hyperfine  $\langle \hat{A}_{iso} \rangle_{\omega} = \frac{-1}{\pi} \frac{8\pi}{3} A_0 |\psi_s(0)|^2 \hat{G}_{s,s}(\omega)$

Anisotropic Hyperfine  $\langle \hat{A}_{ij} \rangle_{\omega} = \frac{-1}{\pi} \text{Im} [\text{Tr}[\hat{G}(\omega) A_0 \hat{r}^{-3} \hat{Q}_{ij}]]$



Think...

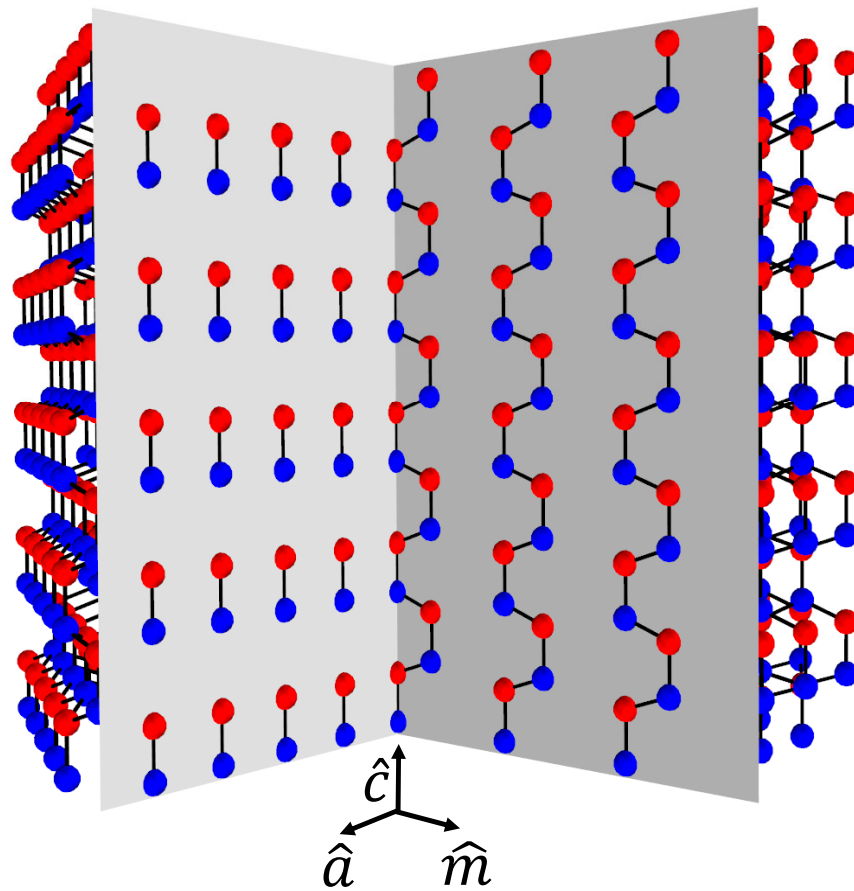


- [1]Koster/Slater PR 95, 1167 1954
- [2]Hjalmarson et al. PRL. 44, 810 1980
- [3]Tang/Flatté PRL 92, 047201 2004
- [4]A. Koh and D. Miller, Atom. and Nuc. Data 33, 235 (1985)

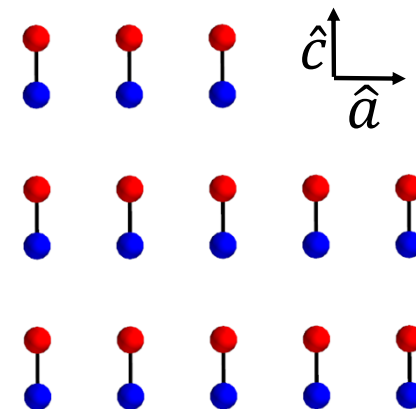


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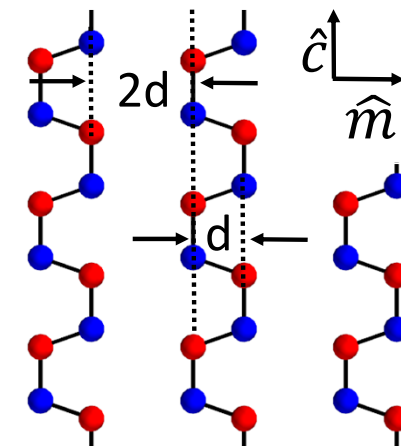
(b)



(c)



(d)



# Observables

$$\langle \hat{O} \rangle_{\omega} = \frac{-1}{\pi} \text{Im} \left[ \text{Tr} \left[ \hat{G}(\omega) \hat{O} \right] \right]$$

$$\hat{A}_{iso} = \frac{8\pi}{3} A_0 \sum_{\beta, \alpha=s} |\beta\rangle \langle \beta| \delta(\mathbf{r} - \mathbf{R}_q)$$

$$\hat{A}_{ij} = A_0 \frac{\hat{Q}_{ij}^{(2)}}{r^3}$$

$$\hat{Q}_{ij}^{(2)} = 3\hat{r}_i \hat{r}_j - \delta_{ij}$$

$$A_0 = g_s g_N \mu_0 \mu_B \mu_N / 4\pi \langle S_z \rangle$$

$$\eta(\mathbf{R}, \omega) = \frac{-1}{\pi} \text{Im} [\text{Tr} [\hat{G}(\mathbf{R}, \mathbf{R}; \omega)]]$$

