



Unified first-principle analysis of ultraintense laser-matter interactions: Theory, computations and experiments

Pavel Polynkin

College of Optical Sciences
University of Arizona
Tucson, Arizona

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Program goals:

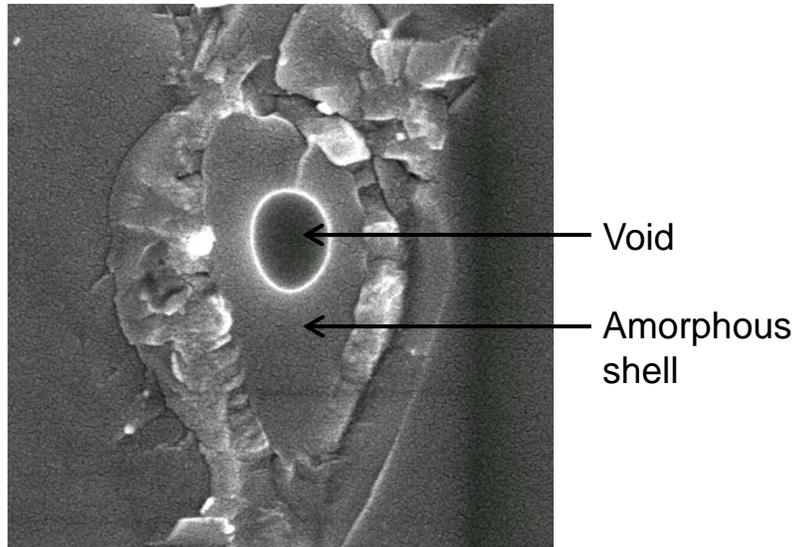
- 1. Devise first-principle models of the interaction of fs laser pulses with materials (both on surfaces and inside transparent materials); implement models in numerical codes**
- 2. Develop non-perturbative ionization models and incorporate them in the codes**
- 3. Conduct experiments to support and verify modeling:**
 - Pump-probe imaging of ablation with ultrashort probe (5 fs)**
 - Pump-probe imaging of ablation of microdroplets with XUV probe**
- 4. Experimentally study exotic ablation situations:**
 - Confined microexplosions inside transparent solids and on interfaces**
 - Ablation with ultrashort laser pulses ~5 fs**
 - Ablation with fs pulses in the wavelength range 200 nm – 2.6 μm**
 - Effects of pulse shaping in ablation**

First-principle models of fs laser-matter interactions

Model #1 – modeling high-NA fs beam propagating inside a dielectric

Non-paraxial Maxwell propagator coupled with rate equations for ionization and electron heating

Simulate first $<100\text{fs}$ \rightarrow lattice remains cold



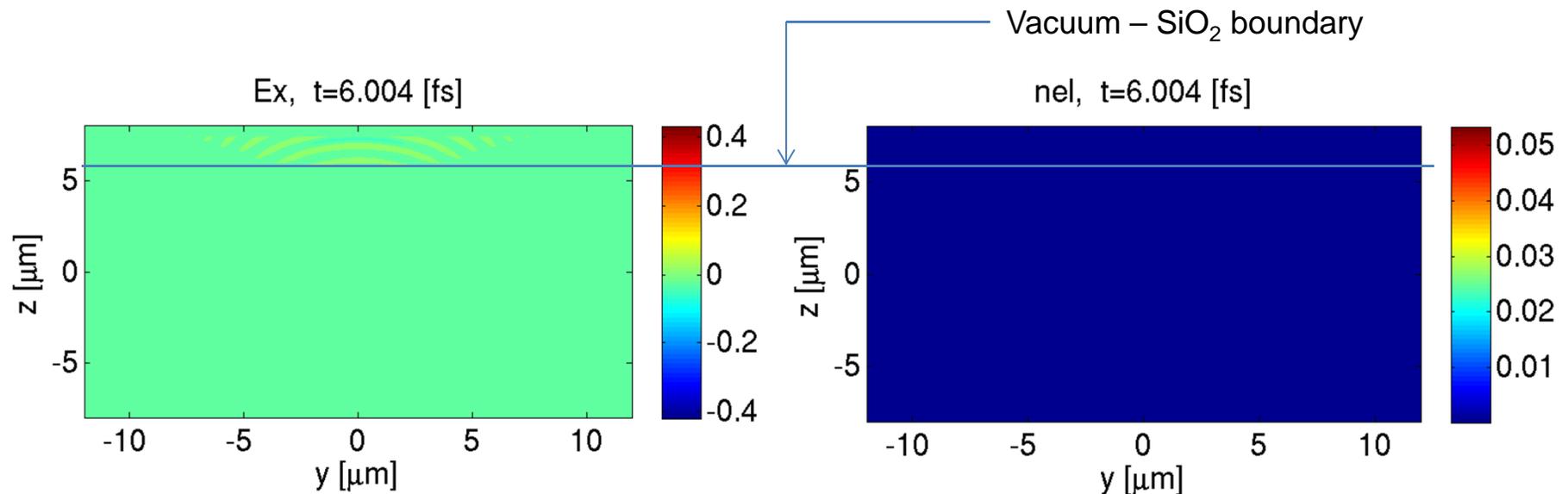
Practical goals:

- Compute distribution of energy absorbed inside dielectric
- Maximize absorbed energy via tailoring beam and pulse shapes
 - \rightarrow Create larger voids
 - \rightarrow Create more extreme pressures and temperatures

Computationally challenging – need to resolve significantly sub-wavelength spatial transients (moving skin layers ~ 10 nm – thick at max. ionization)

Preliminary results in full 3D – Brute force approach: Constant grid size < Skin depth

- Full 3D simulation
- 800nm wavelength, 100fs pulse
- Ionization limited at $n_e = 3 \cdot 10^{27} \text{ cm}^{-3}$ (~1.5 times critical density, skin depth = 175 nm)
- 32 processors, uniform 20 nm grid, 5 hours computation time

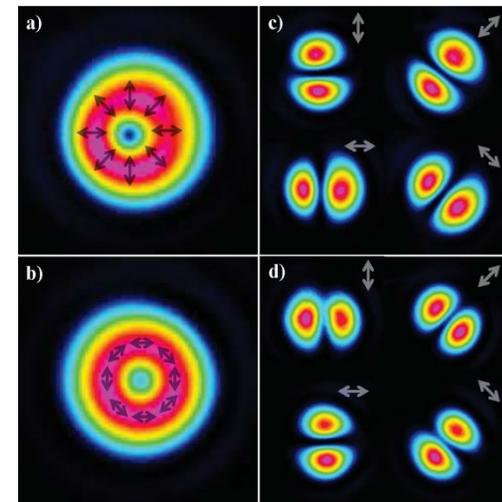


Model #1 – future work

- Brute force in 3D with full ionization is impractical: ~50 years/computation
- Approaches:
 - Variable (but static) grid across computational domain
 - Adaptive grid
 - 2D (x,z,t) - corresponds to cylindrical focusing, axial microexplosion
 - 2D (r,z,t) – corresponds to 3D with azimuthal or radial polarization, realizable through polarization beam shaping with S-plate

- S-plate is a micro-structured optical polarization converter
- Converts linear into azimuthal or radial polarizations
- Produces large longitudinal field in focus

M. Beresna, M. Gecevicius, P. Kazansky, T. Gertus
 “Radially polarized optical vortex converter created
 by femtosecond laser nanostructuring of glass”,
 APL **98**, 201101 (2011)



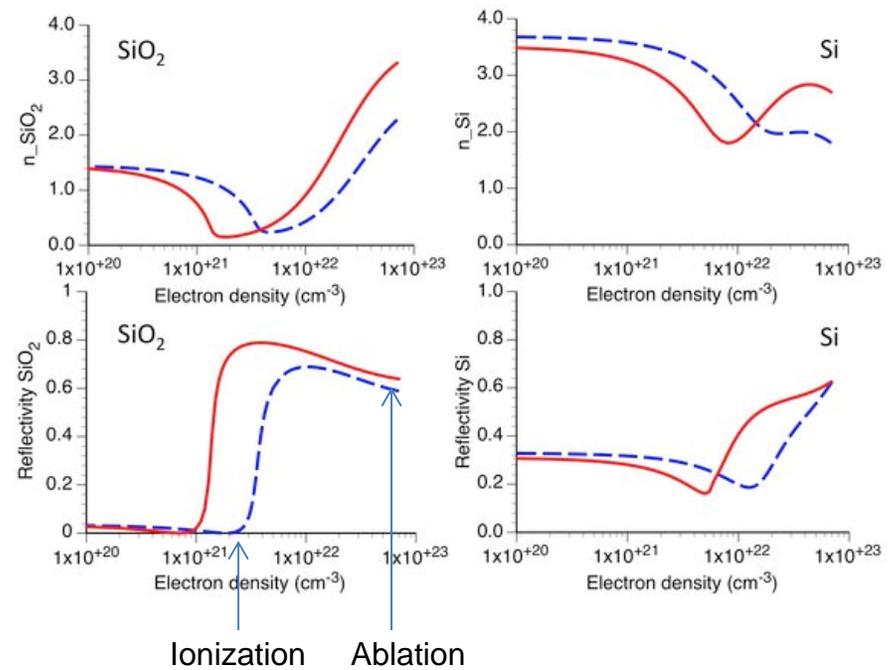
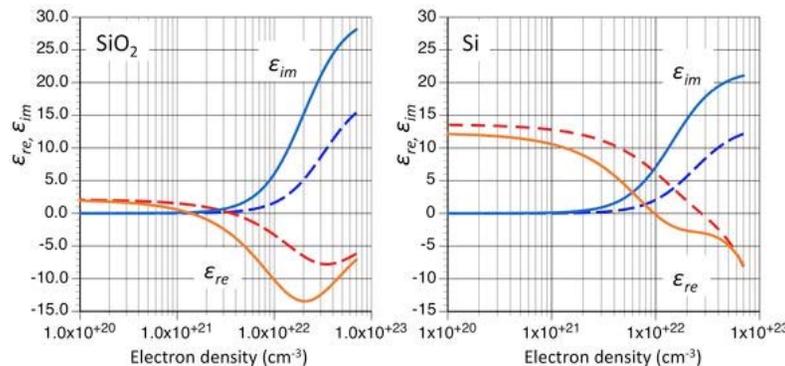
- Implement different (empirical and rigorous) ionization models in the code

Empirical ionization model based on rate equations for n_e and T_e & Drude model (Gamaly-Rode):

- Study the regime between ionization and ablation thresholds (ions are not moving)
- Scattering rate depends on electron temperature:
grows with T_e at low T_e , then $\sim T_e^{-3/2}$ near ablation threshold
- This dependence causes non-trivial dependence of Drude reflectivity on pulse fluence or on time along the pulse

