



# ***Physics of Coupled, Multi-Scale Nonequilibrium Flows***

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# Challenges of Multi-scale Nonequilibrium Flows

- **Multiscale flows include regions of equilibrium and non-equilibrium.**
- **Understand sensitivity of flows to physical models such as thermal relaxation and chemistry.**
- **Use experiments to validate approach:**
  - **Data from HET to validate gas dynamic- shock interactions,**
  - **Spectral emissions to validate thermochemical models (especially NO emissions.)**
- **Want to treat these using non-continuum, particle approaches:**
  - **Severe numerical constraints,**
  - **Employ hybrid, particle methods → quest for breakdown criteria.**

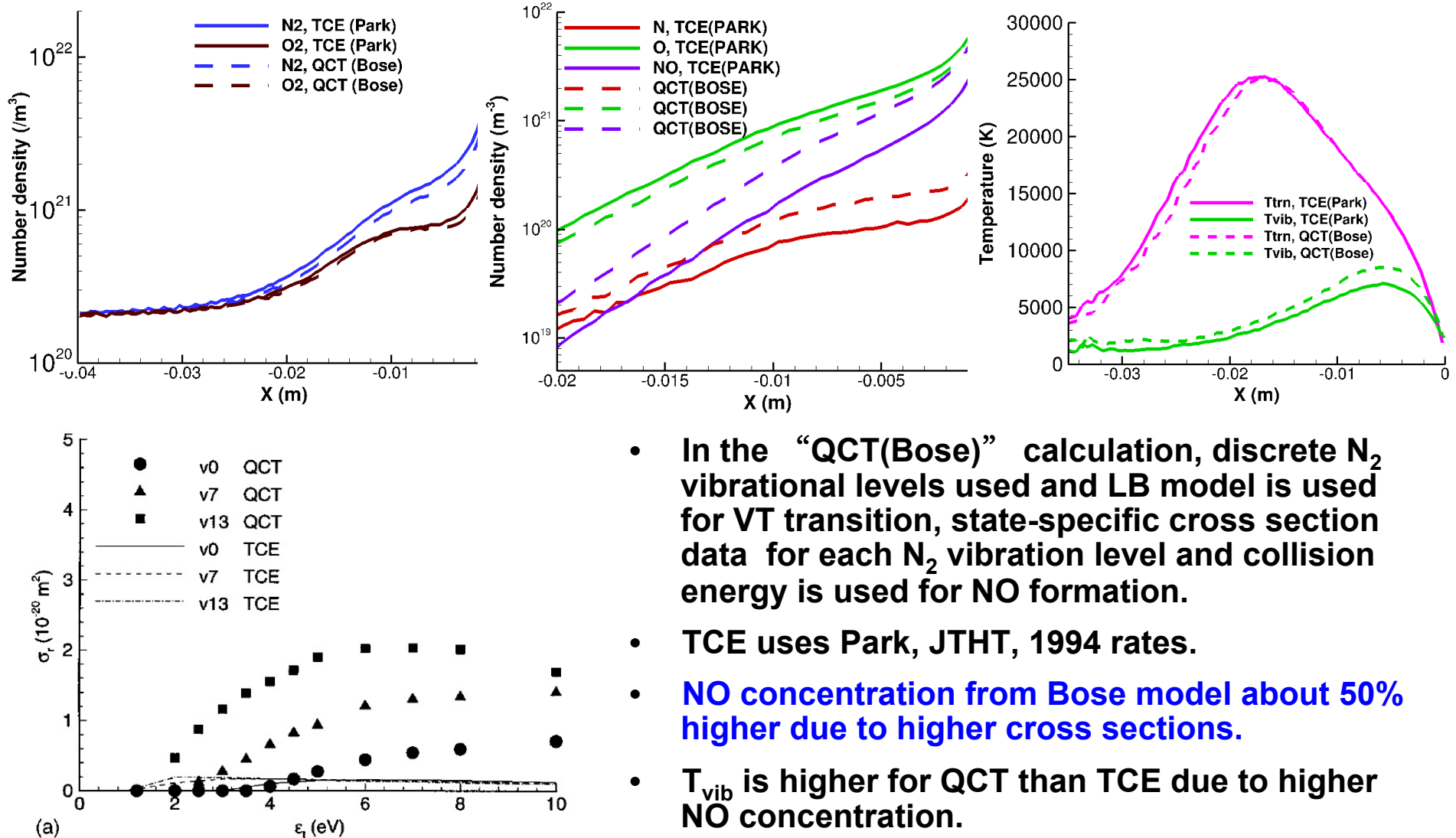


## Objectives and Approach of Thermochemical Modelling

- The transitions between the vibrationally excited states of the nitrogen molecule, as well as its dissociation, and formation of NO from different vibrational excited states are being modeled.
- The relaxation models that will be assessed include the discrete LB VT rate model, Schwartz-Slawsky-Herzfeld (SSH) V-T model, and Forced Harmonic Oscillator (FHO) V-T model.
- The chemistry models include: (1) TCE, (2) QCT - Bose, and (3) QCT - Jaffe and Magin ( $N_2$  dissociation.)
- *Electronic excitation of NO molecules using quenching rate data from recent experiments are modeled for accurate calculation of spectral radiation.*

