



# New paradigm for multi-TW, multiple Joule $10\text{ }\mu\text{m}$ USP self-trapping over kilometer ranges

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Support: AFOSR FA9550-16-1-0088, FA9550-15-1-0272



# Talk Outline

- Introduction
- Filament Modeling Hierarchy
- MWIR Light Bullet – shock regularization
- LWIR self-trapping at  $10\mu\text{m}$ 
  - many-body modification of NL response
- Summary & Conclusion



# Chaotic Filamentation in 800nm TW Pulses

Relative disposition of filaments dictated by initial aberrations  
across the beam

D.E. Roskey, M. Kolesik, J.V. Moloney and E.M. Wright  
Appl. Phys. B **86** 249 (2007)

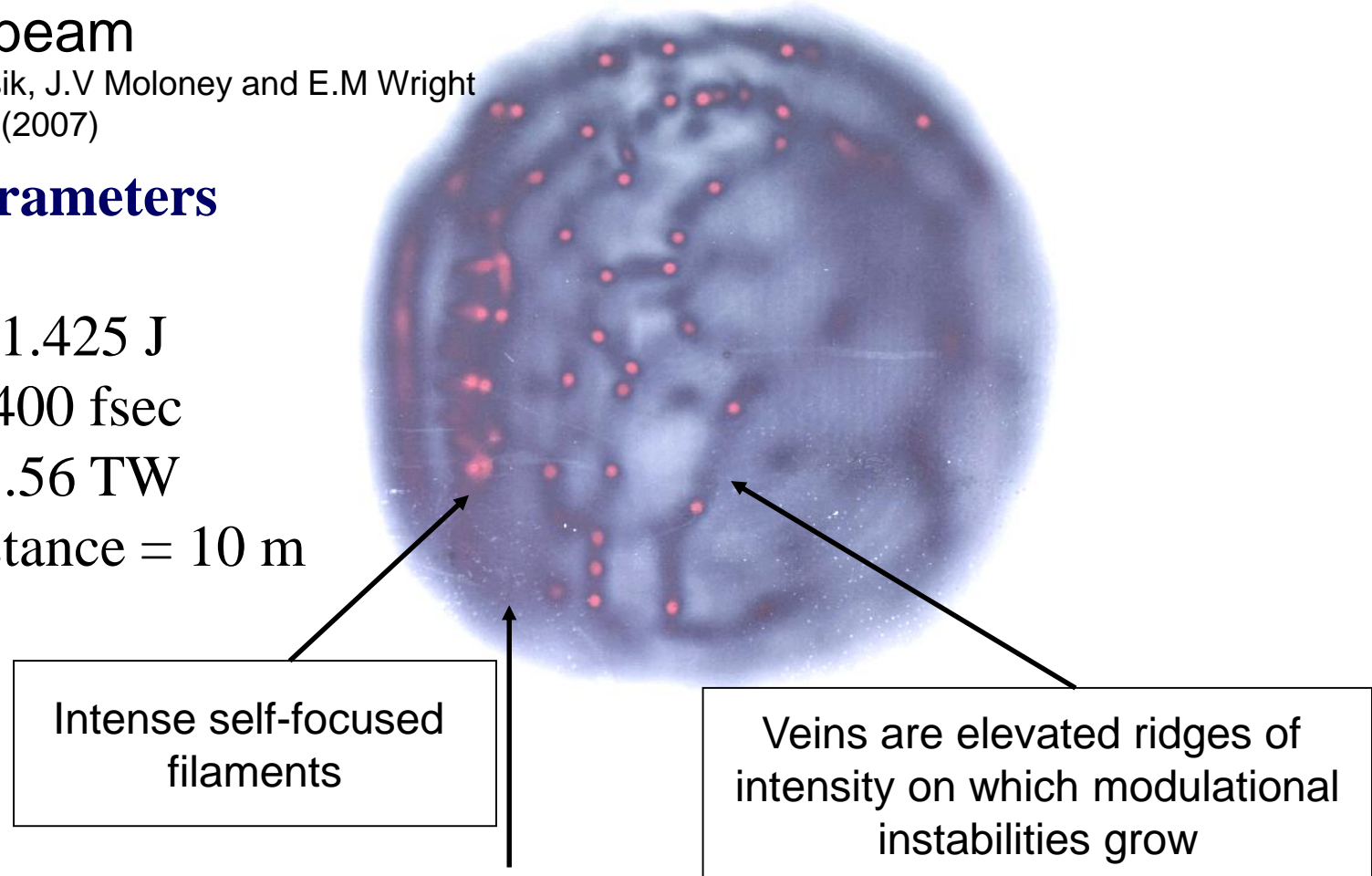
## NRL Laser Parameters

Pulse energy = 1.425 J

Pulse length = 400 fsec

Peak power = 3.56 TW

Propagation distance = 10 m



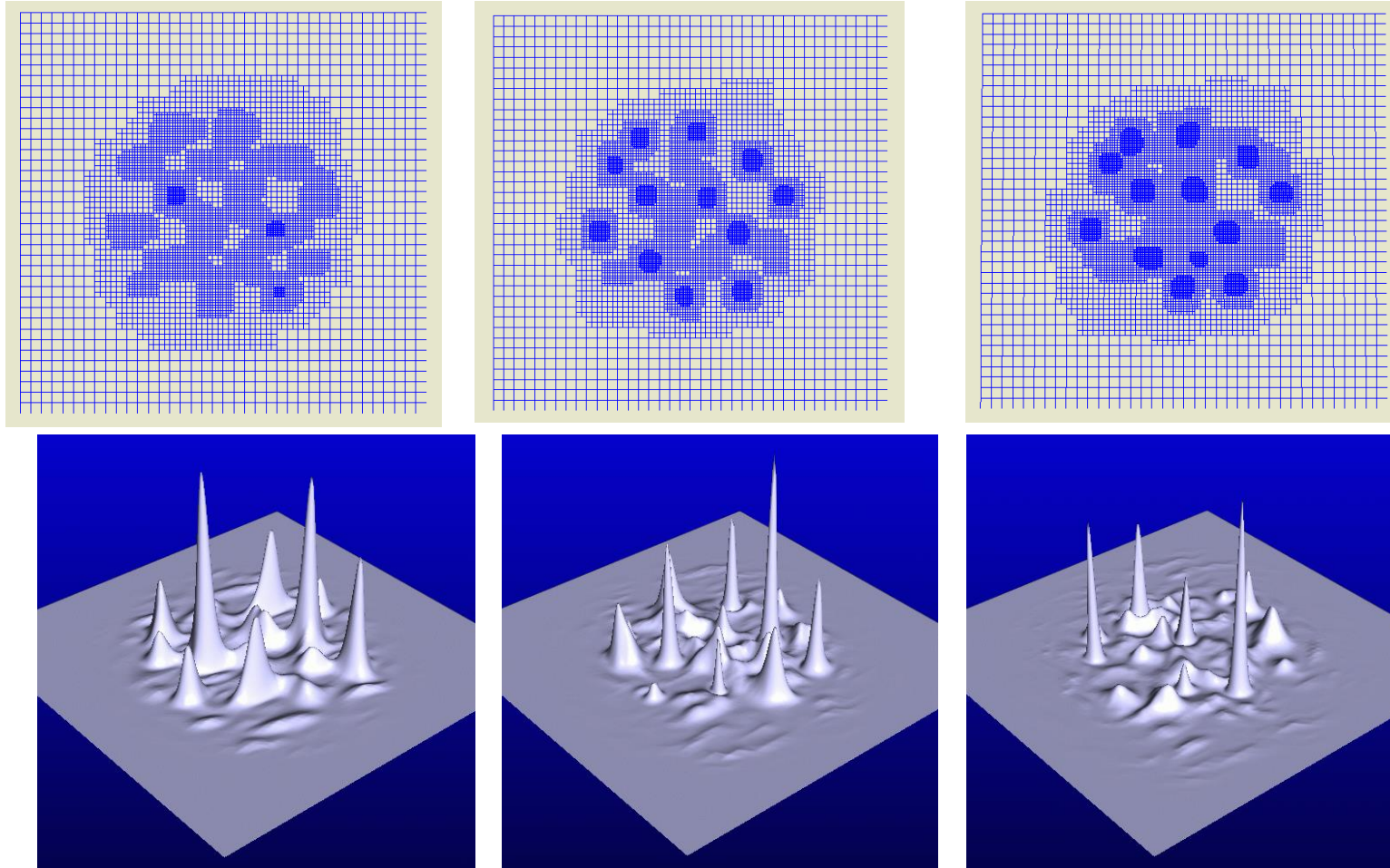
Broad background acts as an energy reservoir (photon bath) to sustain recurring filaments

M. Mlejnek, M. Kolesik, J.V. Moloney, E.M. Wright, *PRL*, **83**(15) pp. 2938-2941 (1999).



# Adaptive Mesh GNLSE Parallel Solver

*Dynamic regridding in space and time – Multiple light strings*



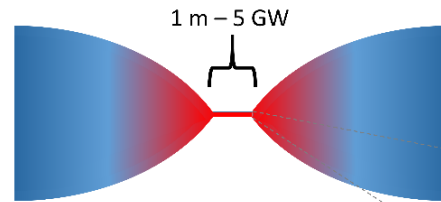


# IR vs Mid-IR Atmospheric Filament Scaling

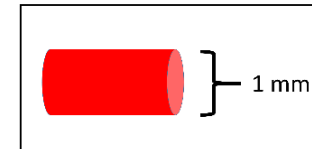
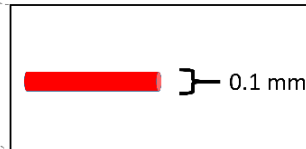
Linear propagation



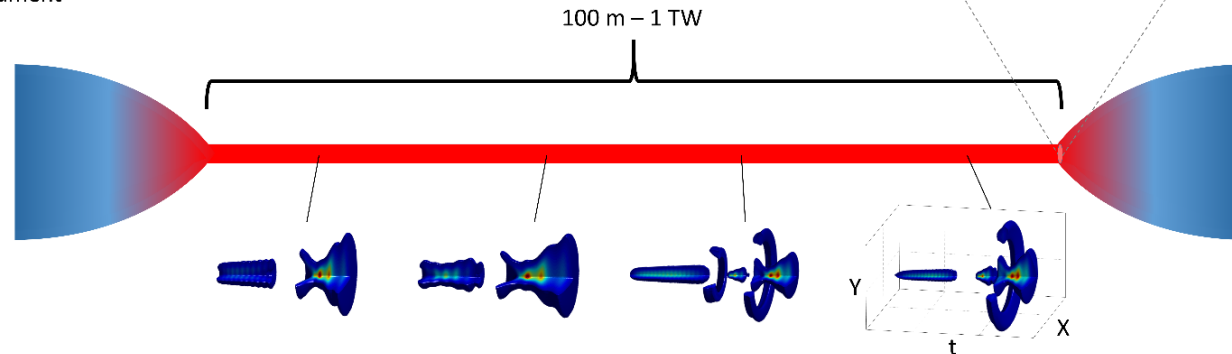
800nm filament



Filament diameter



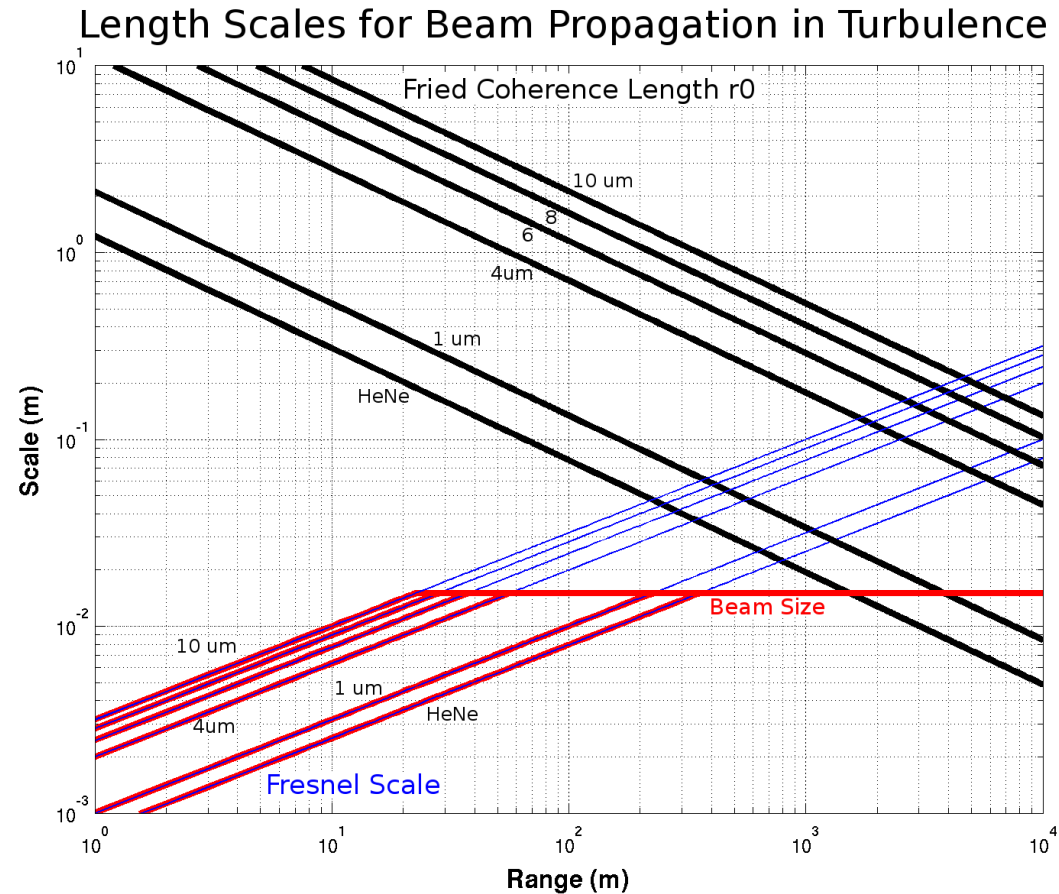
4 $\mu$ m filament





# Worst Case Scenario – Ground Level Turbulence

- Simple estimate for linear propagation of a 1.5 cm beam



- Confined filament or self-trapped beam can beat diffraction limitation



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# Scalar UPPE Model (Unidirectional)