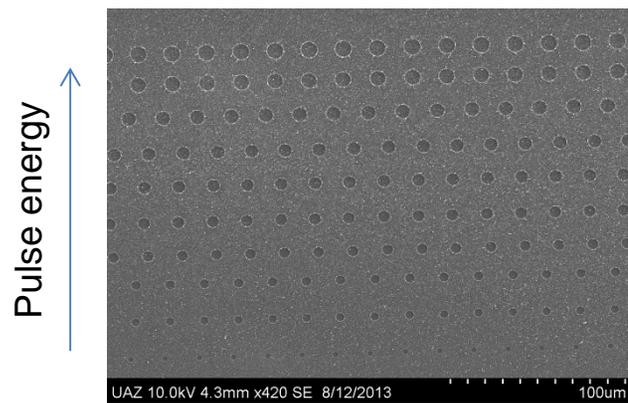
$$\epsilon_{Re} = \epsilon_0 - (\epsilon_0 - 1) \frac{n_e}{n_{at}} - \frac{n_e}{n_{cr} \left[1 + \left(\frac{v_{eff}(T_e)}{\omega} \right)^2 \right]}$$

$$\epsilon_{Im} = \frac{n_e}{n_{cr} \left[1 + \left(\frac{v_{eff}(T_e)}{\omega} \right)^2 \right]} \cdot \frac{v_{eff}(T_e)}{\omega}$$



Supporting experiments (UA)

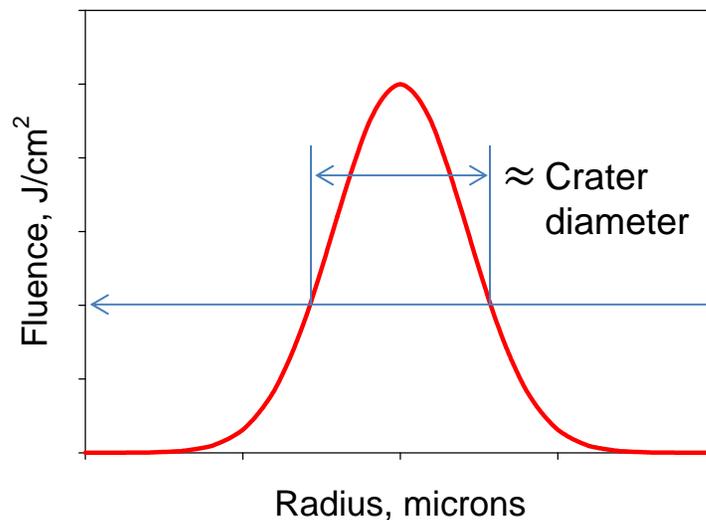
Studies of ionization dynamics – regime between ionization and ablation thresholds
 Measurements of transient dielectric function (SiO₂)



$$F(r) = \int_{-\infty}^{+\infty} e^{-2(r/R_{beam})^2} \cdot I(r=0, t) \cdot dt$$

$$F_{th} \approx e^{-2(r_{crat}/R_{beam})^2} \cdot \int_{-\infty}^{+\infty} I(r=0, t) dt$$

$$\frac{F(r=0)}{F_{th}} = e^{2(r_{crat}/R_{beam})^2}$$



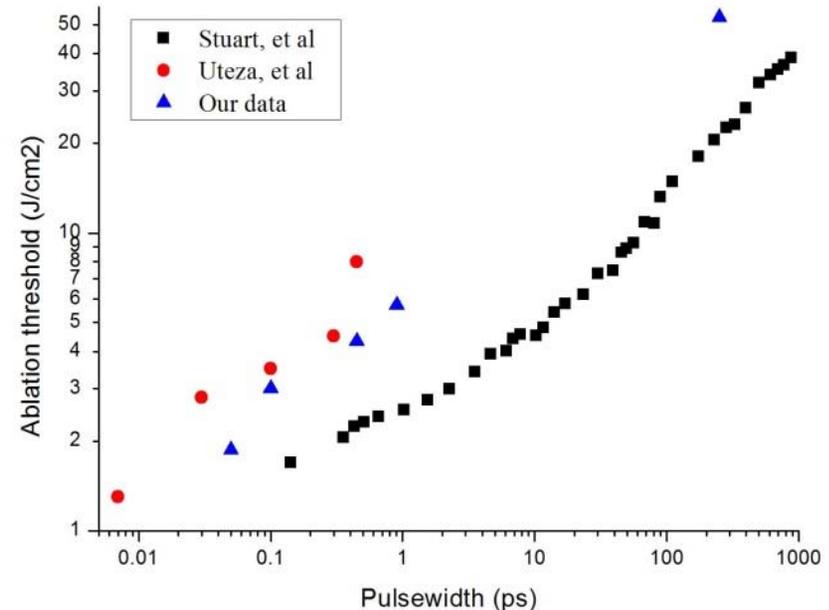
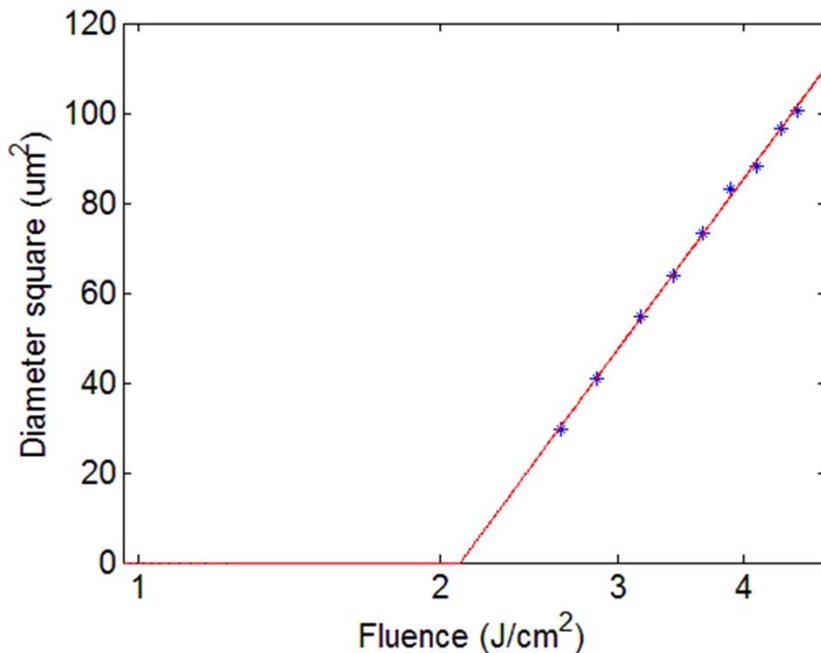
Plot r_{crat}^2 vs. $\log(F) \Rightarrow F_{th}, R_{beam}$

J. M. Liu, Opt. Lett. **7**, 196 (1982)

Ablation threshold fluence

Supporting experiments (UA)

Studies of ionization dynamics – regime between ionization and ablation thresholds
Measurements of transient dielectric function (SiO_2)



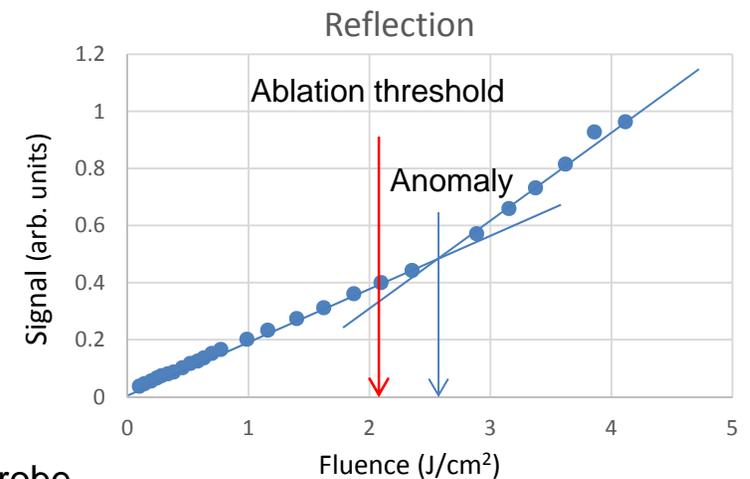
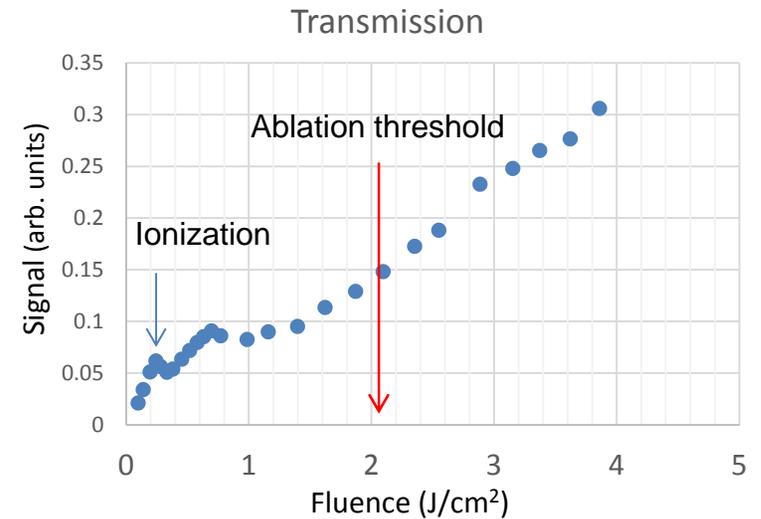
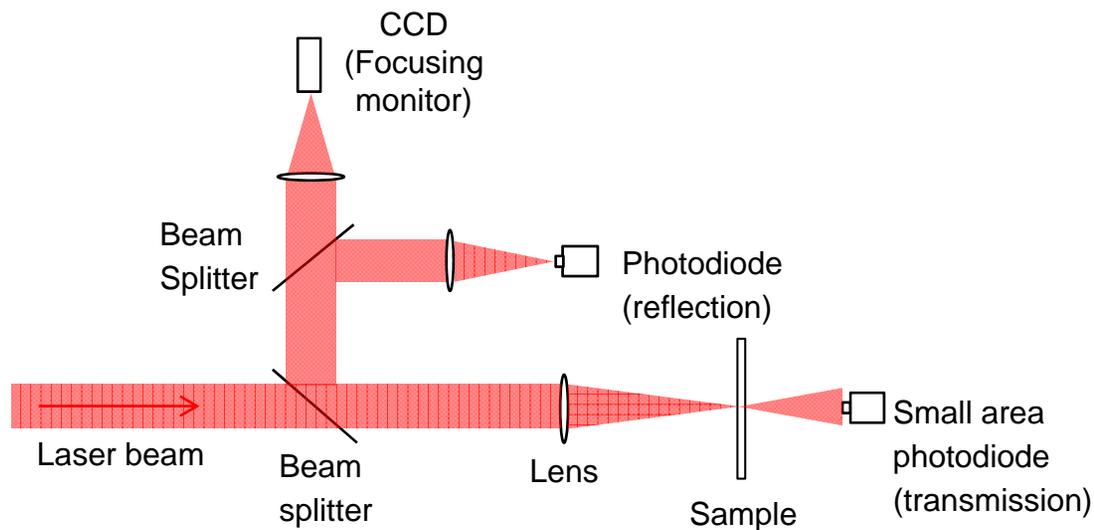
B. Stuart et al. (LLNL), JOSAB **13**, 459 (1996)