# Sensitivity of NO Formation to Chemistry Model TCE vs. QCT/Bose $N_2 + O \rightarrow NO + N$

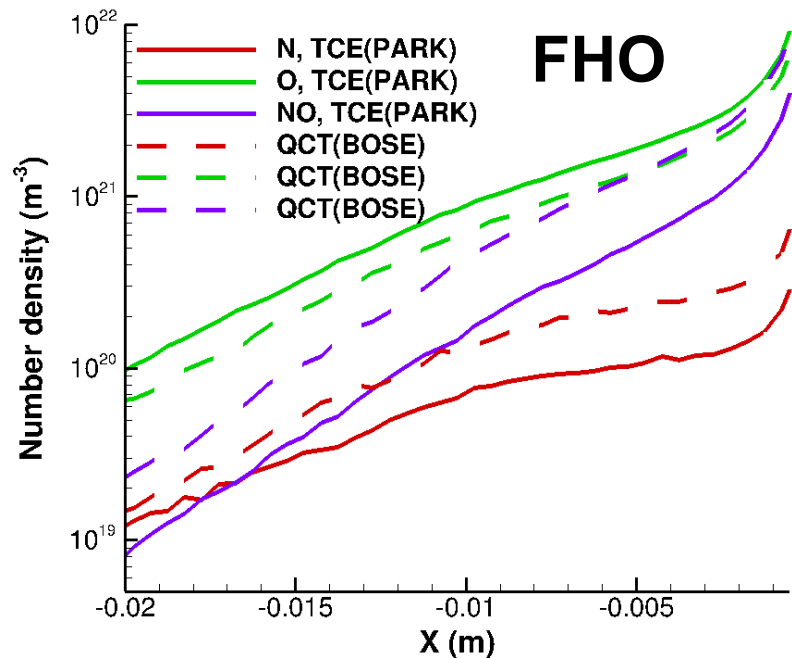
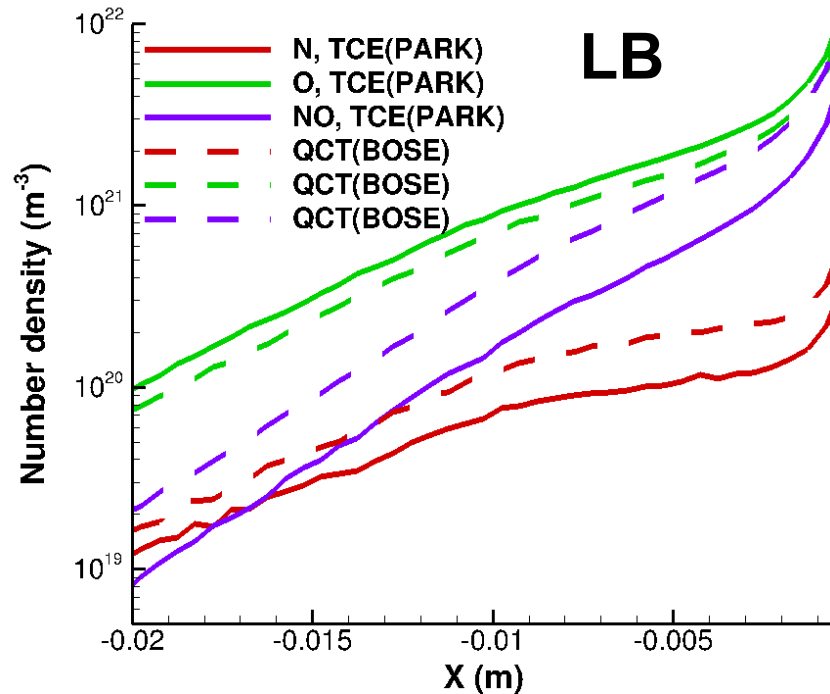
7km/s, 81 km, free stream, 50%  $N_2$  and 50%  $O_2$



- In the “QCT(Bose)” calculation, discrete  $N_2$  vibrational levels used and LB model is used for VT transition, state-specific cross section data for each  $N_2$  vibration level and collision energy is used for NO formation.
- TCE uses Park, JTHT, 1994 rates.
- **NO concentration from Bose model about 50% higher due to higher cross sections.**
- $T_{vib}$  is higher for QCT than TCE due to higher NO concentration.