## Unidirectional Pulse Propagating Equation (z-UPPE)

$$\partial_z \mathcal{E}(z, \omega, k) = \boxed{ik_z(\omega, k)} \mathcal{E}(z, \omega, k) + \frac{i\omega^2}{2\varepsilon_0 c^2 k_z(\omega, k)} \boxed{\mathcal{P}(z, \omega, k)} - \frac{\omega}{2\varepsilon_0 c^2 k_z(\omega, k)} \boxed{\mathcal{J}(z, \omega, k)}$$

$$k_z(\omega, k) \equiv \sqrt{\omega^2 \varepsilon(\omega) / c^2 - k^2}$$

Plasma-related current

Accurate chromatic dispersion

Nonlinear polarization evaluated from real field

$$\boxed{P(z, r, t)} = \varepsilon_0 \Delta \chi_{\text{sf}}(z, r, t) E(z, r, t) = 2\varepsilon_0 \bar{n}_2 \left[ \frac{1}{2} \boxed{E^2(z, r, t)} + \frac{1}{2} \int_0^\infty R(\tau) E^2(z, r, t - \tau) d\tau \right] E(z, r, t)$$

Second Harmonic component = source of TH

**Carrier based approach, no envelope approximations used**

VOLUME 89, NUMBER 28

PHYSICAL REVIEW LETTERS

31 DECEMBER 2002

**Unidirectional Optical Pulse Propagation Equation**

M. Kolesik, J.V. Moloney, and M. Mlejnek\*

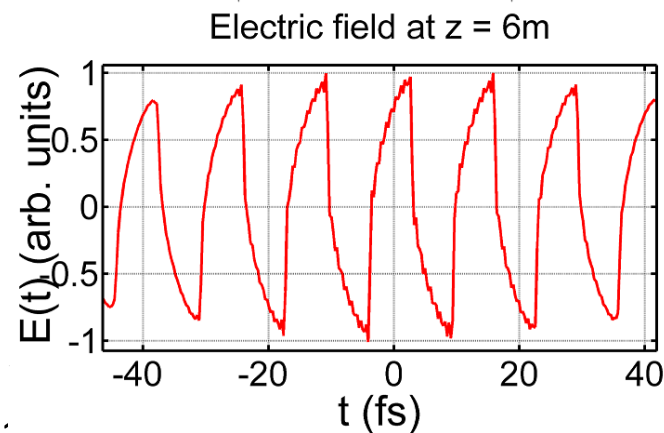




# Modified Kadomtsev-Petviashvili (MKP1)

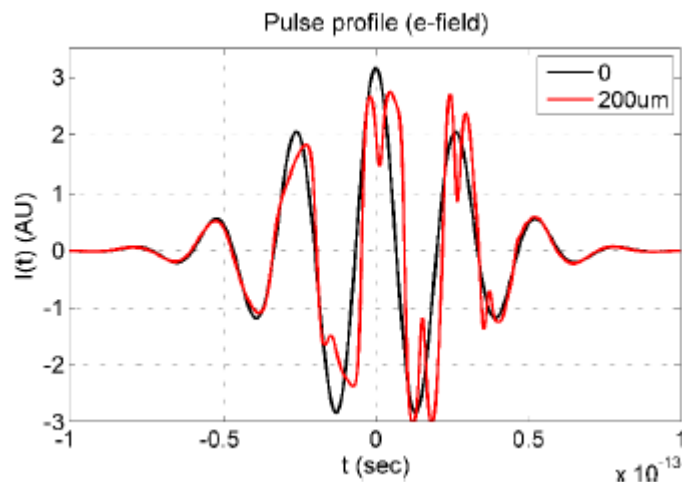
- Canonical Full Field Propagator for long wavelength USPs

$$\partial_{\tau} \left[ \partial_z E(r, z, \tau) + \frac{4n_2}{c} E^2 \partial_{\tau} E - a \partial_{\tau}^3 E \right] + bE = \frac{c}{2n(\omega_R)} \Delta_{\perp} E$$

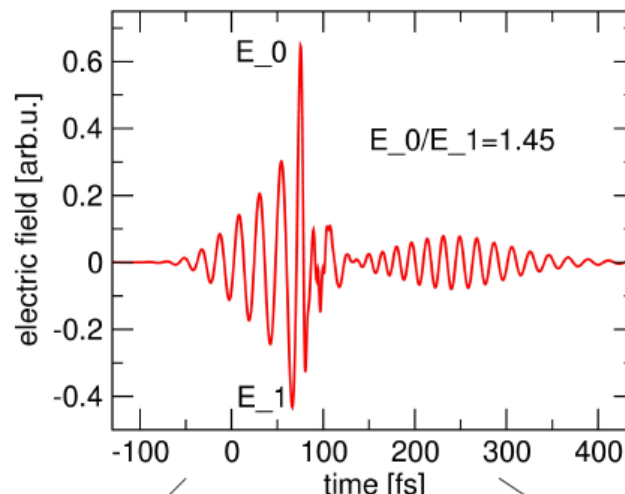


- Asymptotic limit of UPPE for strongly nonlinear weakly dispersive waves
  - K. Glasner et al, Int. J. Optics. <http://dx.doi.org/10.1155/2012/868274> (2012),
- Exhibits carrier shock + blowup - Originally derived for ion-acoustic waves
- P. Whalen et al., Phys.Rev.A, **89**, 023850 (2014); P. Panagiotopoulos et al. JOSAB, **32**, 1718 (2015)
- Balakin, A.A., A.G. Litvak, V.A. Mironov, S.A. Skobelev. JETP, 2007, 104 363-378

Carrier shock in Diamond at  $8\mu\text{m}$

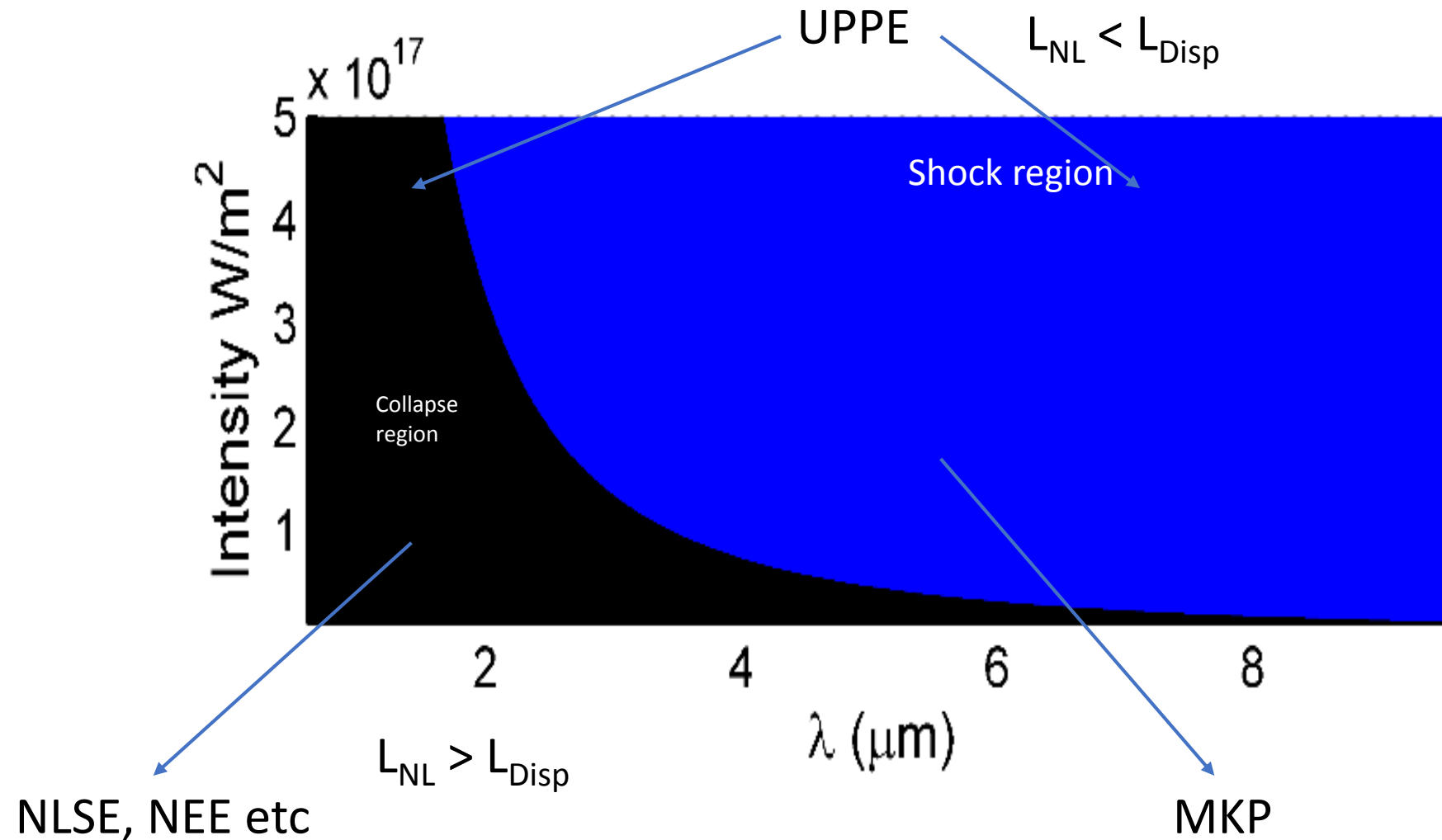


"half-cycle" waveform from a 100fs pulse at 6 micron





# Shock Regularization is Universal for Long Wavelengths



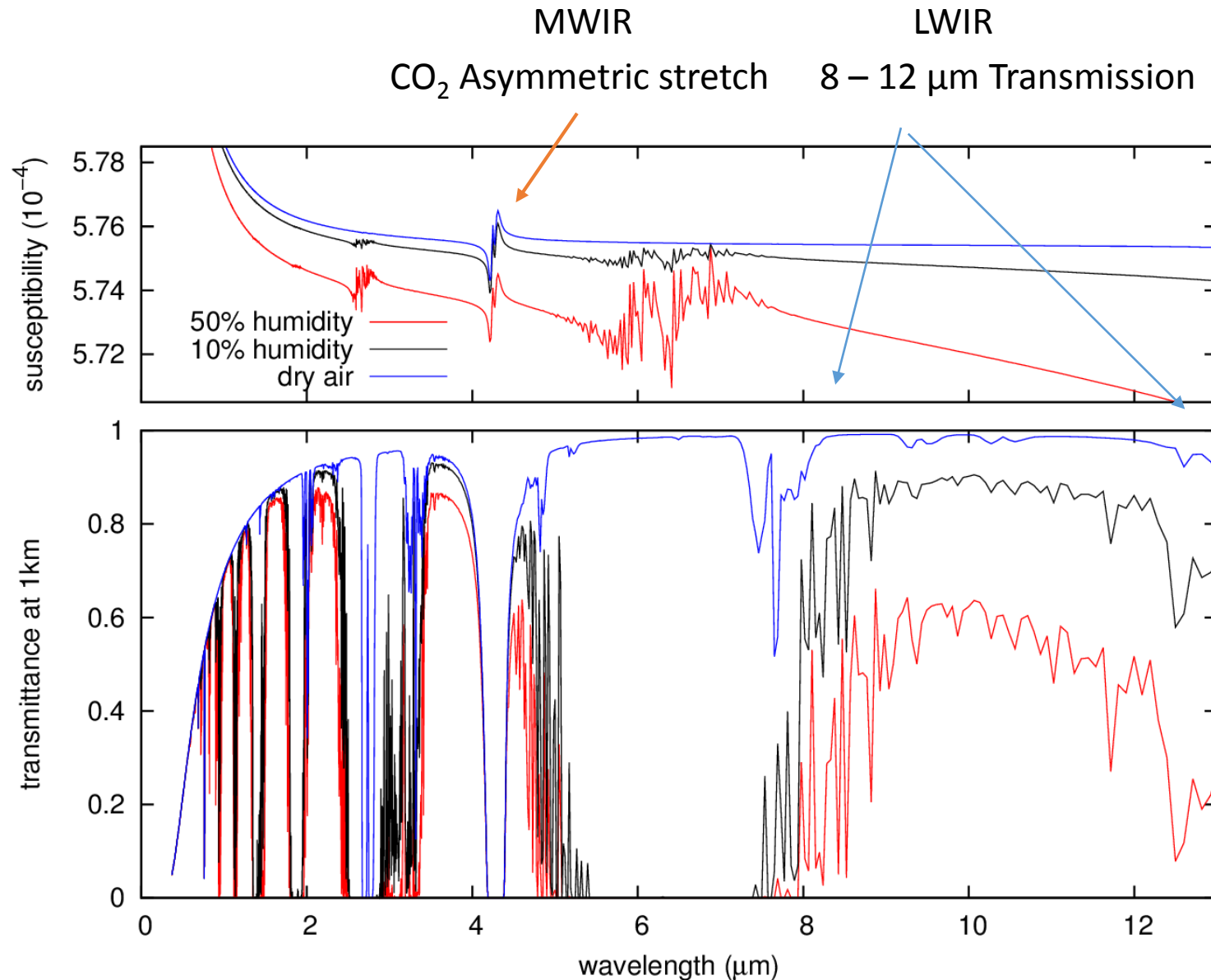


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# Atmospheric Transmission Windows (HITRAN)