O. Uteza et al. (U. Marseille, INRS Quebec), Appl. Phys. A **105**, 131 (2011)

- Ablation threshold fluence $2.1 \text{ J}/\text{cm}^2$ for 70 fs pulse
- Beam radius $8.1 \mu\text{m}$, consistent with knife-edge measurement

Supporting experiments (UA)

Measurements of ionization threshold – detect anomalies in transmission vs. energy



- Measure transmission anomalies in the range 0.2 – 1.0 J/cm²
- Data is difficult to interpret
- Will conduct pump-probe measurements of reflectivity with 5 fs probe

Supporting experiments (UA)

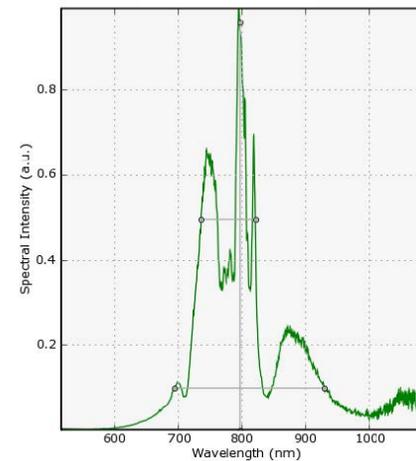
Hollow-fiber pulse compressor installed, being integrated into pump-probe setup.

Will allow transient reflectivity measurements with 5 fs resolution
and ablation measurements in the ultrahigh intensity regime

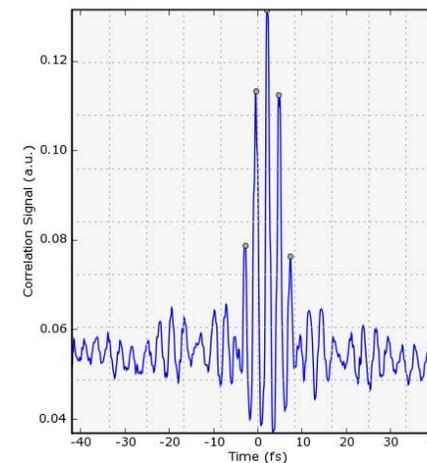


- Neon-filled 100 μm diam. capillary, 1.5 bar.
- Max. compressed output: 0.68 mJ
- Min. pulse duration: 3.7 fringes = 5.1 fs

Spectrum

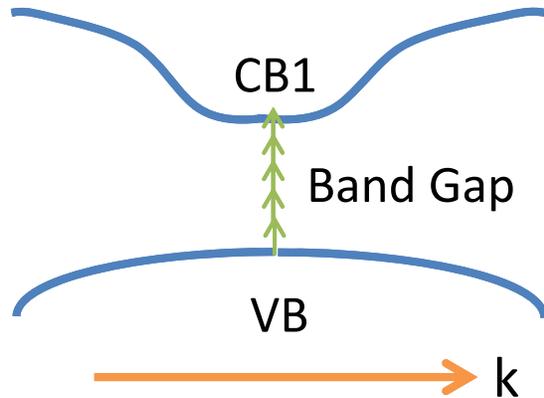


Autocorrelation





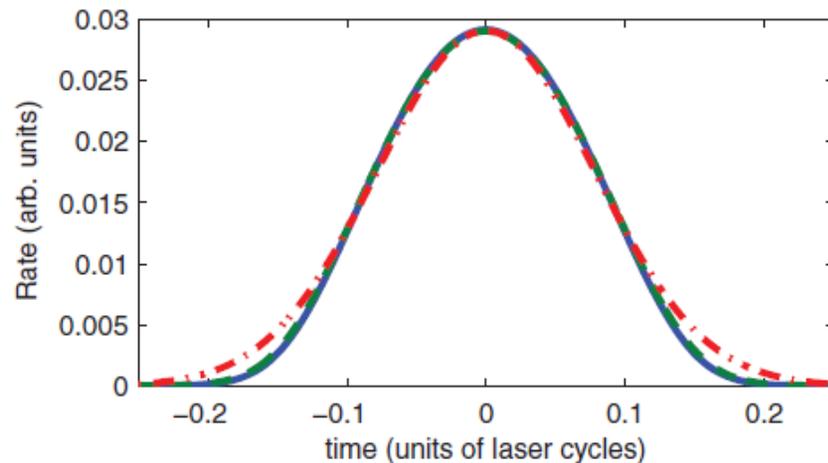
For ultrashort pulses (<10 fs) and ultrahigh intensities (>10¹⁴ W/cm²), sub-cycle effects in ionization become important (M. Ivanov – MBI)



$$\frac{dn_e}{dt} = \sigma \cdot I^k + \alpha \cdot I(t) \cdot n_e(t)$$

MPI Avalanche
↓ ↓

Need non-perturbative treatment



Sub-cycle ionization rate:

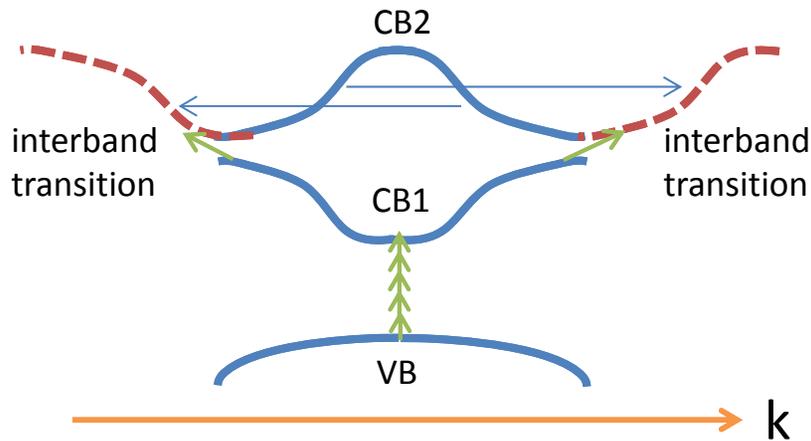
- Blue – numerical integration
- Green – approx. analytical formula
- Red – Gaussian fit

Work in progress:

Calibrate analytical formula against absolute cycle-averaged values measured for SiO₂, for incorporation into the Maxwell code



Related question: In dielectric crystals, what happens to the band structure in strong IR fields? What is the effective mass of conduction band electrons?

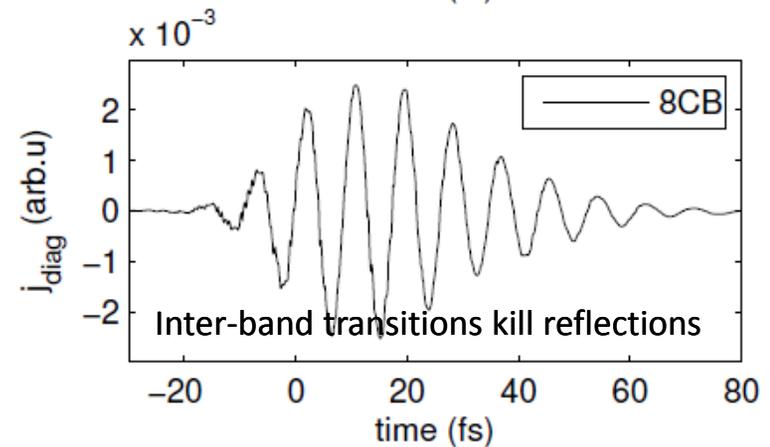
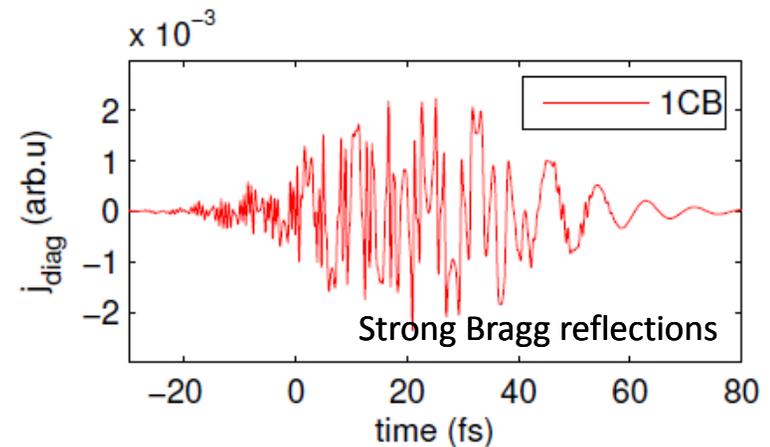


Pilot simulations:

- 1D periodic potential in an IR field
- Solve TDSE with 1 valence and different # of conduction bands

Results:

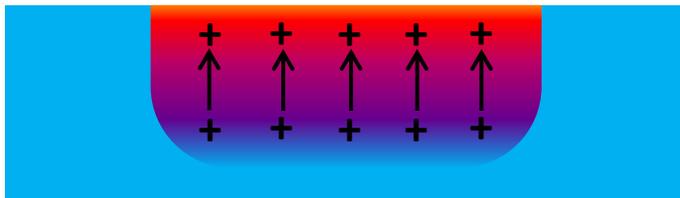
- Strong IR field eliminates band structure, creates a single effective parabolic band
- Conduction band electrons behave like free electrons with effective mass $m=m_0$
- Harmonic generation strongly suppressed



First-principle models of fs laser-matter interactions

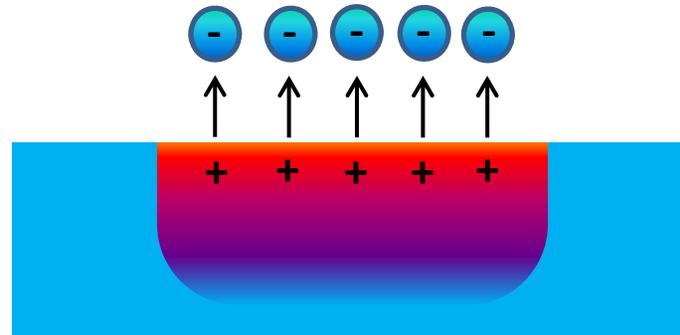
Model #2 – First-principle model of surface ablation

Quantify relative contributions of Coulomb explosion and electrostatic ablation mechanisms



Coulomb explosion: Electrons leave, excessive positive charge pushes ions out of the material.