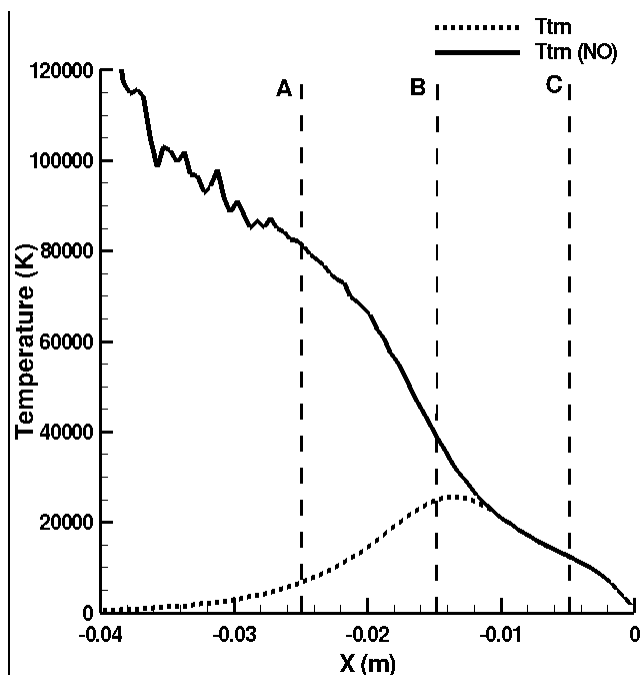
# Sensitivity of NO formation to Chemistry and VT Transition Models

7km/s, 81 km, free stream, 50% N<sub>2</sub> and 50% O<sub>2</sub>

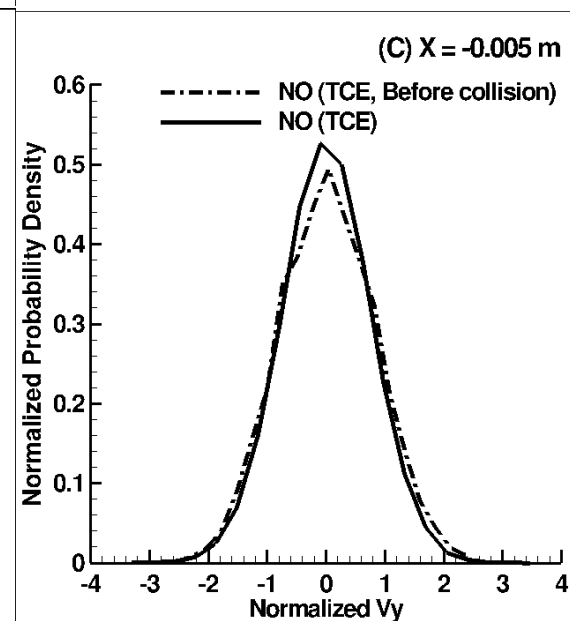
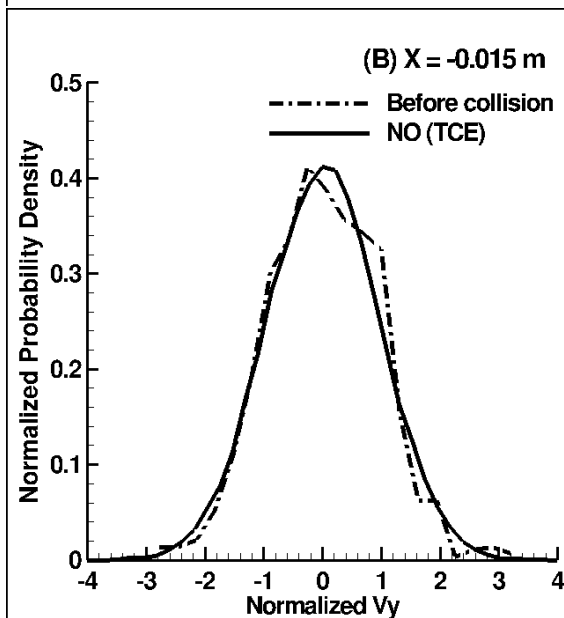
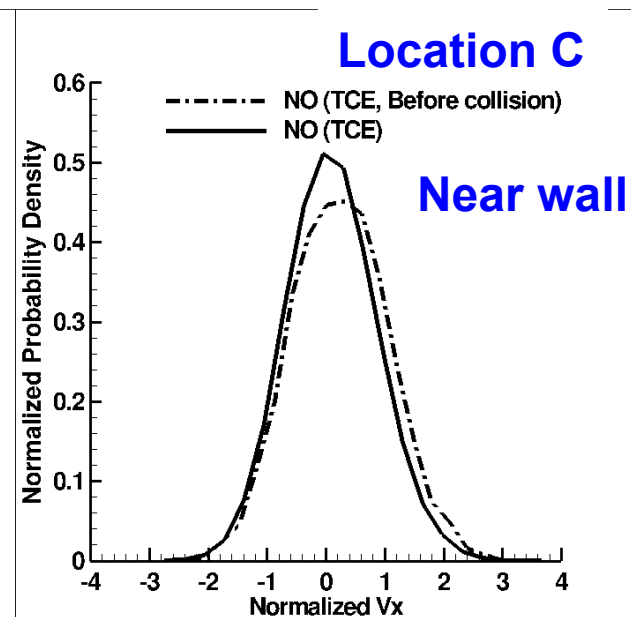
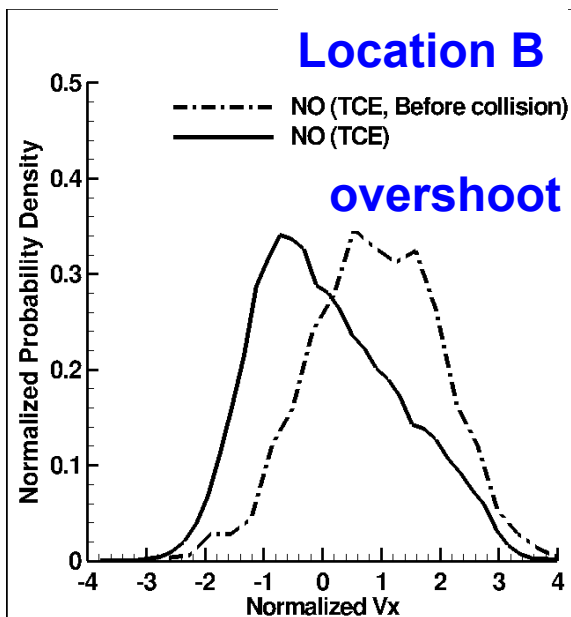