# Multi-TW Mid-IR Light Bullet (4 $\mu\text{m}$ )

P. Panagiotopoulos, P. Whalen, M. Kolesik, and J. V. Moloney, Nat Photon **9**, 543 (2015)

Waist = 1cm

Power = multiple  $P_{\text{cr}}$

$\lambda = 4\mu\text{m}$

$\tau = 30\text{fs}$

## ☐ Initial State

- Onset of Collapse
- NLSE like

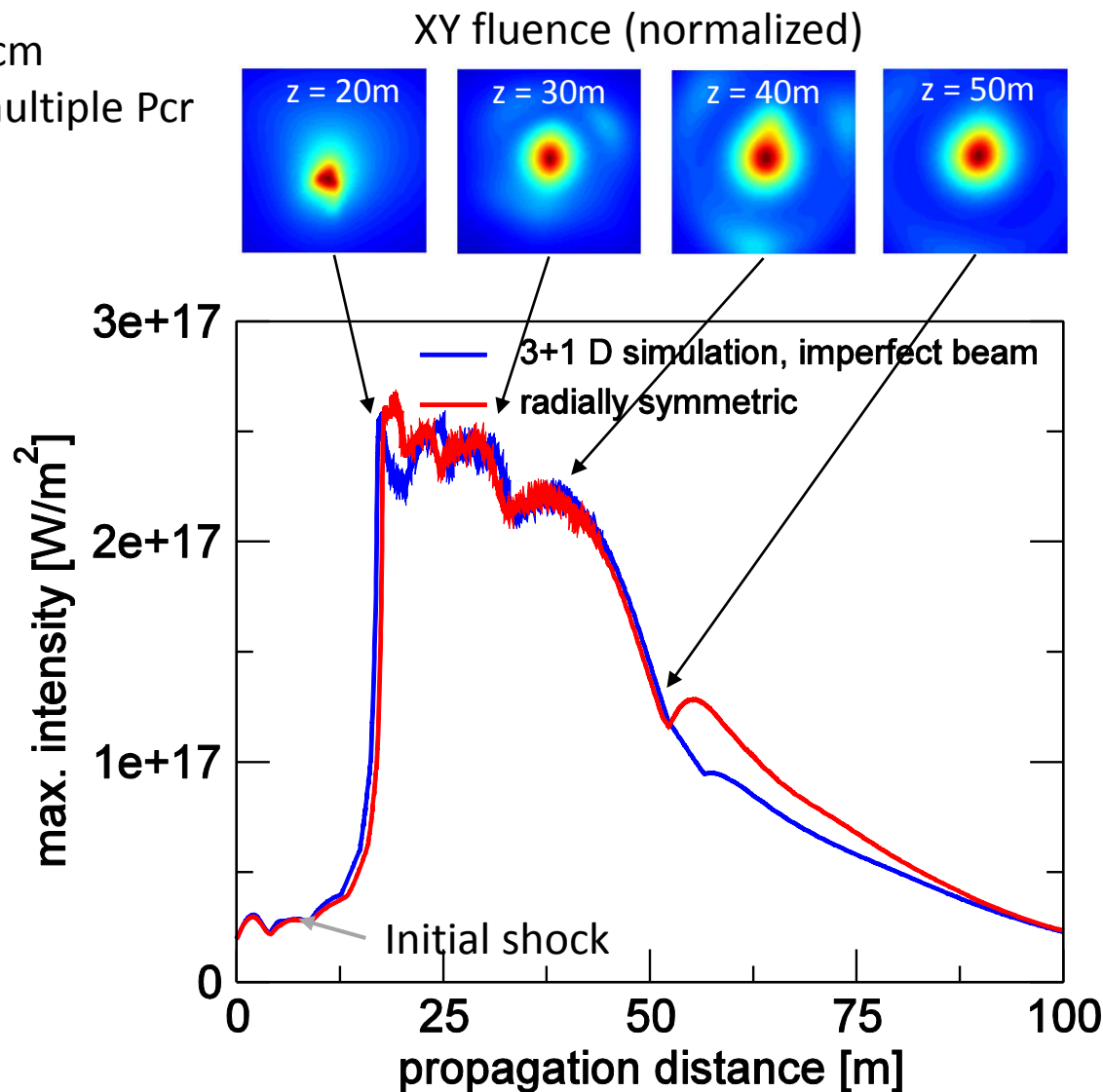
## ☐ Intermediate State 1

- high intensity shock
- MKP like

## ☐ Intermediate State 2

- slow shock walk-off
- regularizes collapse

## ☐ Multiple Recurrence

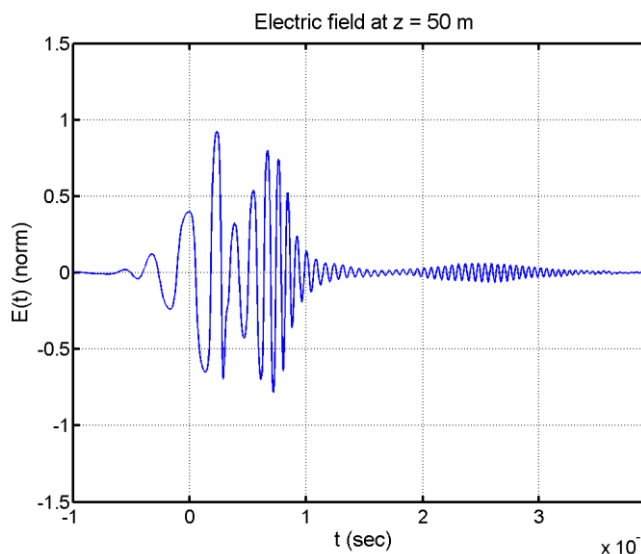
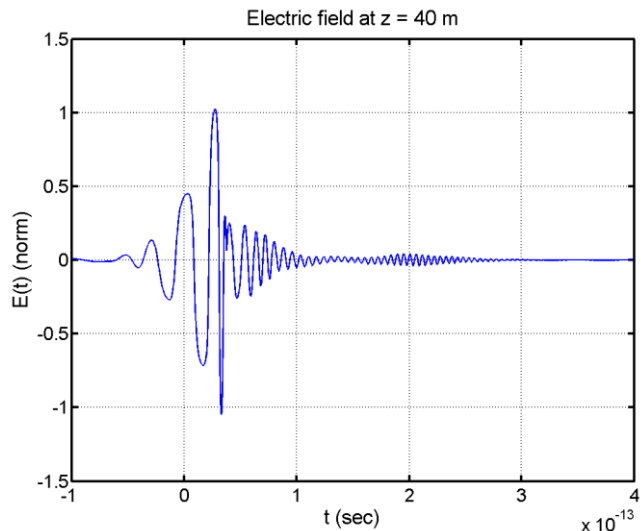
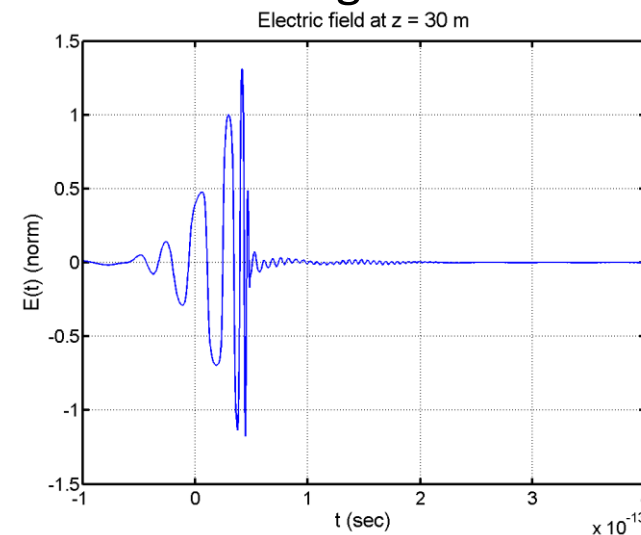
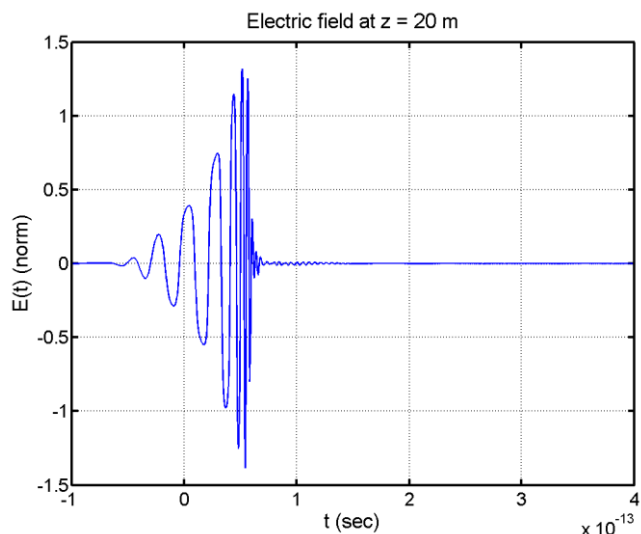




# Light Bullet Dynamics

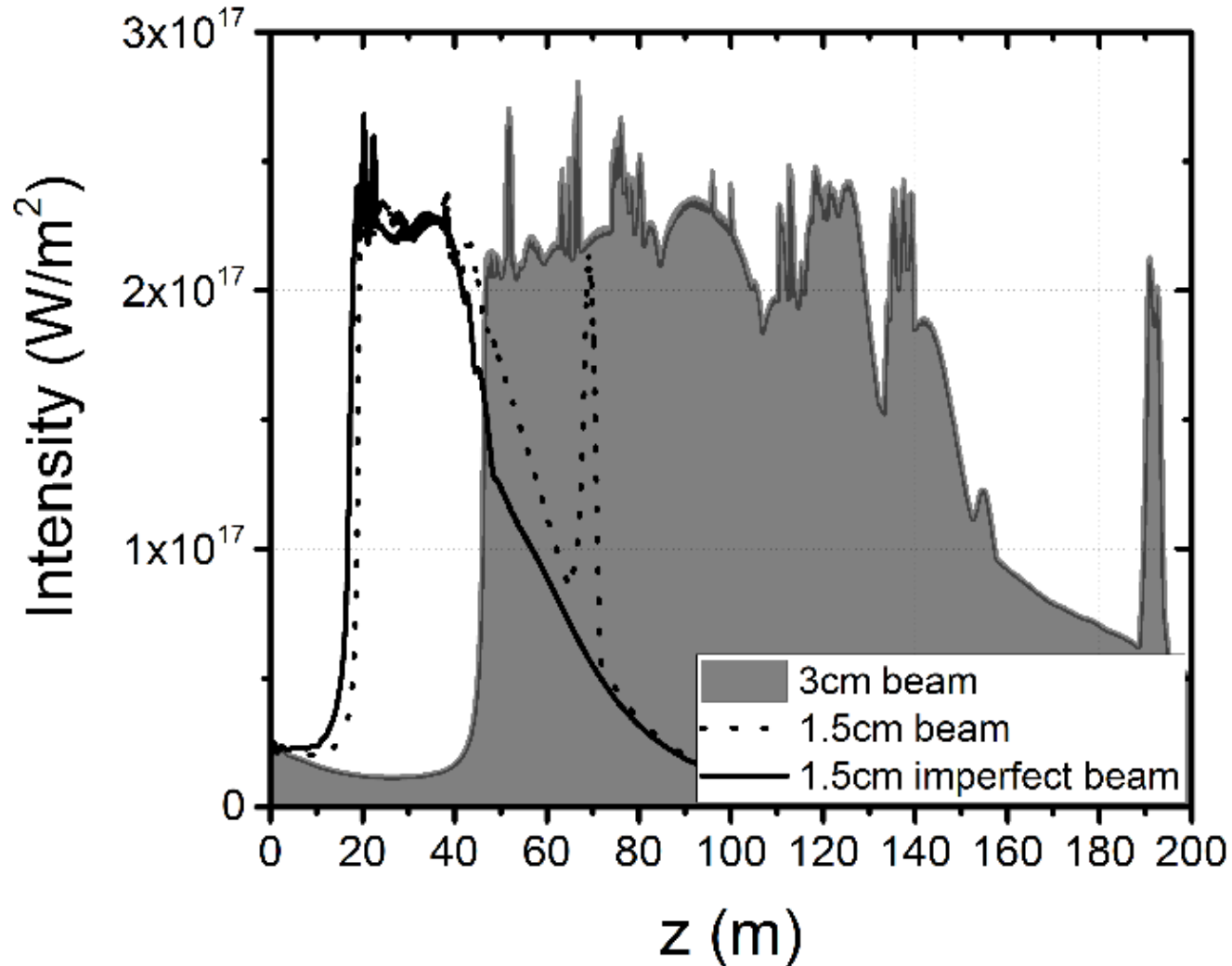
- ❑ Leading edge – quasi-invariant solitonic component
- ❑ Trailing edge – energy leakage into harmonics during walk-off