Some delay between departures of electrons and ions



Electrostatic ablation: Electron sheet pulls ions out of the material.

Electrons and ions leave simultaneously

E. Gamaly, A. Rode, V. Tikhonchuk, B. Luther-Davis, "Electrostatic mechanism of ablation by femtosecond lasers", *Appl. Surface Science* **197-198**, 699 (2002).

W. Roeterdink, L. Juurlink, O. Vaughan, J. Dura Diez, M. Bonn, A. Kleyn, "Coulomb explosion in femtosecond laser ablation of Si(111)", *Appl. Phys. Lett.* **82**, 4190 (2003).

Model #2: Kohn & Sham model –

Quantum mechanics for electrons, classical mechanics for ions.

Computationally very challenging

– Can only treat 1D case with ~30 ions on a “conventional”
(but still large) computer

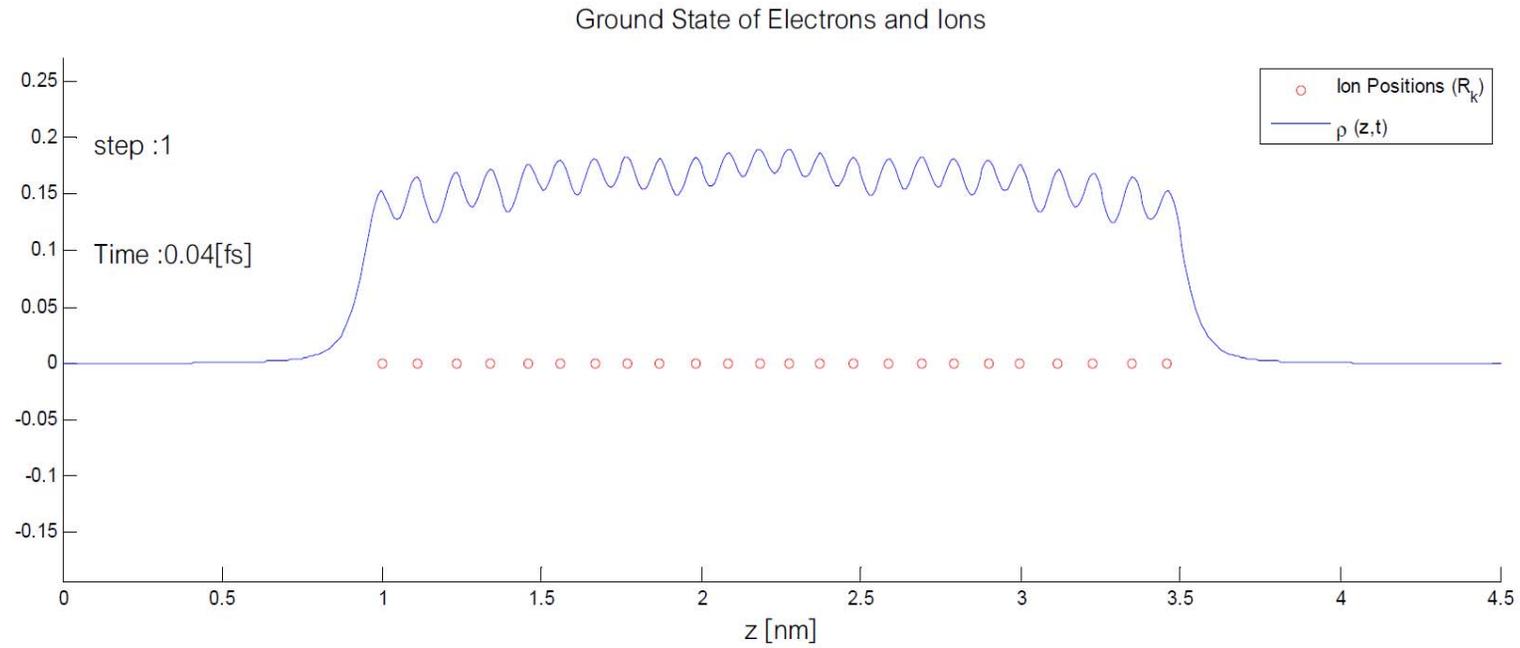
- Electrons interact not individually but through the overall electron density $n(r)$
- Driving of electrons by external field is described by vector potential $A(r)$
- Coulomb interaction is described by total potential $V(r,t,n)$, which is the sum of electron and ion potentials
- Motion of individual ions is treated classically

$$i\hbar \frac{\partial}{\partial t} \Psi_j = \frac{1}{2m_e} \left(\frac{\hbar}{i} \vec{\nabla} + e\vec{A} \right)^2 \Psi_j + V(\vec{r}, t, n) \Psi_j$$

$$V(\vec{r}, t, \rho) = e^2 \int \frac{n(\vec{r}', t)}{|\vec{r} - \vec{r}'|} d^3\vec{r}' + V_{xc}(n) - e^2 \sum_{n=1}^{N_Z} \frac{Z_n}{|\vec{r} - \vec{R}_n|}$$

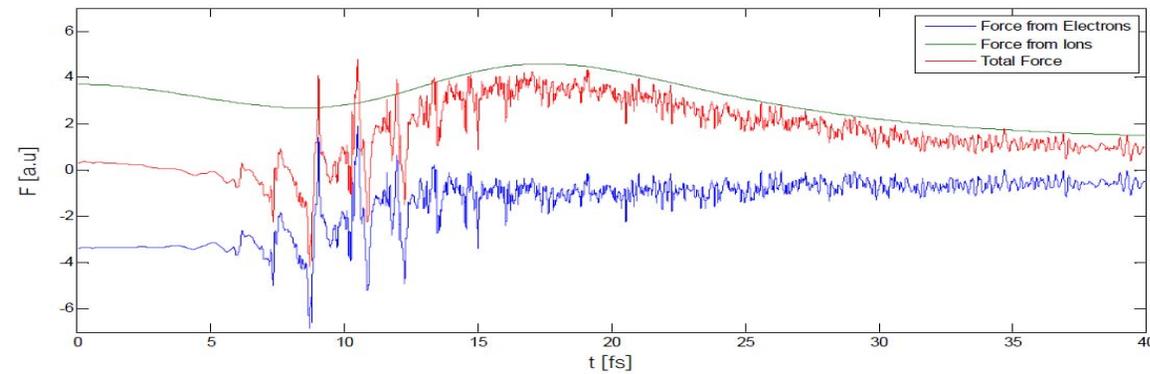
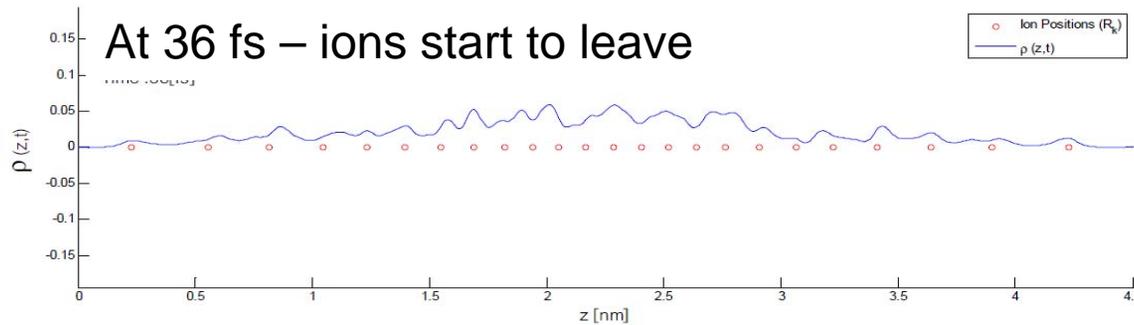
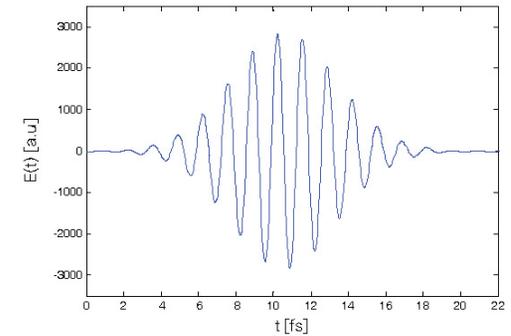
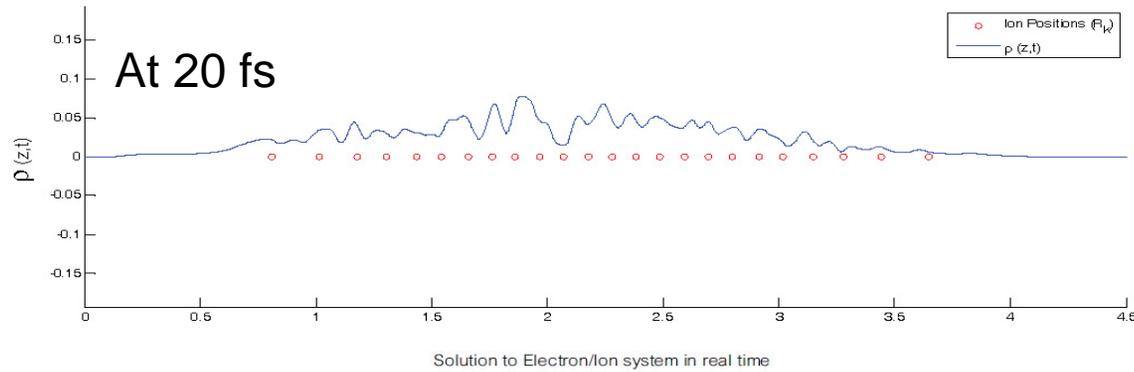
$$m_n \frac{\partial^2 \vec{R}_n}{\partial t^2} = Z_n Z_m e^2 \sum_{m \neq n}^{N_Z} \frac{\vec{R}_n - \vec{R}_m}{|\vec{R}_n - \vec{R}_m|^3} + e^2 Z_n \vec{\nabla}_{\vec{R}_n} \int \frac{n(\vec{r}, t)}{|\vec{r} - \vec{R}_n|} d^3\vec{r}$$

Compute 1D ground state (prior to arrival of laser pulse)



- Computed initial ground state (shown)
- 24 ions (red) are computed, typical distances of ~ 1.1 Angstroms
- Total electron probability density (blue) computed as sum of 48 electron probability densities