- When QCT chemistry is applied, the NO number density from FHO case is about 20% higher than the LB case.
- Using FHO for VT and QCT for chemistry significantly increases the NO formation in the 81 km and 7km/s case.

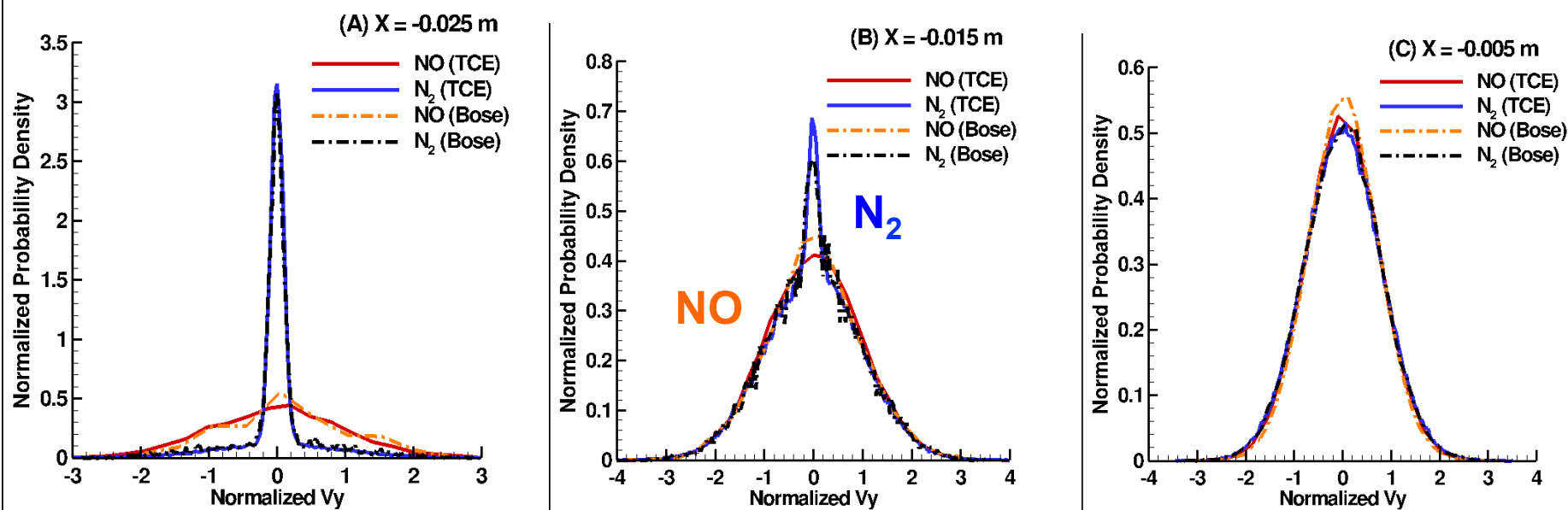
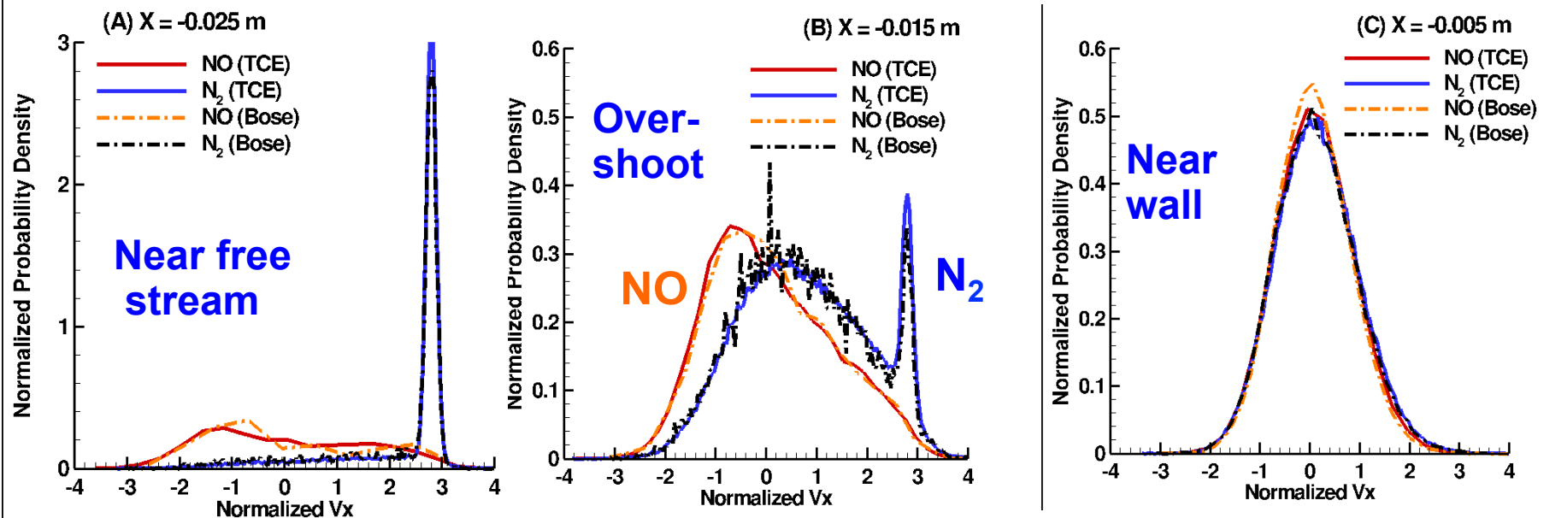
# Velocity Distributions of NO Molecules