1D slice captured  
approximately by 1D  
mKdV with opposite  
sign for dispersion  
coefficient –  
nonintegrable case  
– P. Jakobsen





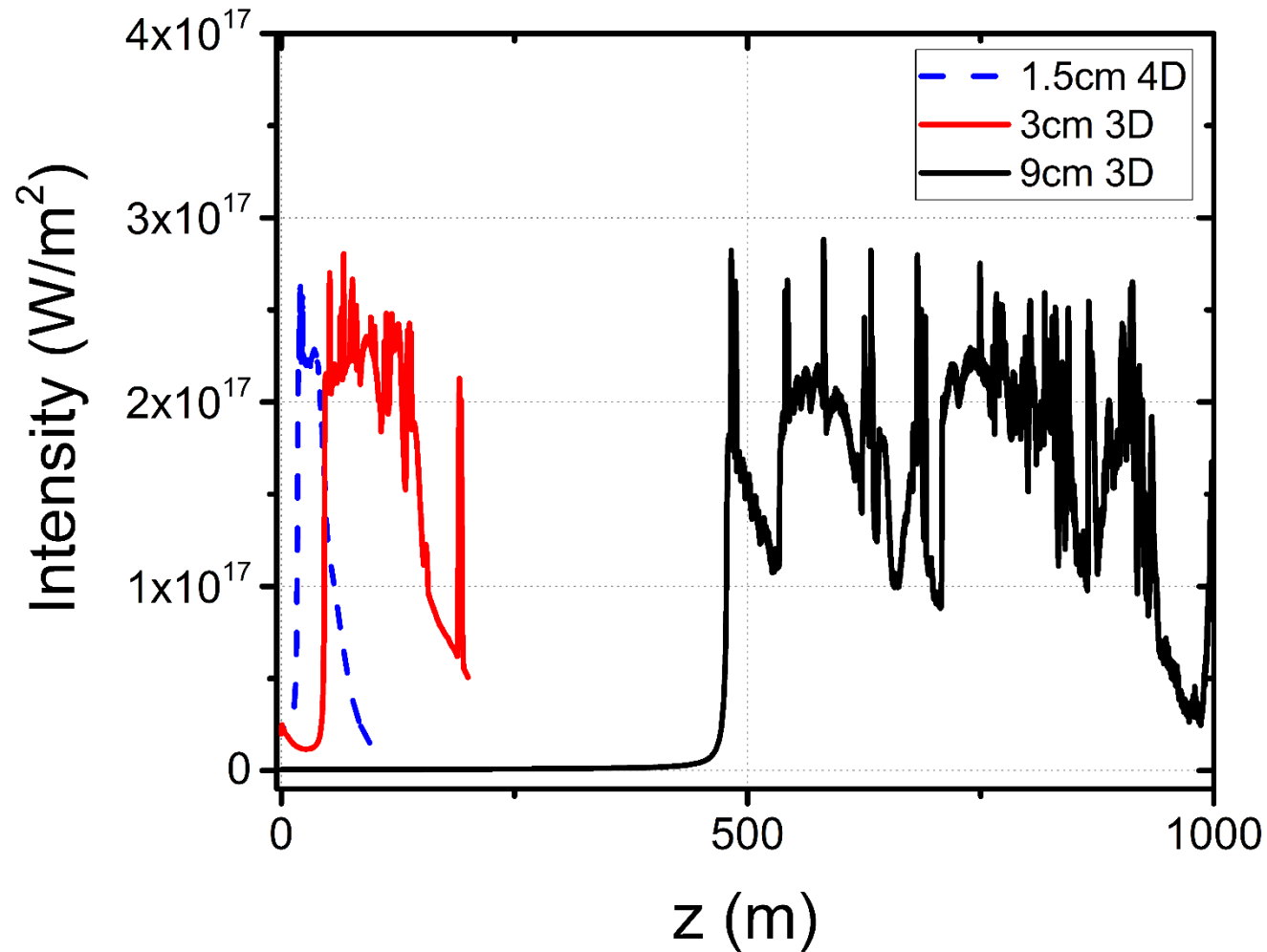
# Scaling Propagation Distance ( $4\text{ }\mu\text{m}$ )





## Filament Lengths vs pre-chirped 4 $\mu$ m – 9cm – 2.87 Joule

P. Paniagotopoulos et al. PRA **94**, 033852 (2016)

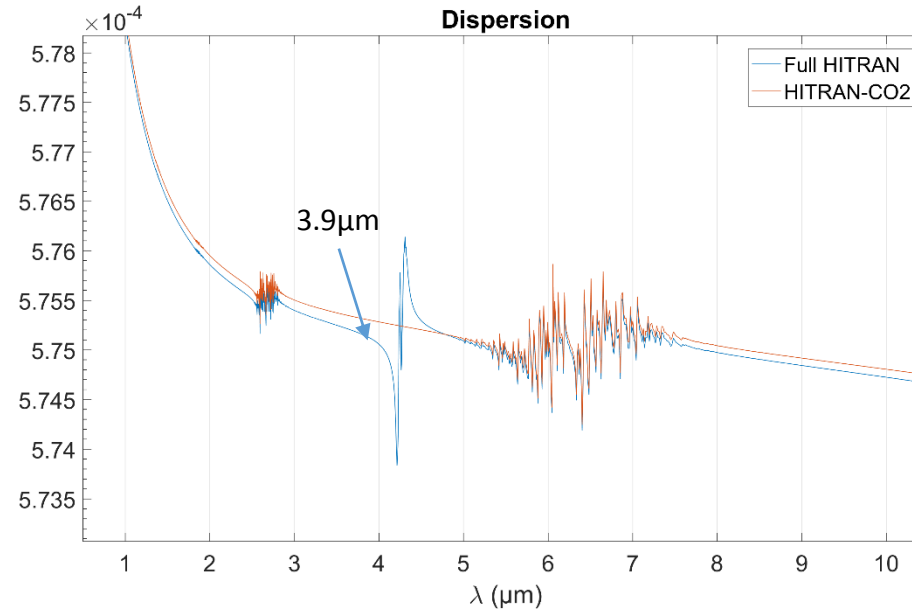
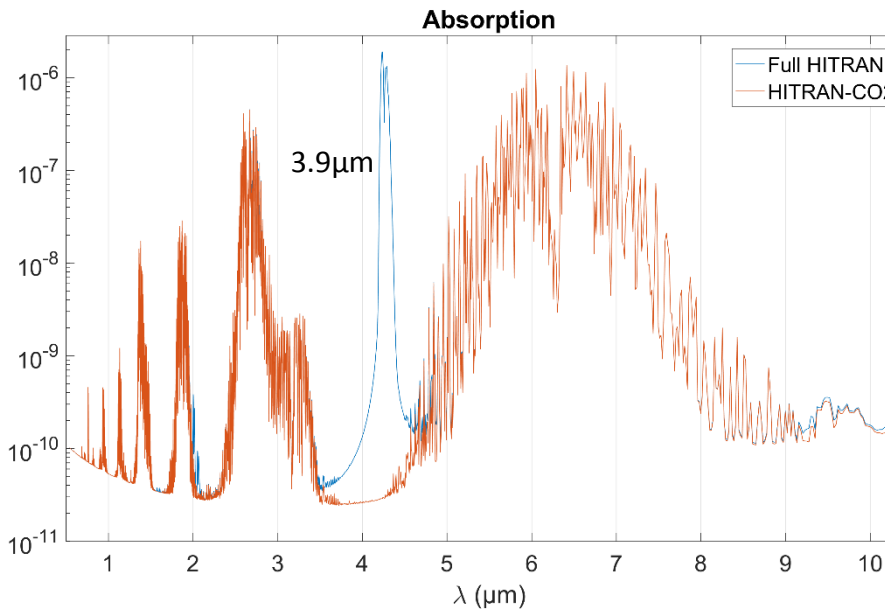






# MWIR Transmission around 3.9 $\mu\text{m}$

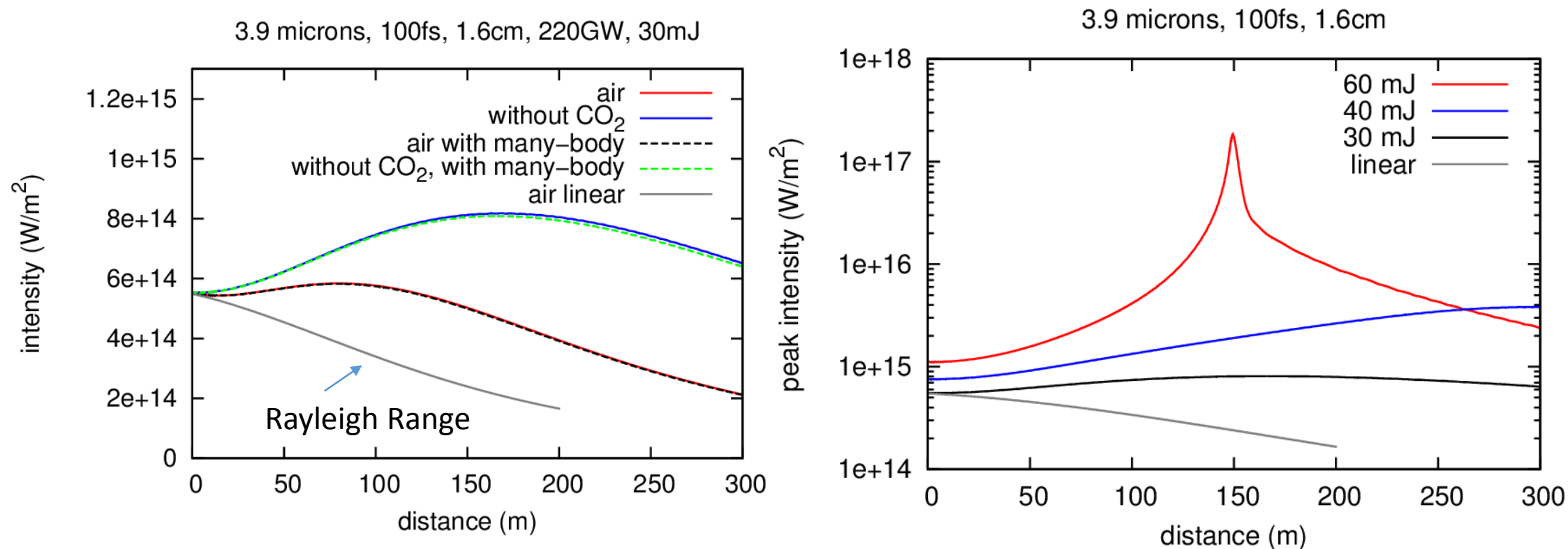
- Asymmetric  $\text{CO}_2$  rovibrational stretch - anomalous dispersion and absorption at short wavelength – soliton regime?



- Implications for long distance propagation?



# Above Critical Long Range Propagation



- Well above critical leads to self-phase modulational spectral broadening.