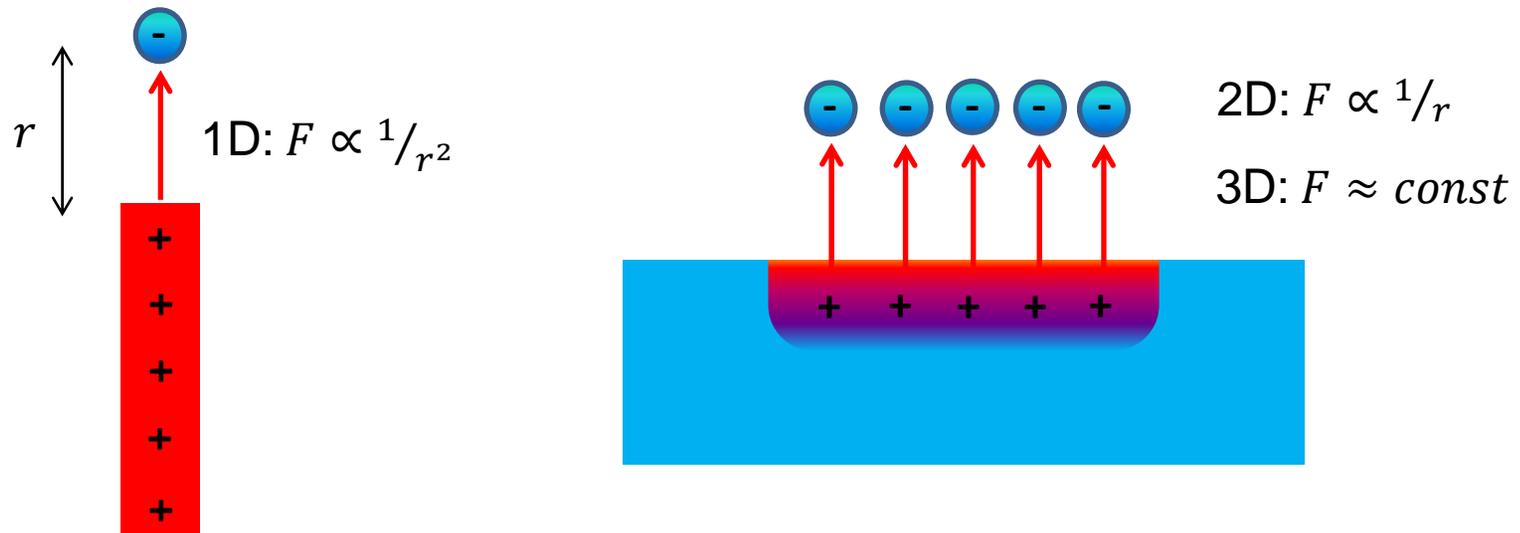
1D string of ions + electrons excited by 20fs laser pulse



Forces acting on the edge ion – pushing by other ions dominates over pulling by electrons

Coulomb explosion wins in 1D

1D, 2D and 3D cases are qualitatively different



DFT treatment of realistic sample sizes, even in 2D, is impractical:
(800 nm)² 2D sample contains $\sim 10^7$ ions $\rightarrow 5^{18}$ bytes simulation - huge

On-going work:

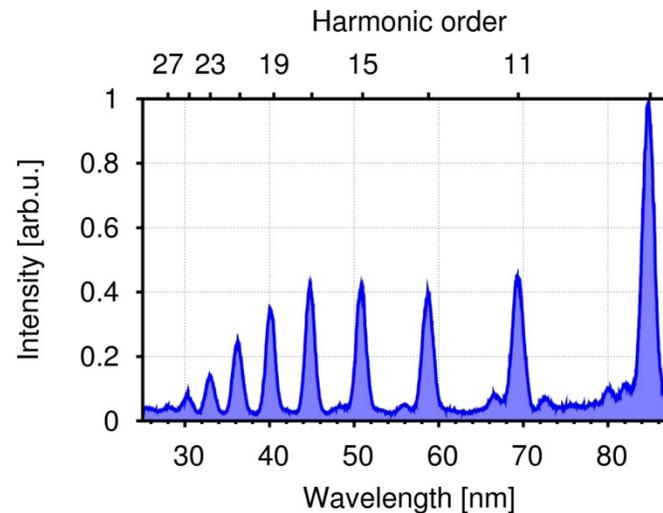
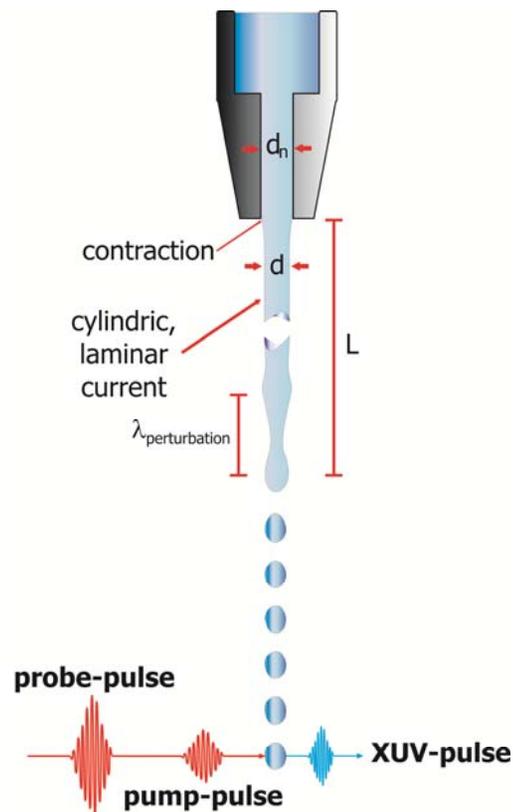
- Implement a semi-classical model instead
 - Electrons and ions are treated as classical particles, with the addition of a velocity-dependent potential preventing electrons falling on ions

(Erik Lotstedt, T. Kato, K. Yamanouchi, "Classical dynamics of laser-driven D3+" (PRL **106**, 203001 (2011))

Supporting experiments

(Hannover – Uwe Morgner, Milutin Kovacev, Heiko Kurz)

So far studied high harmonic generation in water microdroplets driven by pairs of fs pulses separated by several nanoseconds



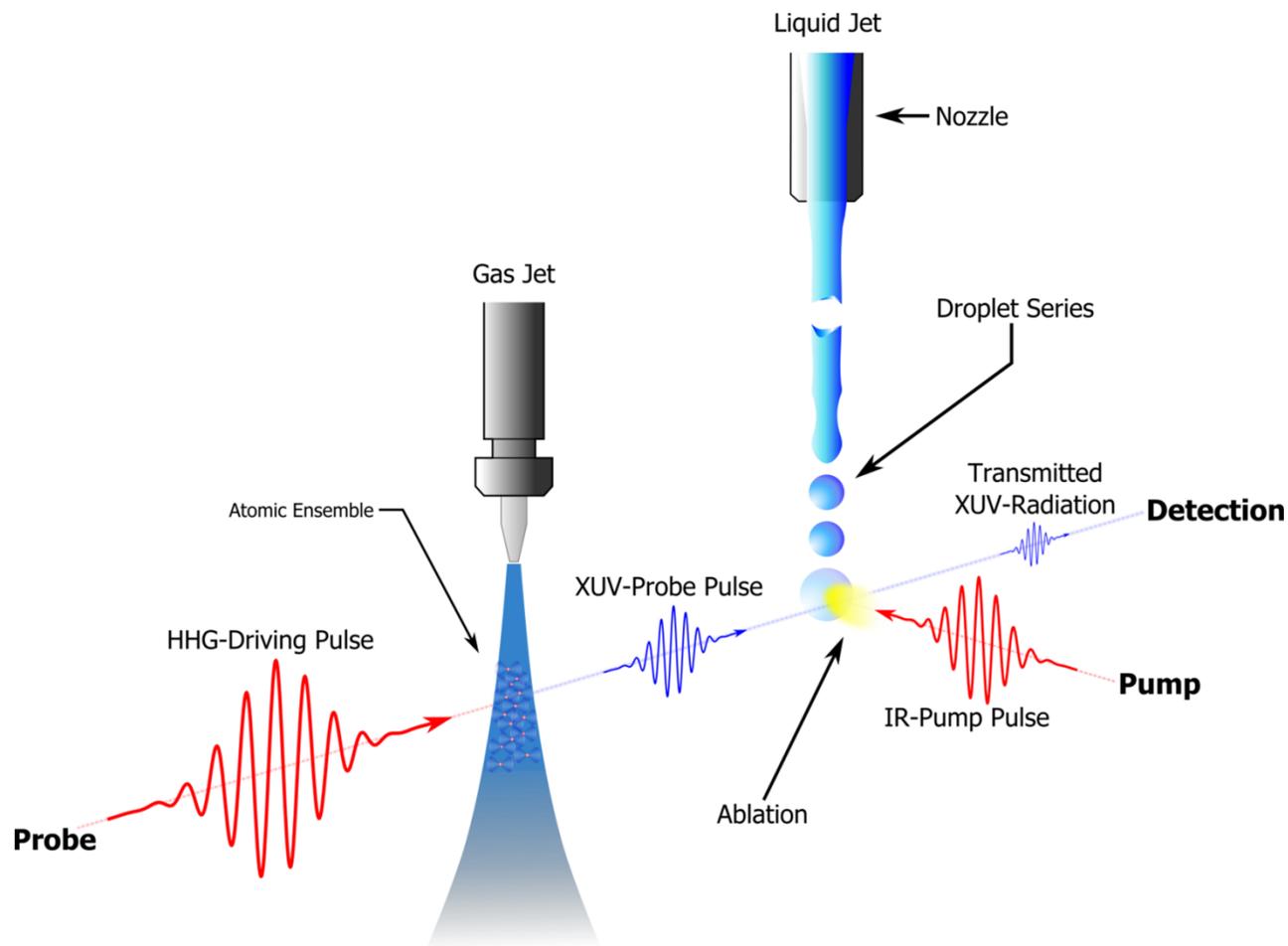
- Pump intensity: $3.7 \times 10^{14} \text{ W/cm}^2 \rightarrow \sim 40 \text{ J/cm}^2$
- Pump-probe delay: 1 ns
- Harmonics of up to the 27th order generated

H. Kurz, D. Steingrube, D. Ristau, M. Lein, U. Morgner, M. Kovacev,
 “High-order-harmonic generation from dense water microdroplets”, PRA **87**, 063811 (2013)

Supporting experiments

(Hannover – Uwe Morgner, Milutin Kovacev, Heiko Kurz)

Imaging of laser ablation of microdroplets in orthogonal pump-probe setup incorporating optical and XUV probe beams



Exotic situations of fs laser-matter interactions

Update on confined microexplosion experiments at ANU:

Creation of new phases of Si through microexplosion on Si-SiO₂ interface

(A. Rode, E. Gamaly, with Chris Pickard from Univ. College London)

Method:

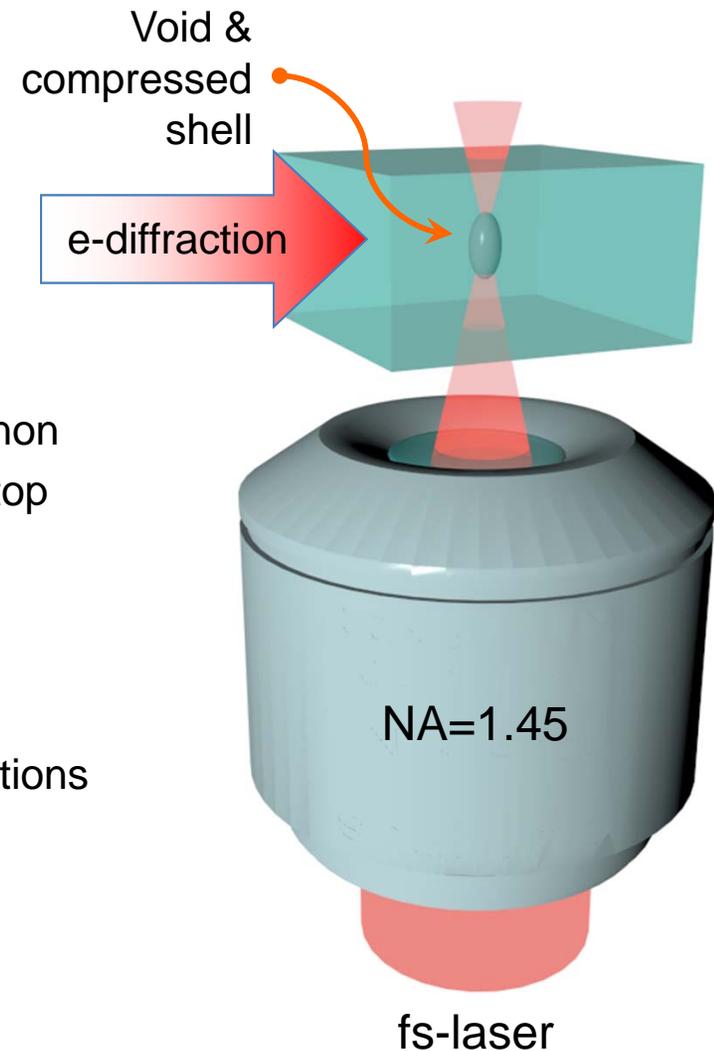
Confined micro-explosion by ultrafast-laser
focused in the bulk of transparent material
– conservation of mass

Motivation:

Formation of material states at extreme pressure and non
equilibrium temperature conditions in laboratory table-top
experiments

Outcome:

- New materials:
high-pressure \leftrightarrow ultra-hard; insulator-metal transitions
- New material phases (metastable?);
- New chemical/physical
properties of “shocked” materials



History of microexplosion studies



I – Indication on the creation of high pressure >TPa (10 Mbar) with fs-laser:

E. Glezer, E. Mazur, “Ultrafast-laser driven microexplosion in transparent materials”, Appl.Phys. Lett. **71**, 882–884 (1997)

II – Experimental evidence of the >3 TPa pressures in sapphire:

S. Juodkazis, et al., “Laser-induced microexplosion confined in the bulk of a sapphire crystal: Evidence of multimegabar pressures”, PRL **96**, 166101 (2006)

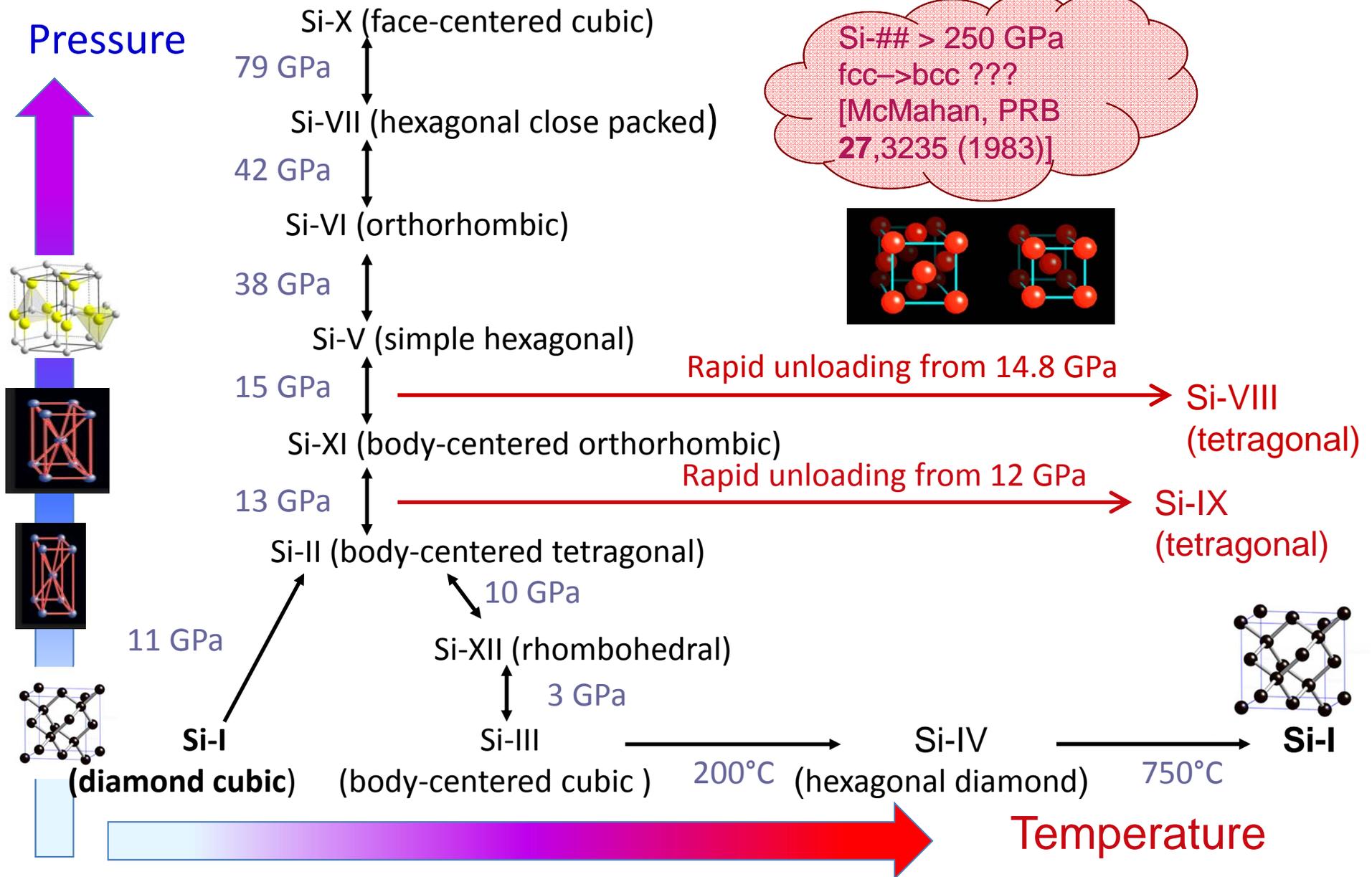
III – Discovery of the creation of super-dense material phases inside microexplosion voids:

A. Vailionis, E. Gamaly, V. Mizeikis, W. Yang, A. Rode, S. Juodkazis, “Evidence of superdense aluminium synthesized by ultrafast microexplosion”, Nature Communications **2**, 445 (2011)

IV – Laser-driven microexplosion on a material interface, densification of opaque materials

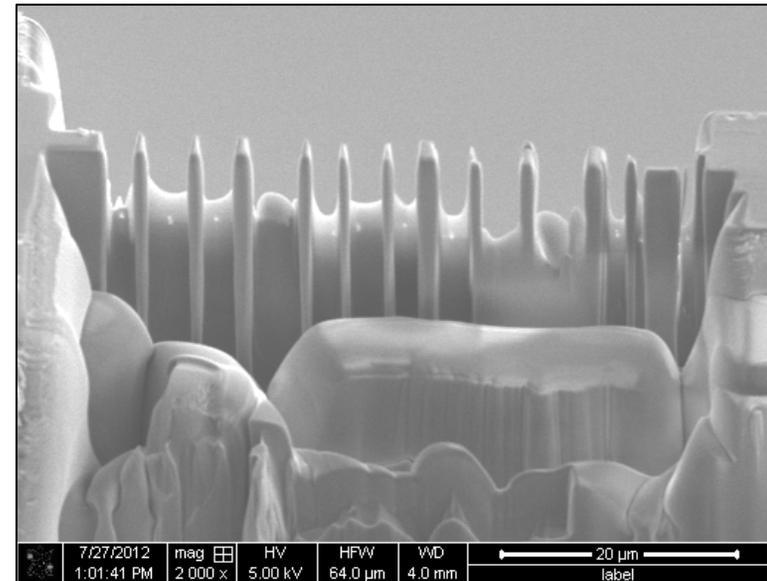
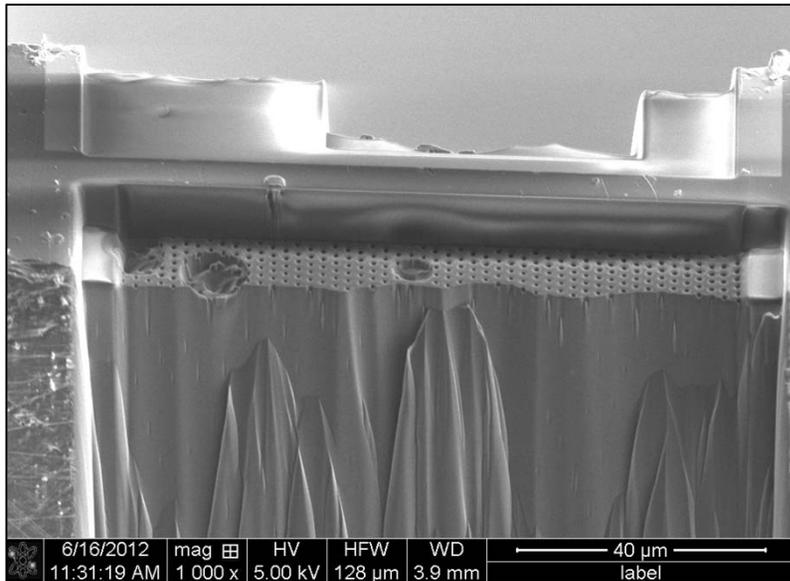
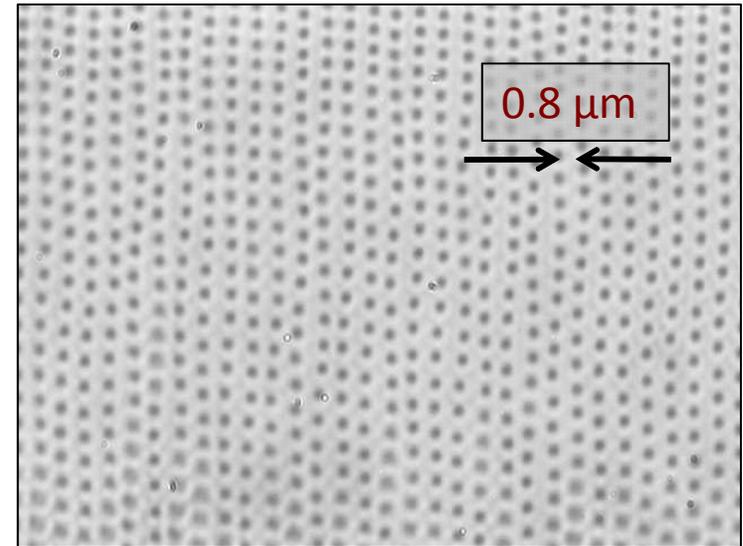
L. Rapp, B. Haberl, J. Bradby, E. Gamaly, J. Williams, A. Rode, “Confined microexplosion induced by ultrashort laser pulse at SiO₂/Si interface”, Appl. Phys. A **114**, 33 (2014)