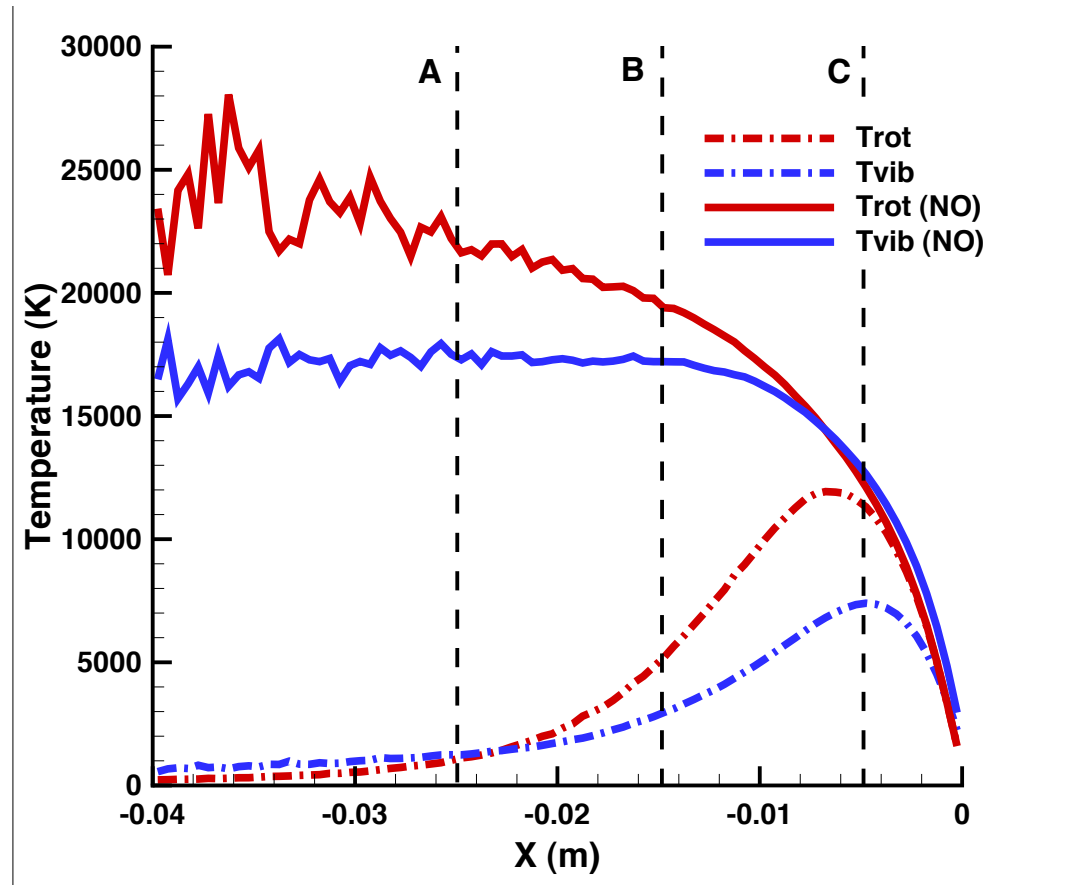
7 km/s, 81 km, TCE  
free stream, 50%  
 $N_2$  and 50%  $O_2$ ,  
 $Kn=0.03$ ,  
 $N_2+O \rightarrow NO^*+N$   
 $NO^*+M \rightarrow NO+M$