# Talk Outline

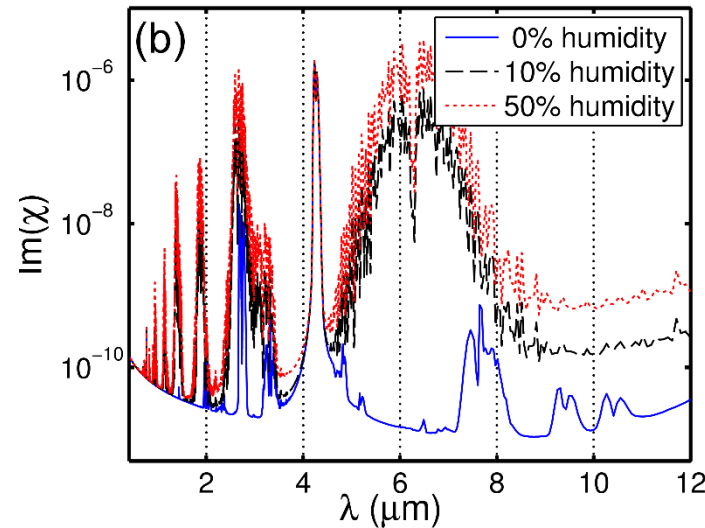
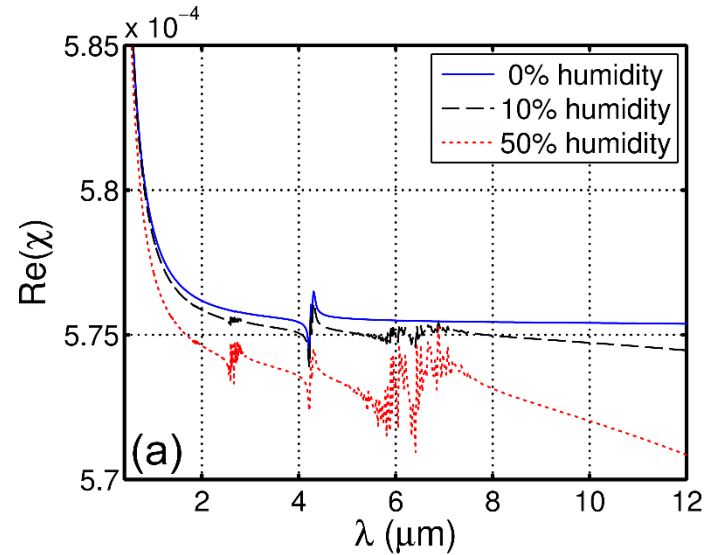
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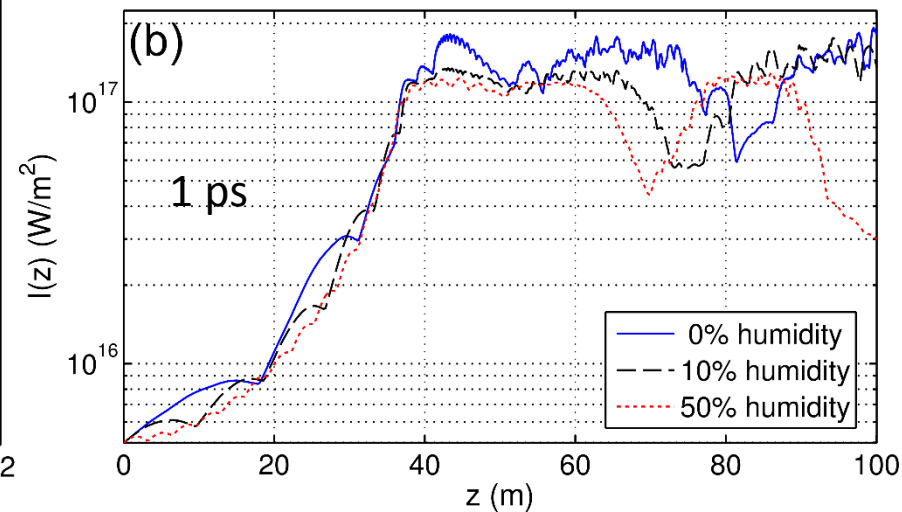
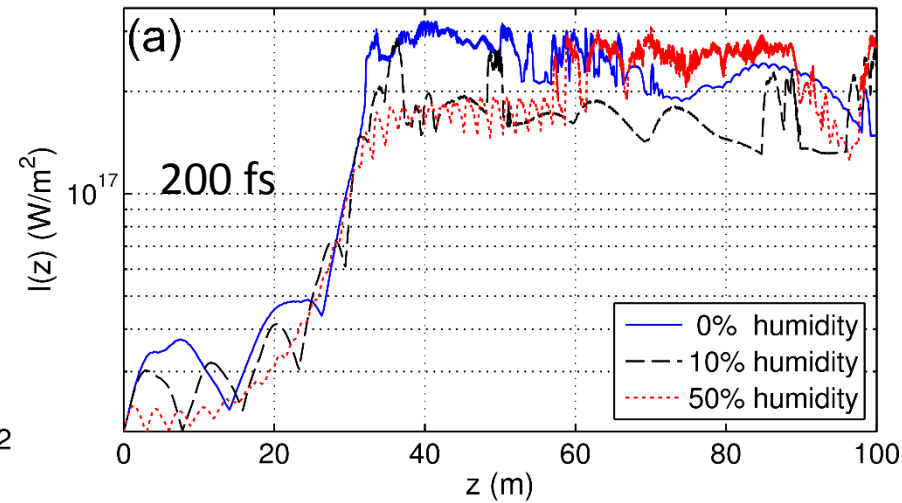
# 10 $\mu\text{m}$ Pulse Propagation in a Realistic Atmosphere

P. Panagiotopoulos et al. JOSA B **33**, 2154(2016). Expt n<sub>2</sub> S. Tochitsky et al. Optics Letters **14**, 3924 (2016)

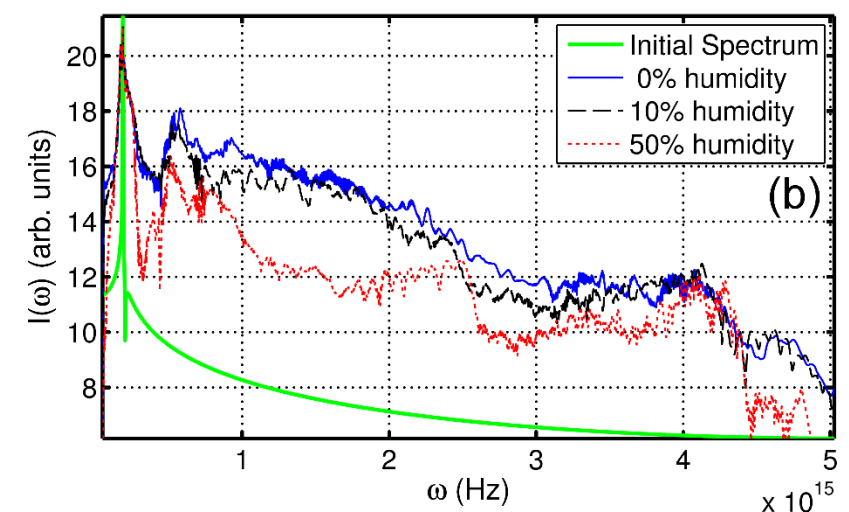
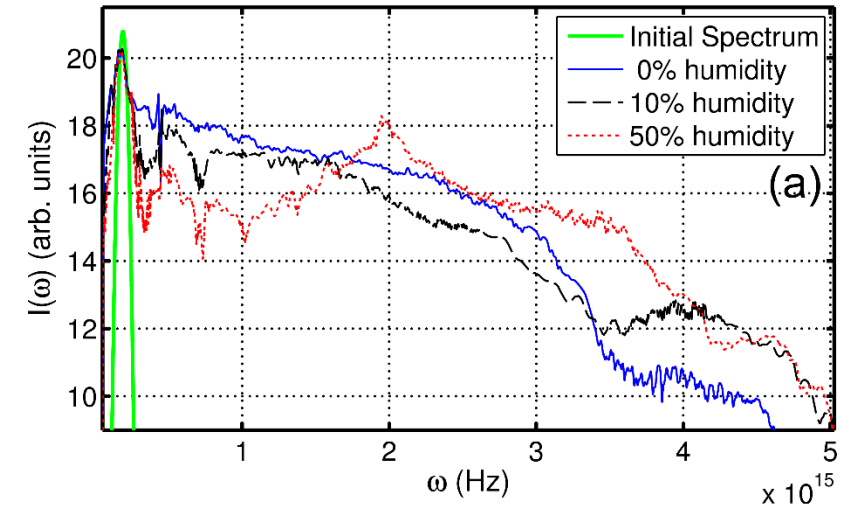
HITRAN Database



Peak Power over 100m



Spectra at 100m





# Quantum Many-Body Equations for Coulomb Scattering

K. Schuh et al., PRE **88**, 063102 (2013); PRE **89**, 033103 (2104); PRE **93**, 013208 (2016)

- Assume ions are stationary

$$i\hbar \frac{d}{dt} f_s = \sum_{\vec{k}} \Omega_{s\vec{k}}^* P_{s\vec{k}}^* - \Omega_{s\vec{k}} P_{s\vec{k}}$$

$$i\hbar \frac{d}{dt} f_{\vec{k}} = N \left[ \Omega_{s\vec{k}} P_{s\vec{k}} - \Omega_{s\vec{k}}^* P_{s\vec{k}}^* \right] - \frac{e}{\hbar} \vec{\nabla}_{\vec{k}} f_{\vec{k}} \vec{E}$$

$$i\hbar \frac{d}{dt} P_{\vec{k}\vec{k}'} = \left[ \dot{\epsilon}_{\vec{k}} - \dot{\epsilon}_{\vec{k}'} \right] P_{\vec{k}\vec{k}'} - \frac{e}{\hbar} \vec{\nabla}_{\vec{k}} P_{\vec{k}\vec{k}'} \vec{E} + \Omega_{s\vec{k}} P_{s\vec{k}'} - \Omega_{s\vec{k}'}^* P_{s\vec{k}}^*$$

$$i\hbar \frac{d}{dt} P_{\vec{k}\vec{k}'} = \left[ \dot{\epsilon}_{\vec{k}} - \dot{\epsilon}_{\vec{k}'} \right] P_{\vec{k}\vec{k}'} - \frac{e}{\hbar} \vec{\nabla}_{\vec{k}} P_{\vec{k}\vec{k}'} \vec{E} + \Omega_{s\vec{k}} P_{s\vec{k}'} - \Omega_{s\vec{k}'}^* P_{s\vec{k}}^*$$

Requires solution of Quantum Boltzmann Equation

$$H_{el-el} = \frac{1}{2} \sum_{\vec{q}, \vec{k}, \vec{k}'} a_{\vec{k}}^{\dagger} a_{\vec{k}'}^{\dagger} a_{\vec{k}+\vec{q}} a_{\vec{k}-\vec{q}} W(q)$$



# Long Wavelength Scaling of Critical Parameters

Critical Power:

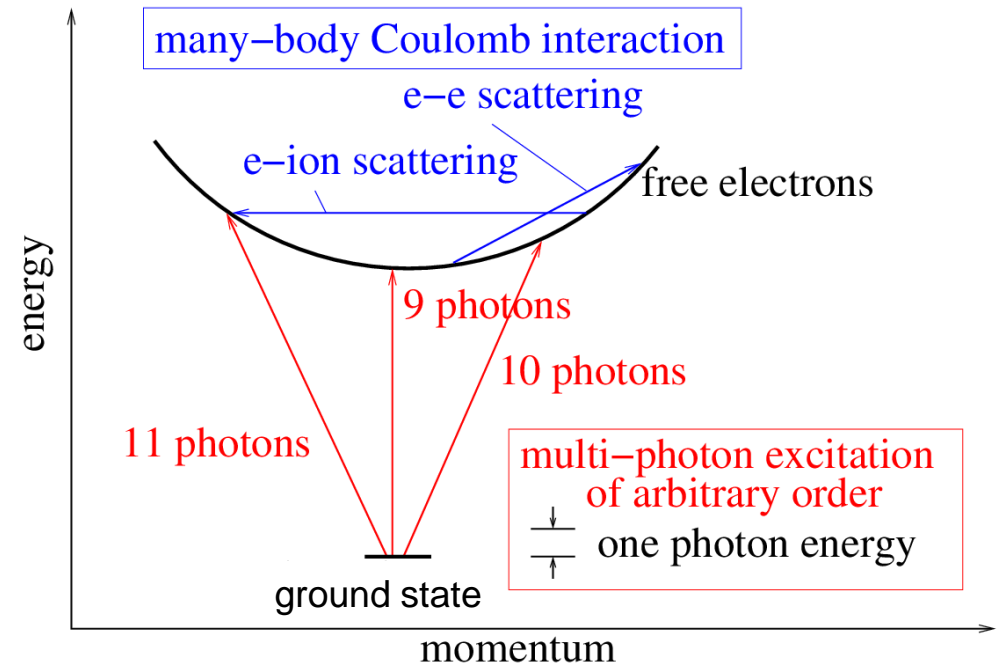
$$P_{\text{crit}} = \frac{0.3\lambda^2}{nn_2}$$