Phase transitions of dc-Si to metallic Si

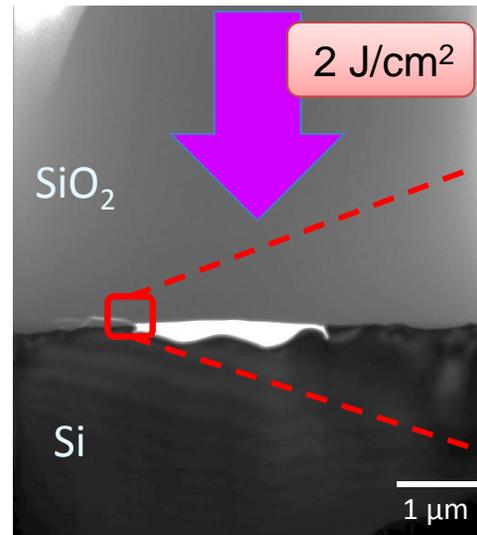
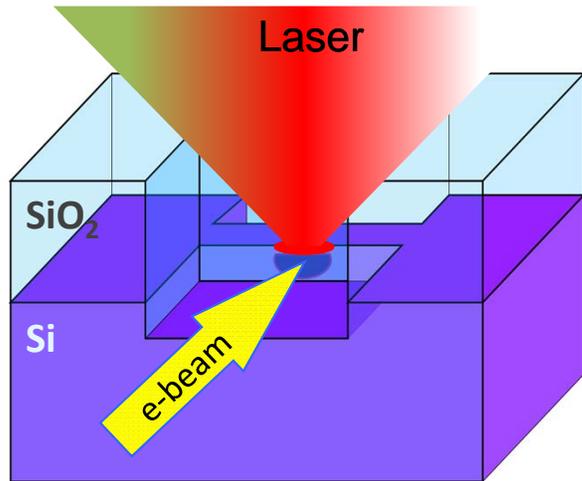


Preparation of samples for TEM and e-diffraction

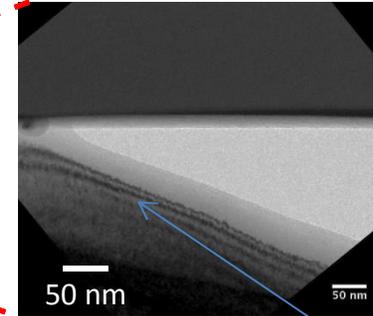
- Preparation of arrays of micro-explosions ~10 μm under the surface, ~1 μm apart;
- Polishing and cutting to 100- μm thick sample
- Removal of 10- μm thin surface layer with a focused ion beam (FIB)
- Thinning lamella to <100 nm for TEM



TEM imaging of voids on material interfaces

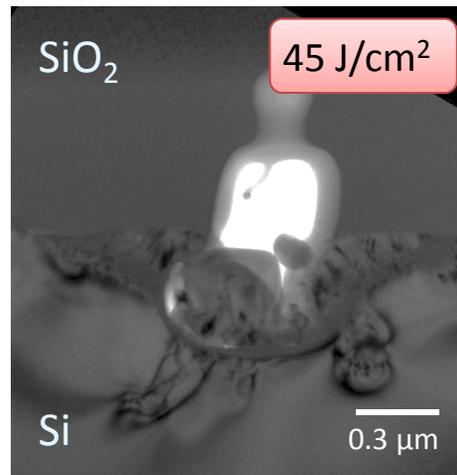
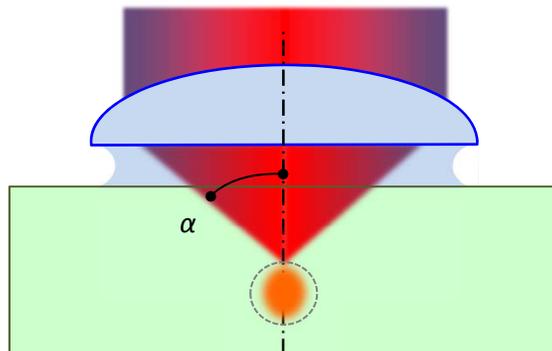


Below threshold
 $>2 \text{ J/cm}^2$ in SiO₂
 (SiO₂ remains intact)



Amorphous Si

High N.A. with x150

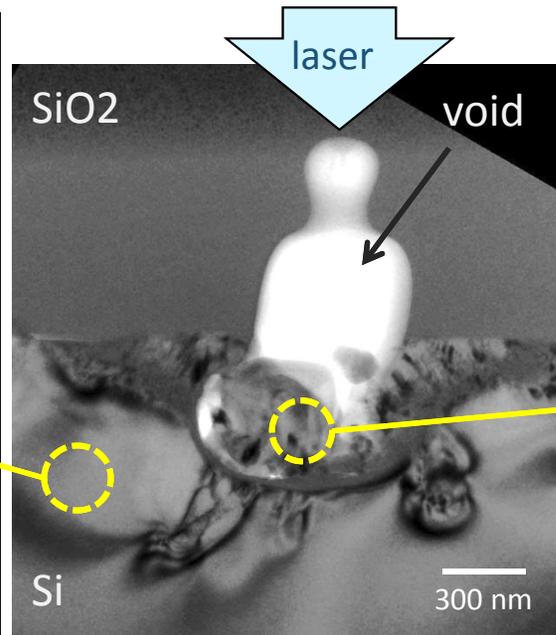
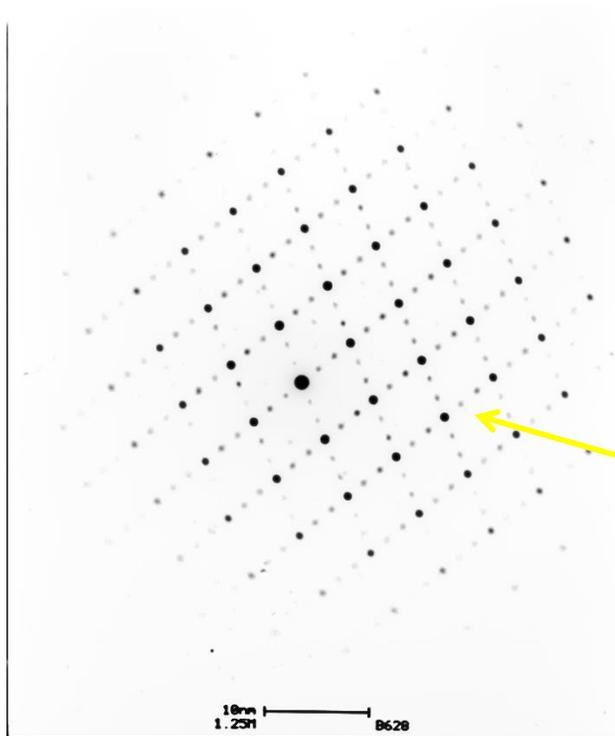


Above threshold in SiO₂
 (Absorption in SiO₂)

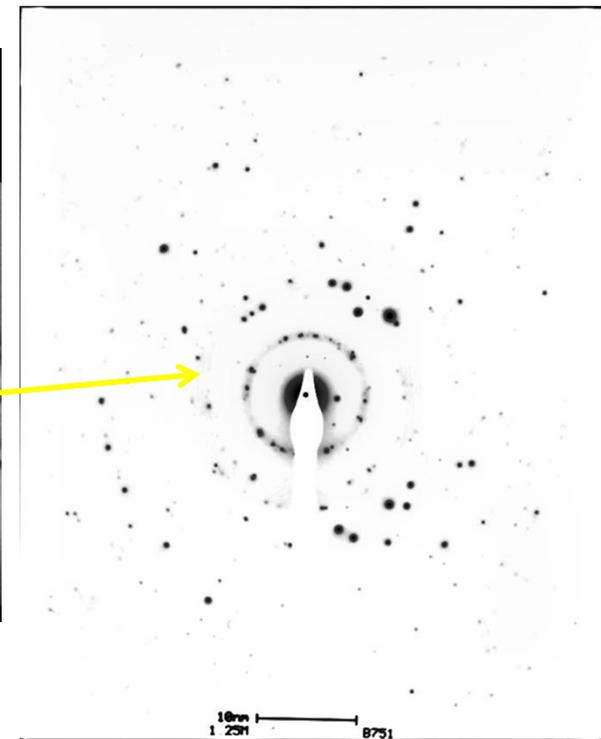


Electron diffraction reveals new material phases

Conventional
diamond-cubic Si

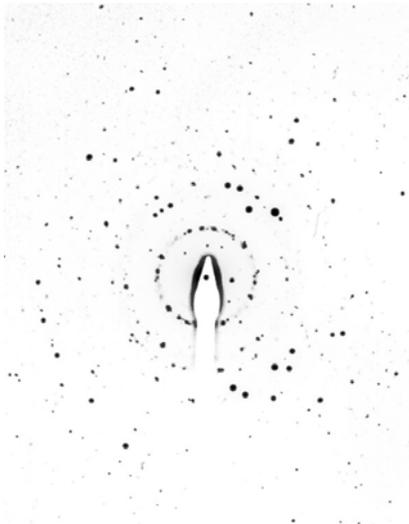
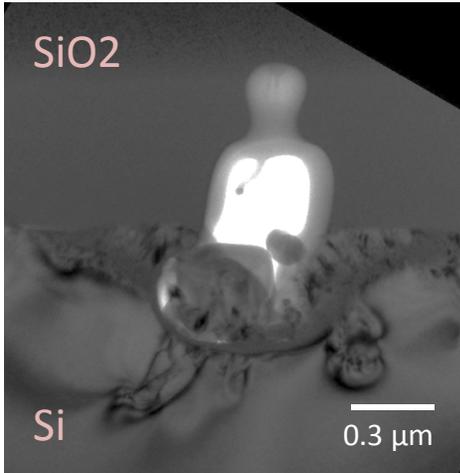