# Comparison of Velocity Distributions of NO vs N<sub>2</sub>



# Comparison of Bulk vs NO Internal Temperatures along Stagnation Streamline

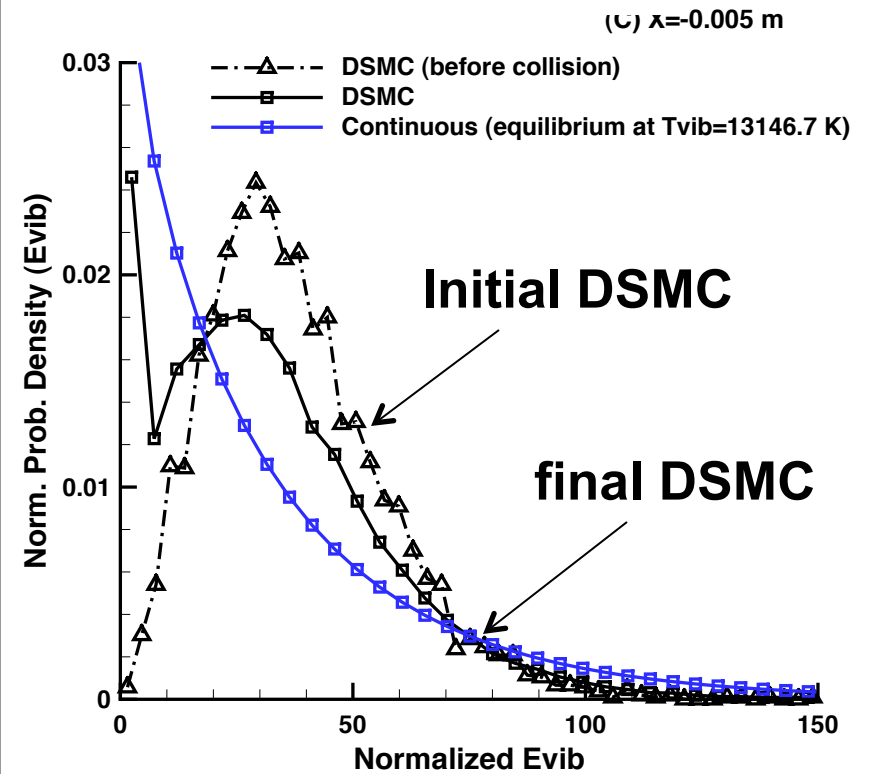
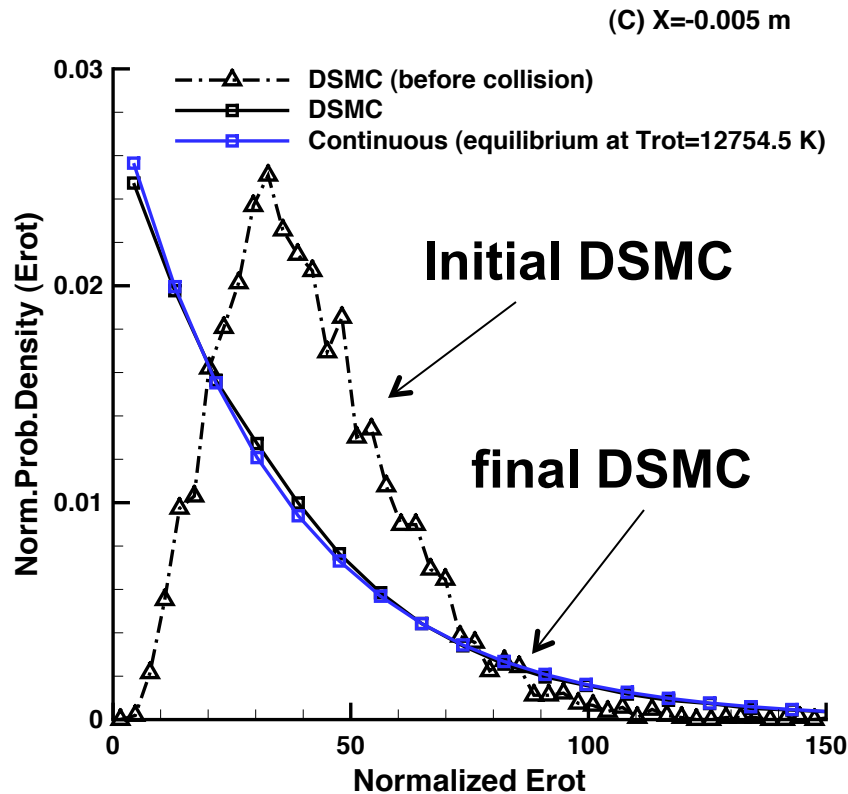