Ionized Electron Polarization

$$P_{\text{pl}} = -f(t) \frac{e^2 \mu_0}{m} \lambda^2 E$$

Ionized Electron Density

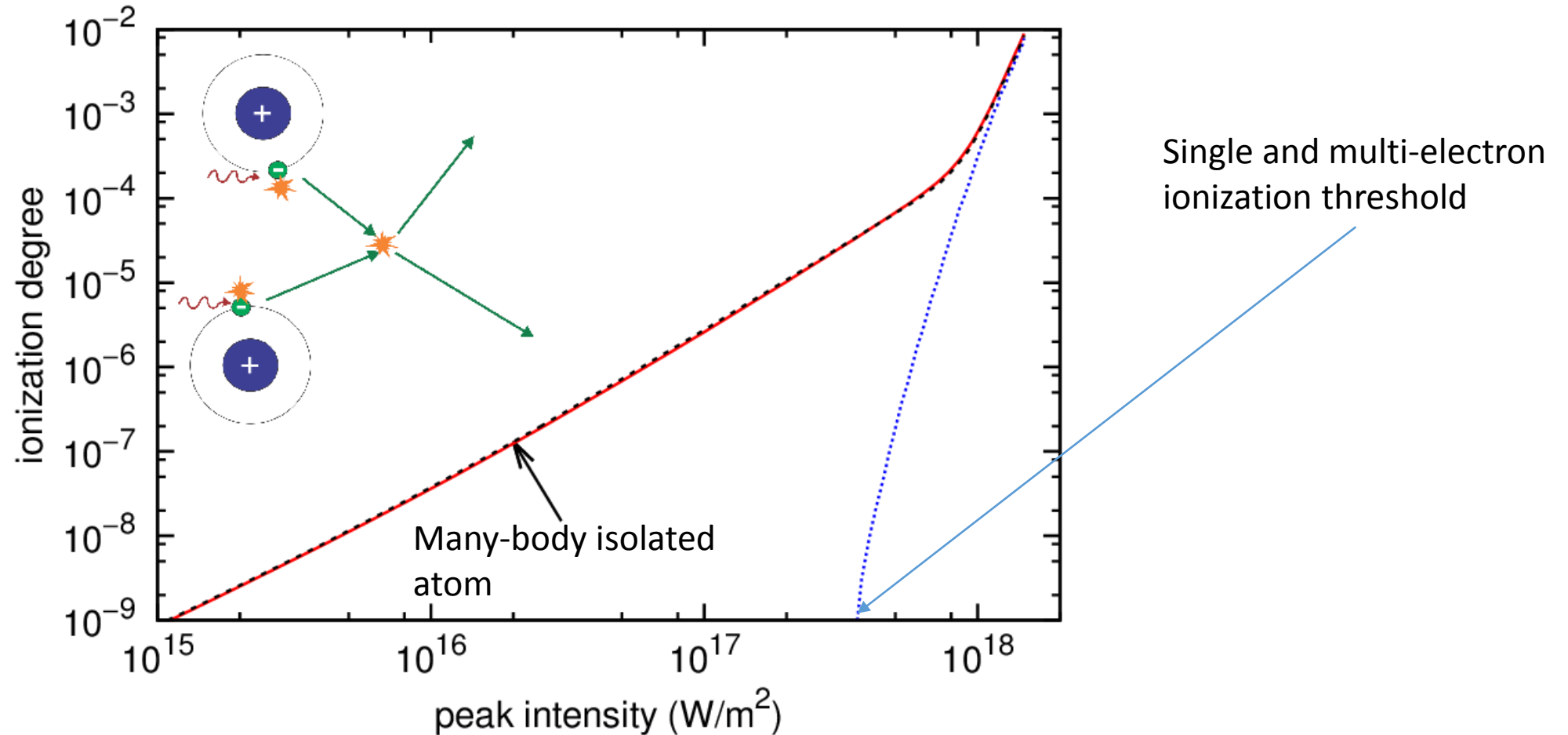
$$n_{\text{pl}} = -f(t) \frac{e^2 \mu_0}{2m} \lambda^2$$





# Self-Channeling of High Power LWIR Pulses in Atomic gases

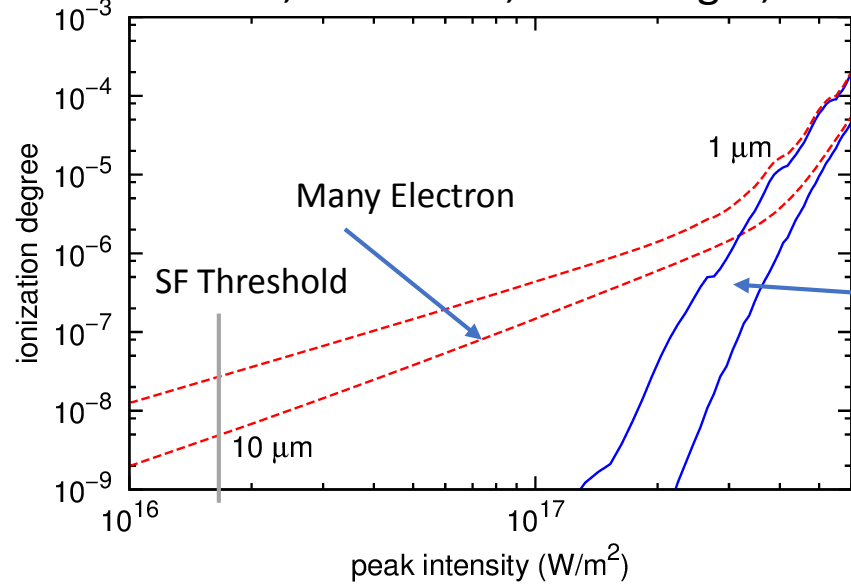
K.Schuh, M. Kolesik, E.M. Wright, J.V Moloney and S.W Koch, PRL, **118** 063901 February 10 (2017)



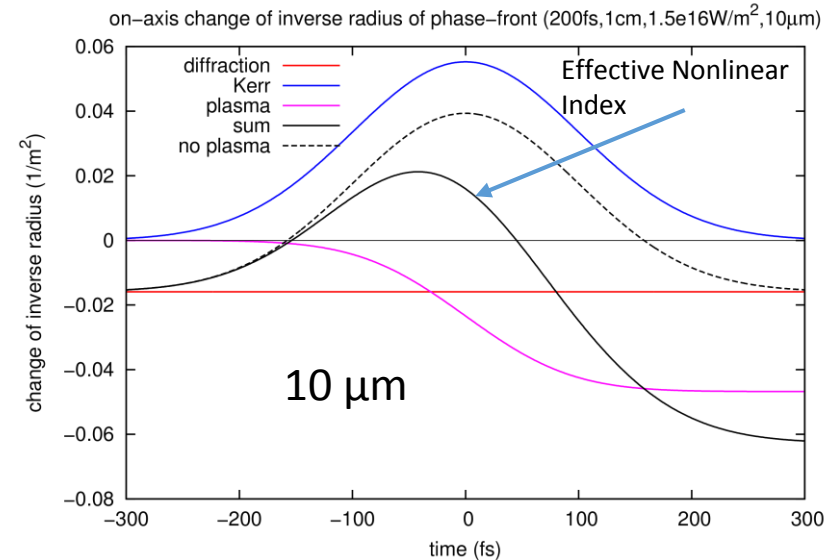
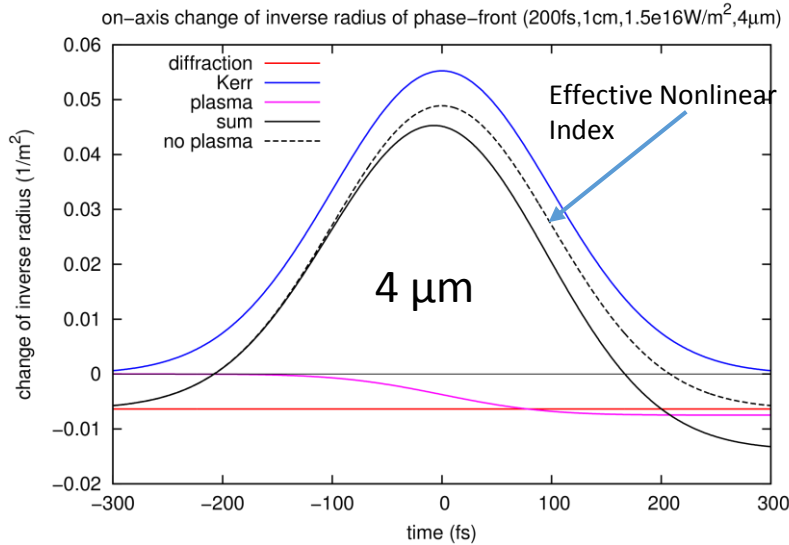
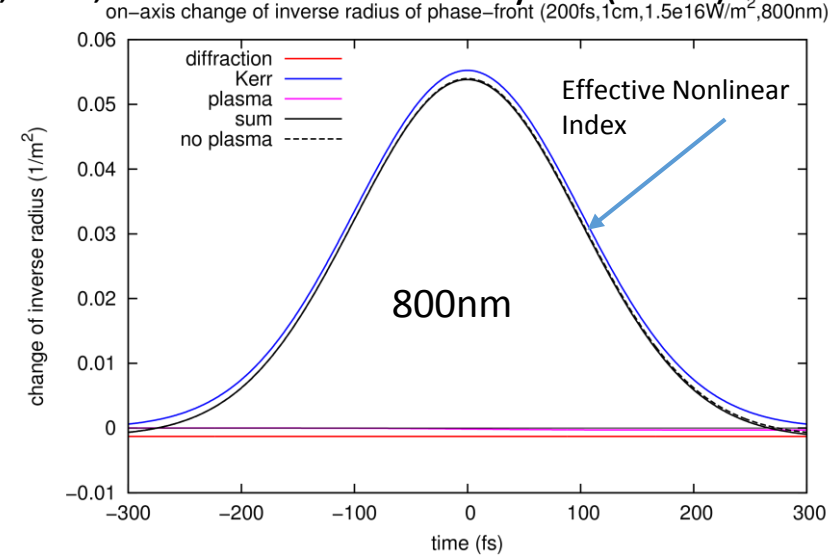


# Many-Body Interactions of Weakly Ionized Electrons

K.Schuh, M. Kolesik, E.M. Wright, J.V Moloney and S.W Koch, PRL, **118** 063901 February 10 (2017)



Single Active and multi-Electron (MESA)  
M. Kolesik

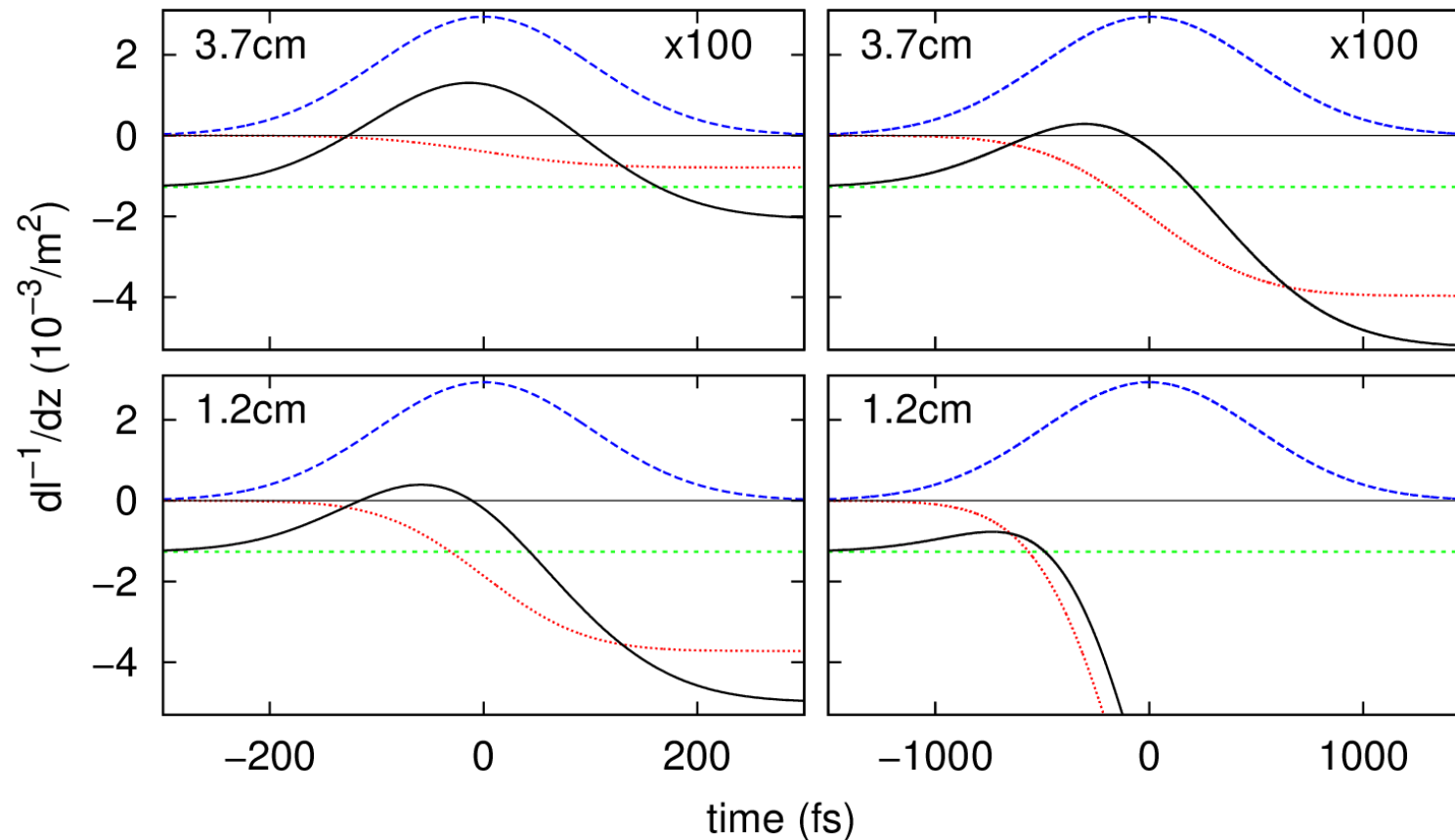






# Physics of beam confinement – Dynamical Index Suppression

- K.Schuh et al., PRL **118**, 063901 (10 Feb. 2017)
- Hold power fixed but shrink waist – turns off effective Kerr lensing (10 $\mu$ m)