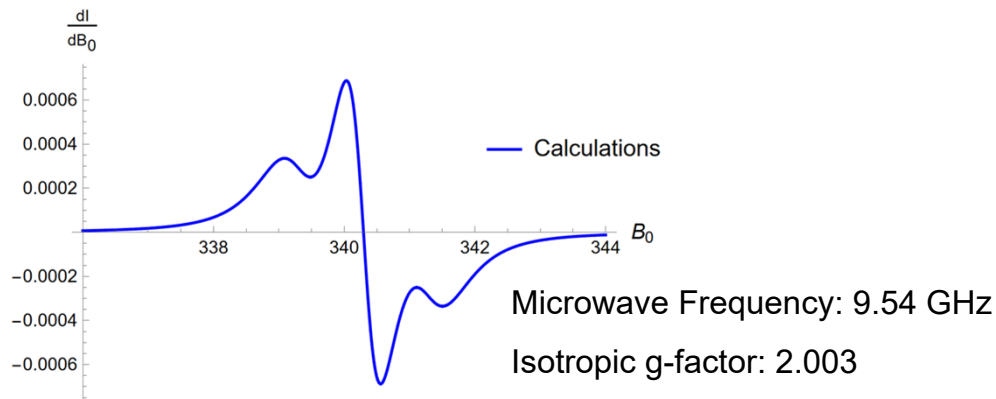
$$\langle \hat{A}_{iso} \rangle_{\omega} = \frac{-8}{3} A_0 \sum_q \text{Im} [\text{Tr} [G_{s,s}(\mathbf{R}_q, \mathbf{R}_q, \omega)]]$$

$$\langle A_{ij} \rangle_{\omega} = \frac{-1}{\pi} \text{Im} \left[ \sum_{\beta, \beta'} A_0^{\beta} G_{\beta', \beta}(\omega) \langle r^{-3} \rangle_{\beta', \beta} \langle \hat{Q}_{ij} \rangle_{\beta', \beta} \right]$$



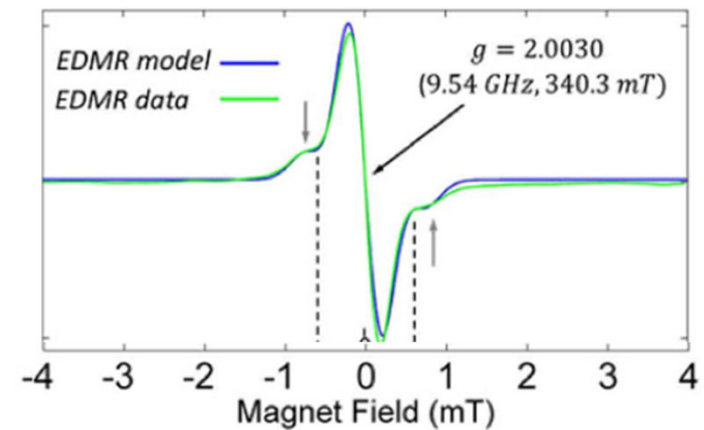
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# EDMR $V_{Si}^0$ (S=1) in 4H-SiC Simulation Results



Extracted Parameters:

- Axial Zero Field Splitting:  $2D = 57$  MHz
- Microwave B field strength: 0.1 mT
- $T_{2,d}^* \sim 25$  ns



*Sci Rep* **6**, 37077  
(2016)

Code is validated for these effects

The challenge of EDMR in GaN: large numbers of high-spin magnetic nuclei



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# Timeline and Milestones: Year 1

- (1) Simulation of nitrogen vacancies in GaN and their effect on EDMR and NZFMR. The nitrogen vacancies are spin  $\frac{1}{2}$  shallow donor states with known g tensors, and are likely radiation-induced defects.
- (2) Commencement of the AC bias simulations of spin-dependent trap-assisted tunneling (SDTAT) and spin-dependent recombination (SDR) currents. Defect parameters will be taken from the literature, and from Tuttle and Jin as their calculations become available.

**Milestone:** EDMR and NZFMR magnetic-field-dependent curves for N vacancies a range of device bias for GaN leakage currents.



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## Timeline and Milestones: Year 2

- (1) Simulation of Ga antisite defects in GaN and their effect on EDMR and NZFMR. These defects have been calculated to have several mid-gap states, but little is known experimentally about these levels and their spin configuration. These are also likely radiation-induced defects.
- (2) Completion of AC bias simulation formalism and test calculations of SDTAT and SDR. Inferences on what structures may make devices less sensitive to radiation.

**Milestone:** EDMR and NZFMR magnetic-field-dependent curves for Ga antisite defects for a range of device bias for GaN leakage currents. Results for AC bias simulations of SDTAT and SDR and input back into device design.



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