# Near-wall Nascent and Final NO Rotational and Vibrational Energy Distributions in a Shock

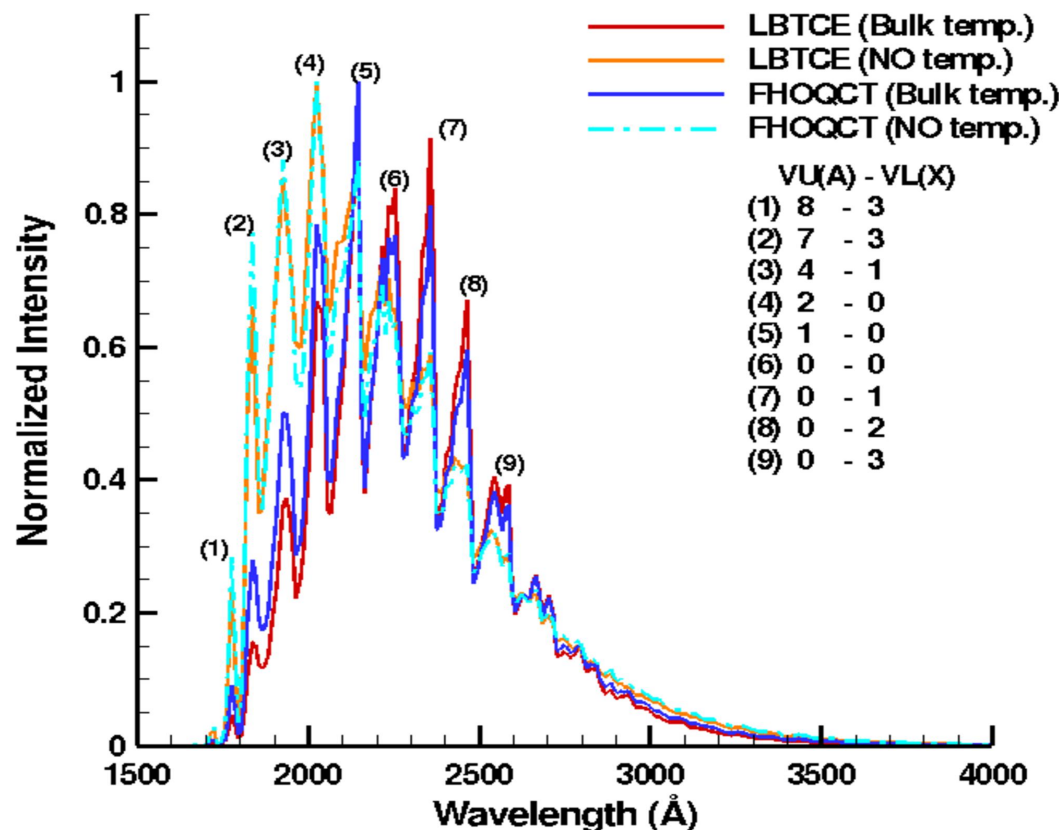
## Rotational

## Vibrational



- Nascent rotational and vibrational distributions are similar,
- Since  $T - T_{rot} \gg T - T_{vib}$ , vibrational distribution never equilibrates,
- Consistent with usual temperature profiles across shock.