Si
quenched from WDM state

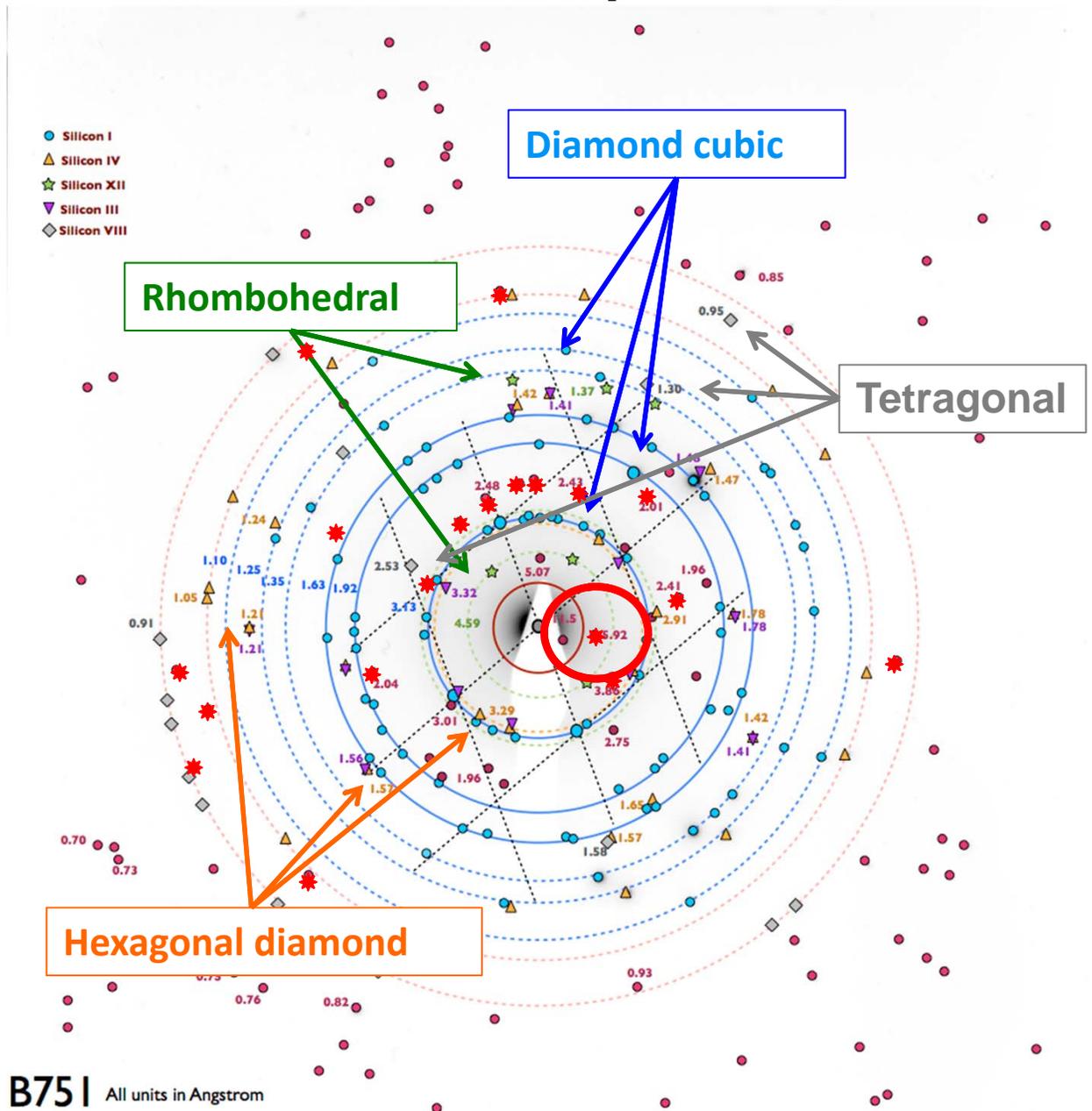


Electron diffraction reveals new material phases

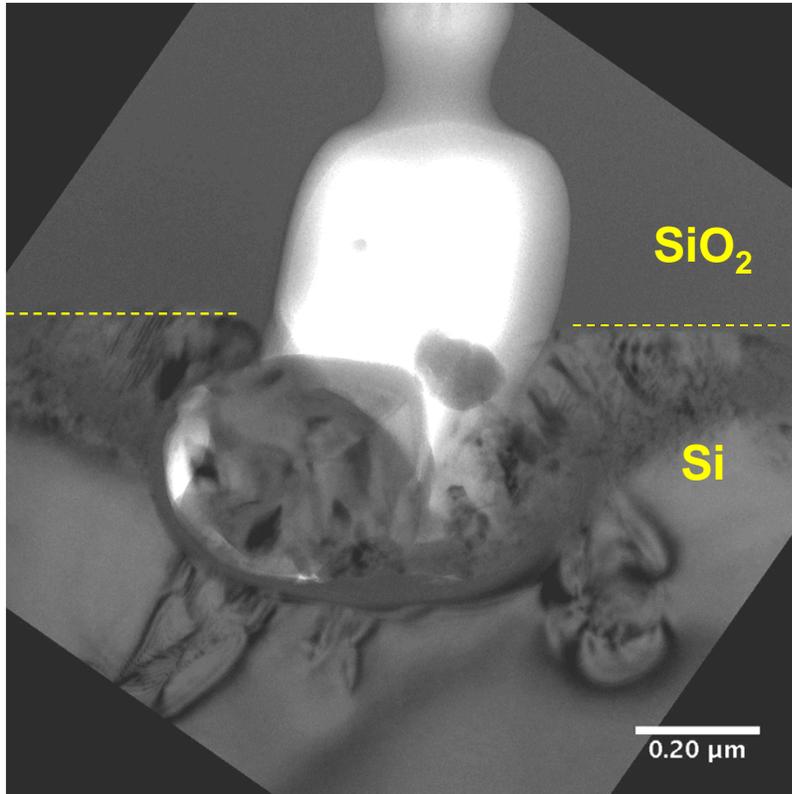
45 J/cm²



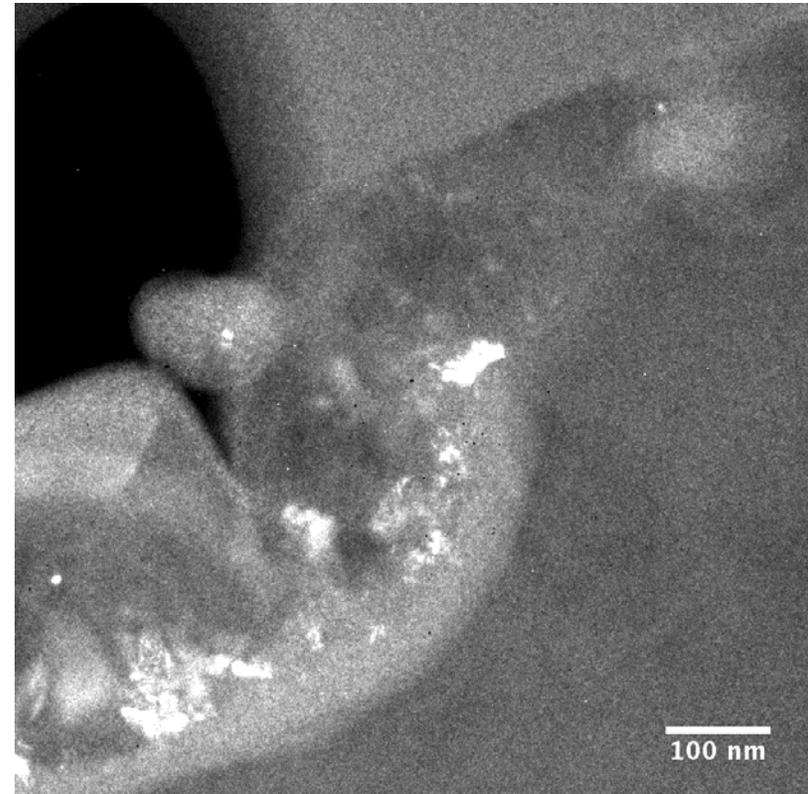
Electron diffraction at 300 kV
data #B751



TEM within a particular diffraction order shows spatial locations of new material phases



TEM image of void at Si/SiO₂ interface



Bright-field image at 5.92 Å bright spot

Results so far:



- First observation of two new tetragonal phases of silicon: 16-atom Si-BT8 (probably metallic) and 12-atom Si-ST12 (probably narrow-band SC)
- Demonstration of low kinetic barrier in non-equilibrium conditions for formation of new metastable phases – synthesis of phases directly from WDM
- BT8-Si density is 2.73 g/cm^3 at 5 GPa, which is about 17% more dense than dc-Si. Computed density of states indicate the phase is a narrow band gap semiconductor
- ST12-Si density is 2.47 g/cm^3 , 6% more dense than dc-Si at ambient pressure. Density of states indicate the phase is an indirect bandgap semiconductor with a bandgap energy between 1.1 eV and 1.67 eV
- These metastable phases are of significant interest, as they may have new electronic and photovoltaic properties

Summary

- 1. First-principle modeling of fs laser-matter interactions**
 - Inside dielectrics: Non-paraxial Maxwell propagator coupled with ionization
 - On surfaces: DFT model of ablation – computationally very challenging, implement a simpler semi-classical model
 - Sub-cycle effects in ionization with ultrashort pulses (<10 fs)
 - Modifications of band structure of crystals in ultraintense laser fields
- 2. Supporting experiments:**
 - Investigations of regimes between ionization and ablation thresholds
 - Measurements of transient reflectivity of ionized dielectrics using 5 fs probe pulse
 - Imaging of ions created through fs ablation of microdroplets with XUV probe
- 3. Experimental studies of exotic ablation situations:**
 - Confined microexplosion inside transparent solids and on interfaces
 - Creation and identification of new super-dense material phases
 - Ablation with ultrashort laser pulses ~5 fs – sub-cycle ionization effects in ablation