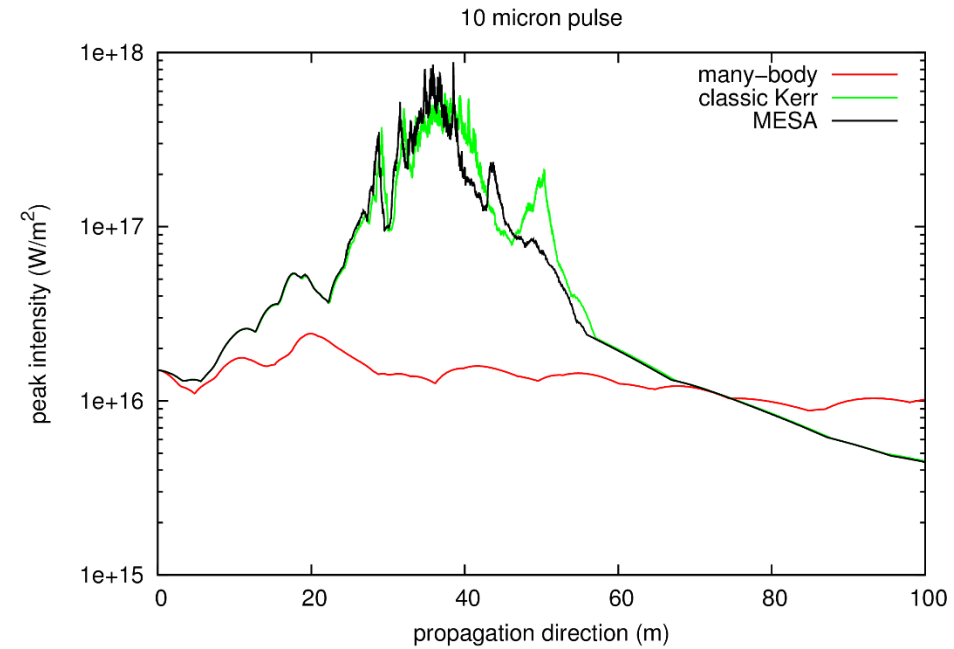
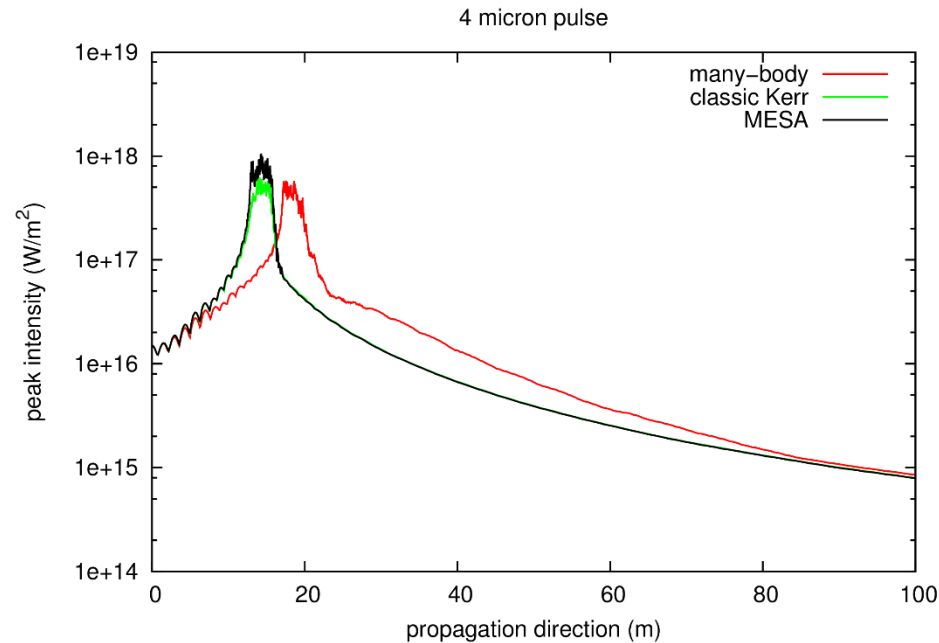


- Beam confinement sensitive to launch conditions and cumulative ionization



# Propagation Characteristics at 4 and 10 $\mu\text{m}$

- K.Schuh et al., PRL **118**, 063901 (10 Feb. 2017)
- Use Argon as test medium – no molecular contributions;  $n_2$  comparable to air electronic



## Prediction:

- Weak positive lens keeps waist collimated but no localized filament



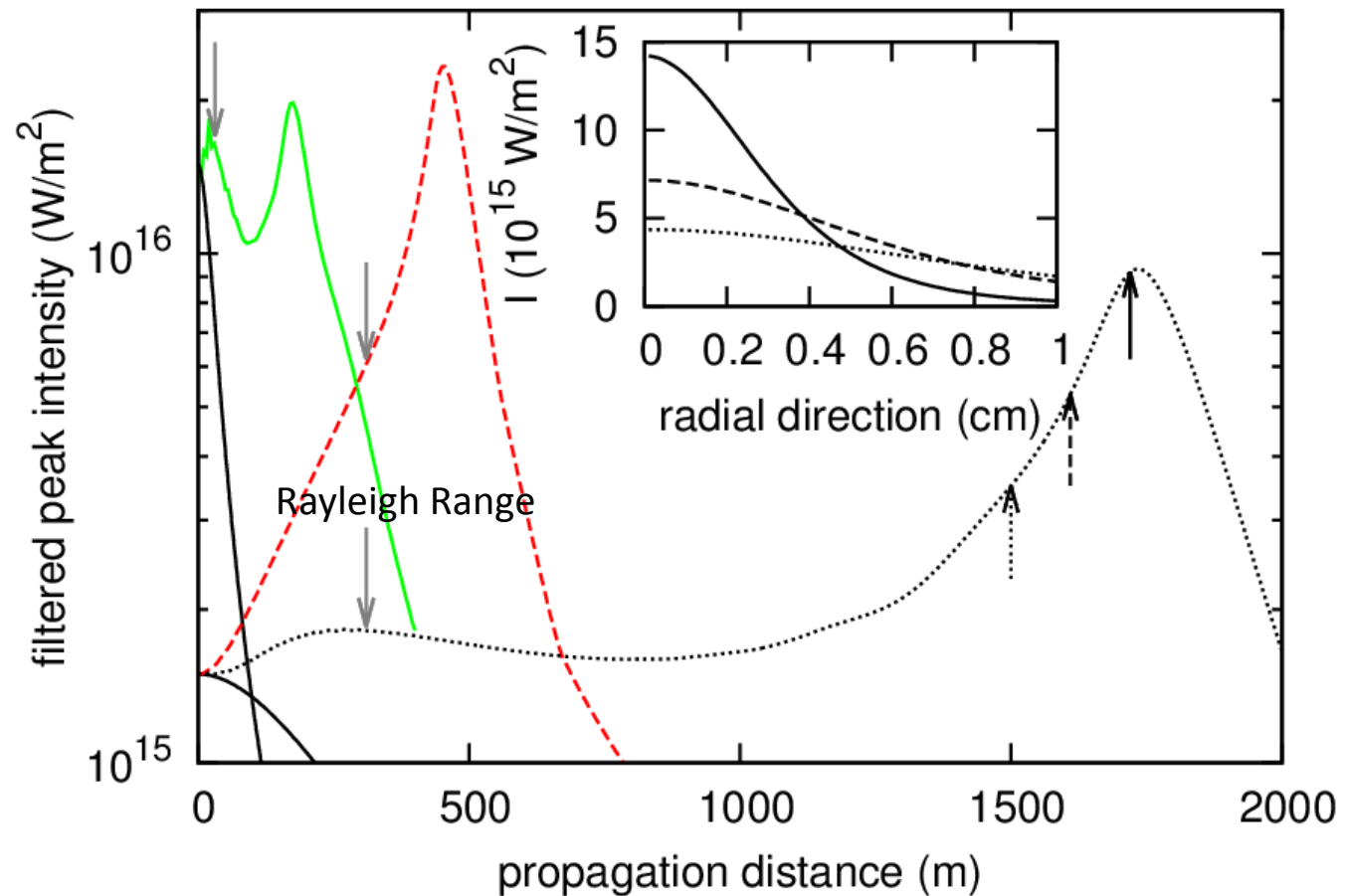
# Long Range Multi-Joule Pulse Delivery

K.Schuh, M. Kolesik, E.M. Wright, J.V Moloney and S.W Koch, PRL, **118** 063901 February 10 (2017)

- Cumulative ionization (plasma) dispersion weakens effective Kerr lens

## Beam characteristics at 10 $\mu\text{m}$

- 100 fs pulse – filament (red dashed)
- 1 ps pulse - Self-trapped whole beam self-channeling (black dashed).
- Weak self-focusing compression beyond 1.5 km

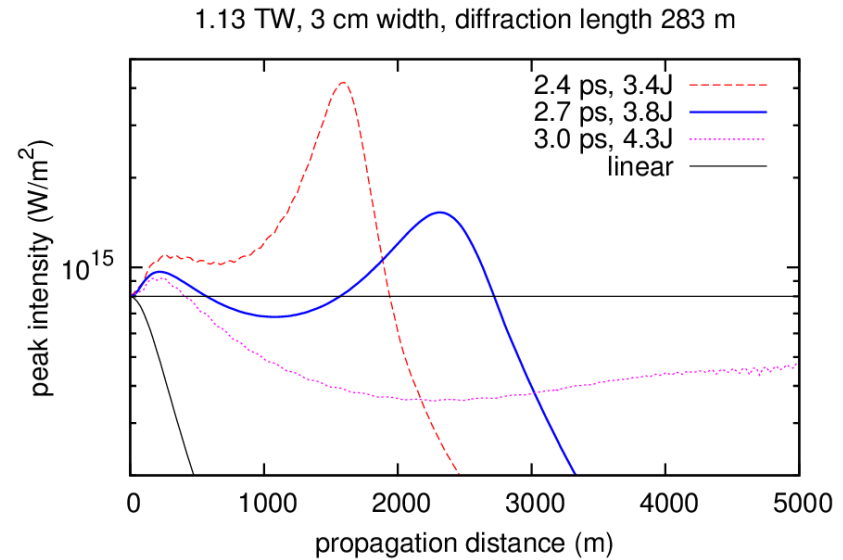
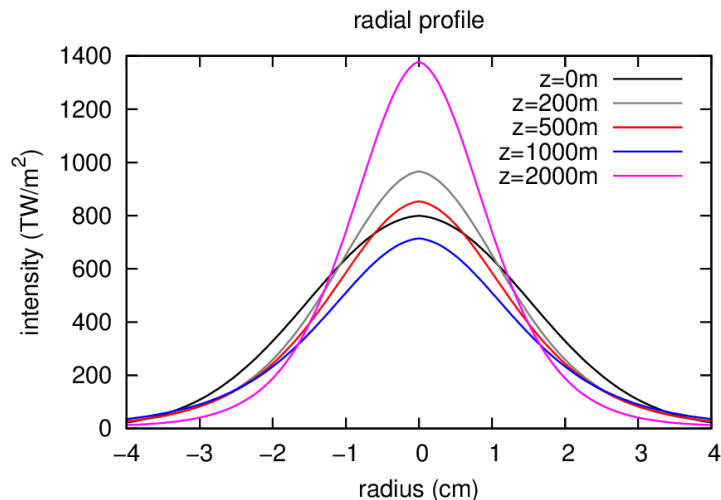




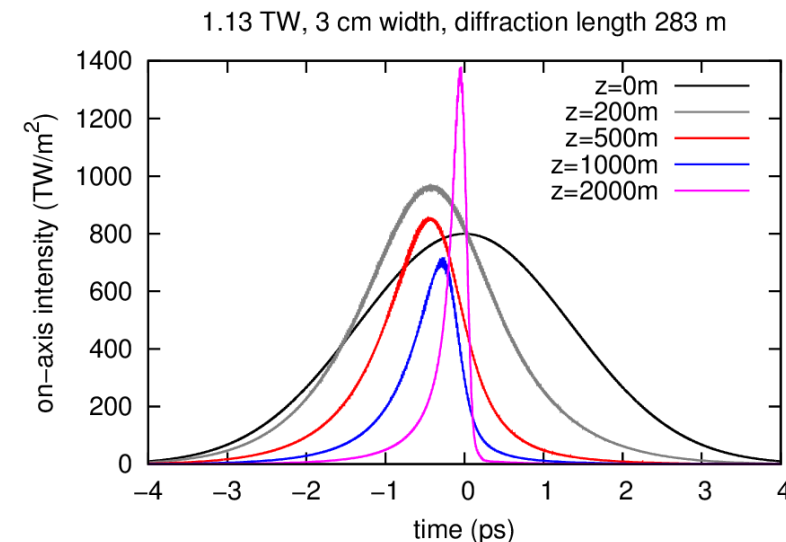
# Multi-Kilometer Air Propagation at $10\mu\text{m}$

- Fix peak power above critical
- Increase energy (pulse duration)
- Longer (higher energy) pulses tend to suppress strong focus but self-trap over longer ranges.

Whole beam radial compression beyond 2km

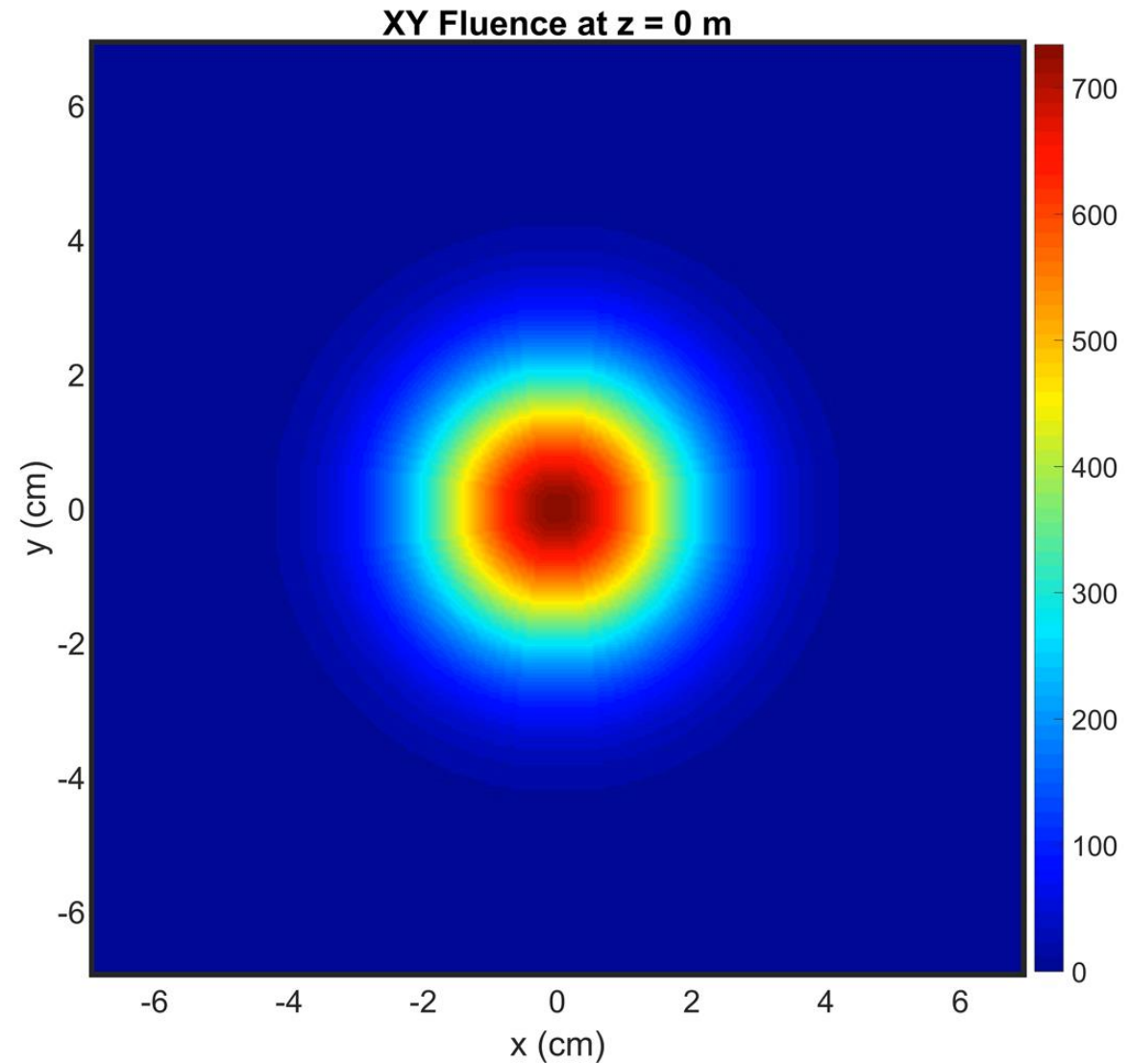
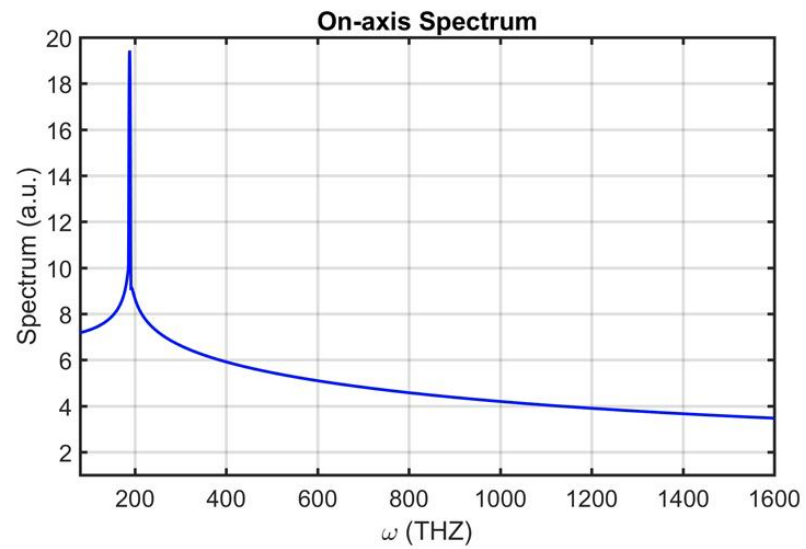
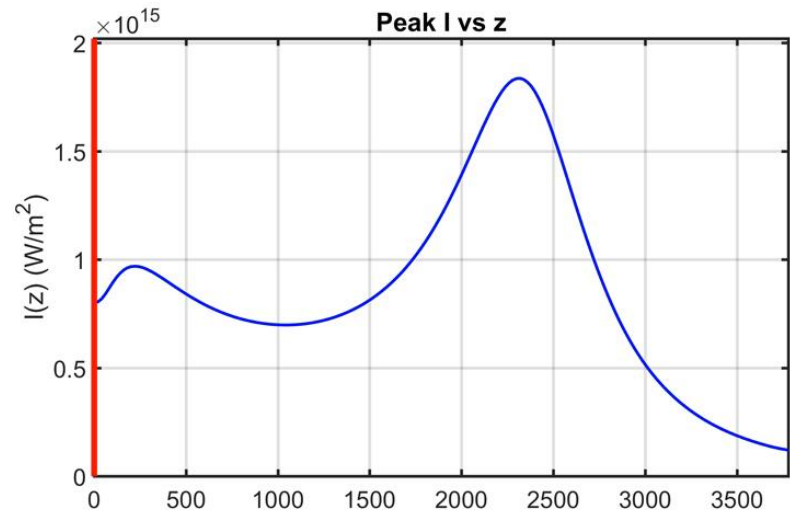


Strong pulse compression in time





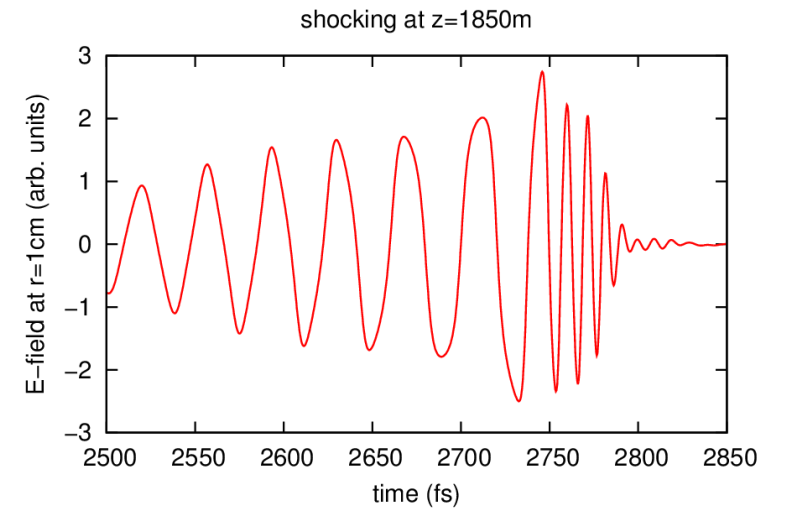
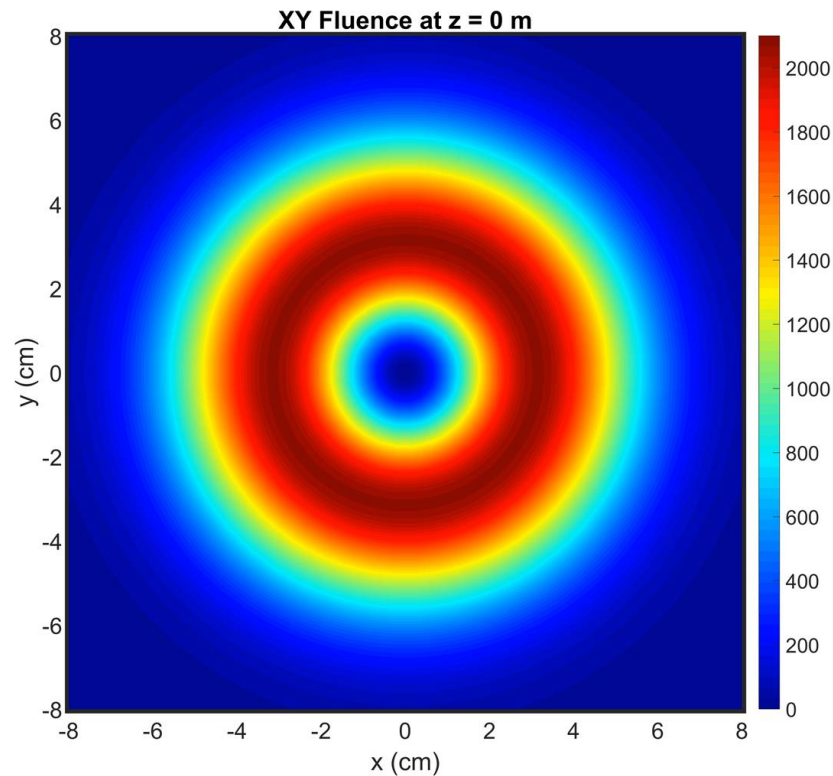
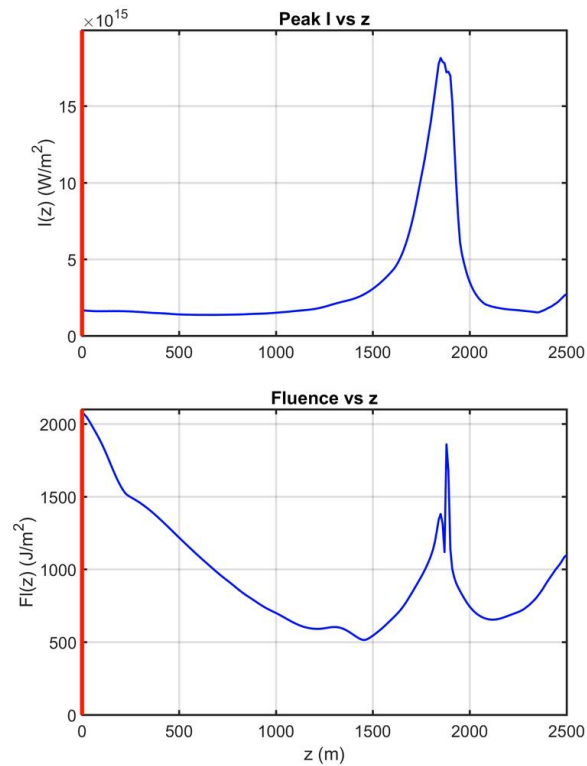
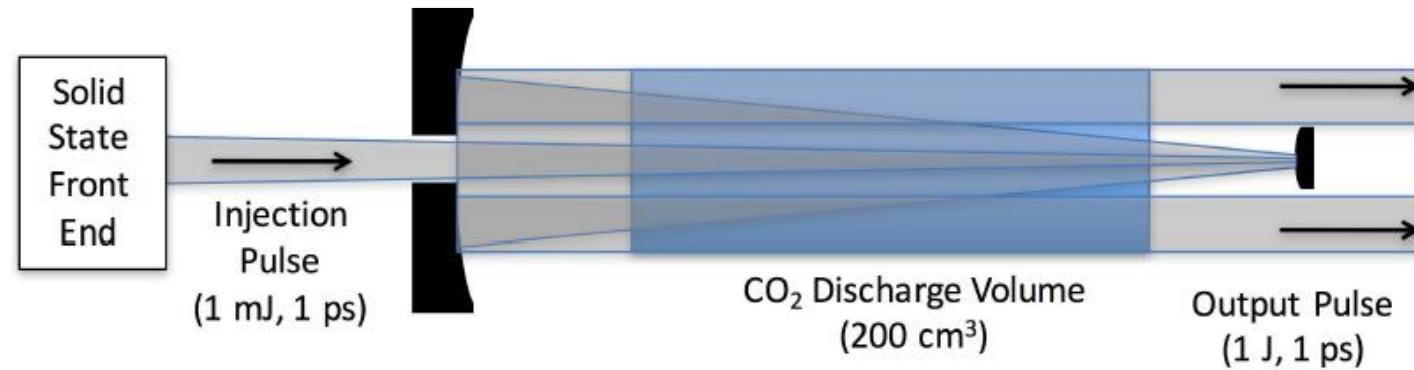
# Whole Beam Self-trapping





# Non-Gaussian Vortex Beams

- D. Gordon et al Proc. SPIE Vol 9835, (2016)





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# Summary and Conclusion

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- Recurrent carrier shocks maintain light bullet  $\sim 100$ 's meters.
- Carrier shock and blow-up singularity act in concert to maintain solitonic leading edge – envelope description invalid.
- Anomalous dispersion and absorption around  $4.3\mu\text{m}$  limits propagation
- Potential to create very long thermal waveguides
- Many-body effects enable self-trapping over multiple kilometers
- Pulse stays trapped over tens of ( $>20$ ) Rayleigh ranges of the launched beam.
- Currently developing a nonlinear HITRAN database