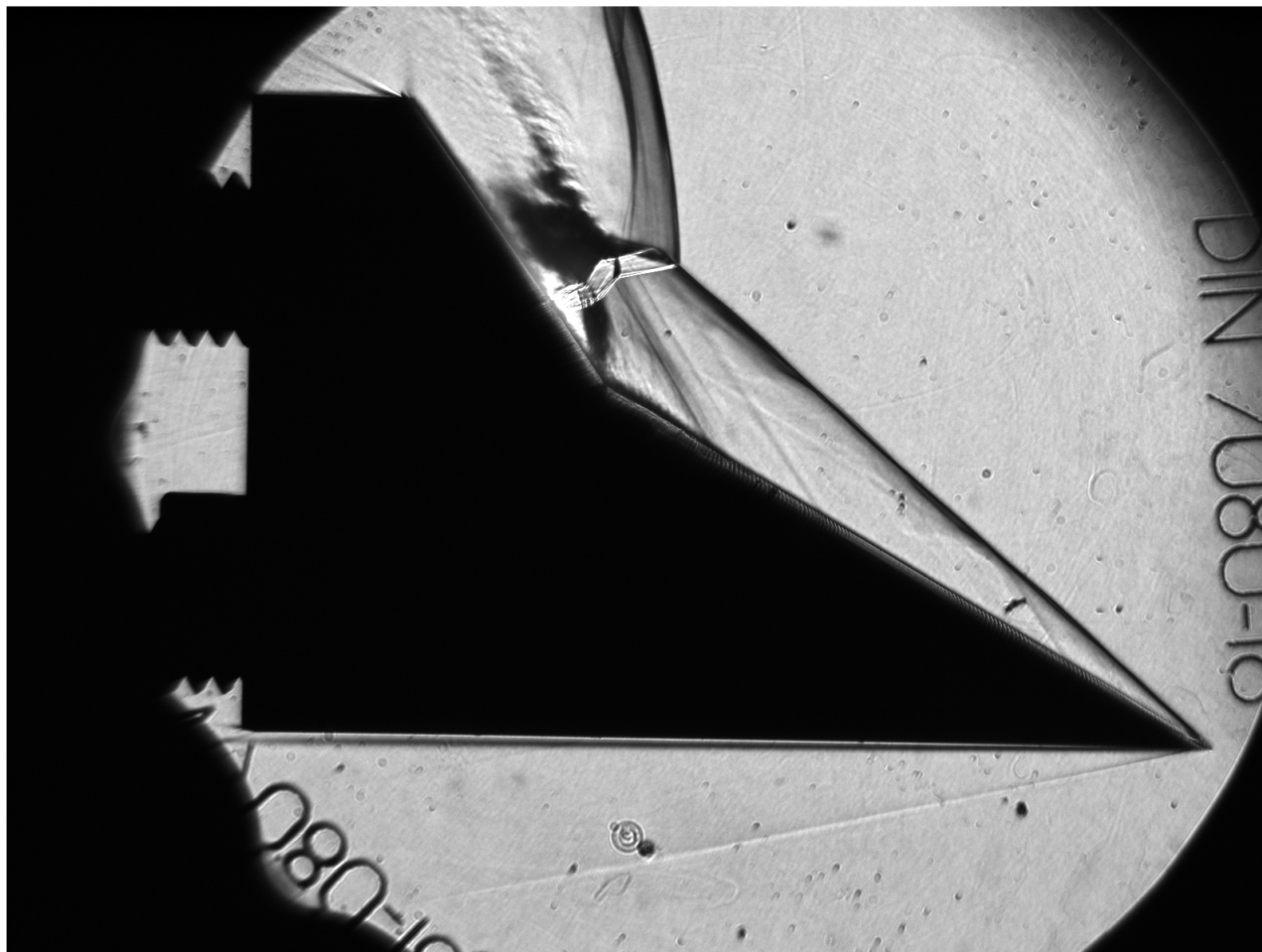
## Effect of T-V Relaxation Rates, Chemistry Models, and Temperatures on NO Vibronic Spectra



- Use of NO vs bulk temperatures most important in determining spectral shape.
- Measured spectra necessary to validate nonequilibrium thermochemical models.

# Gas Dynamic Modeling

**Hypervelocity Expansion Tube (HET) at the  
University of Illinois- Prof. Joanna Austin**





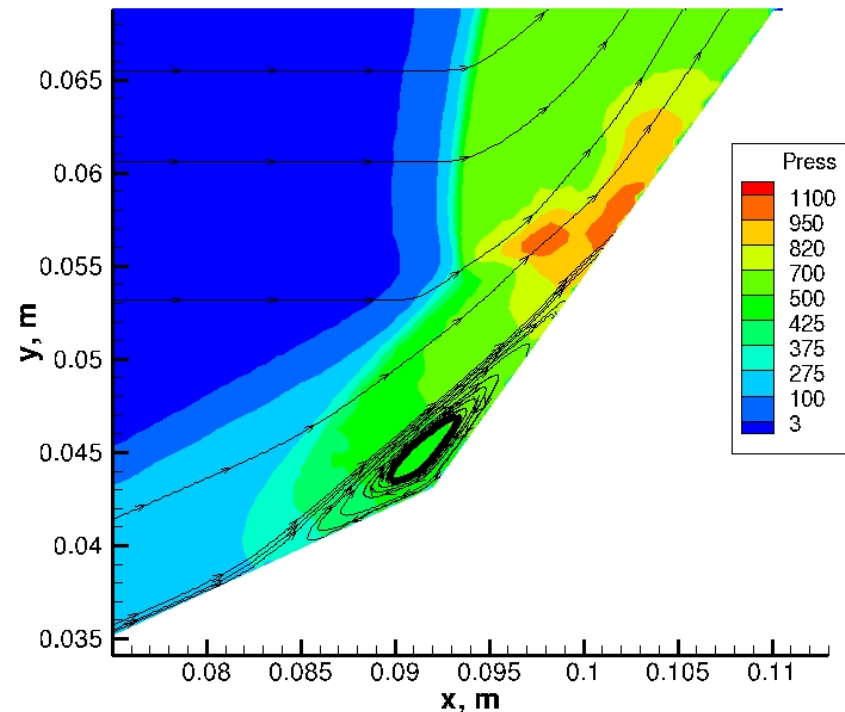
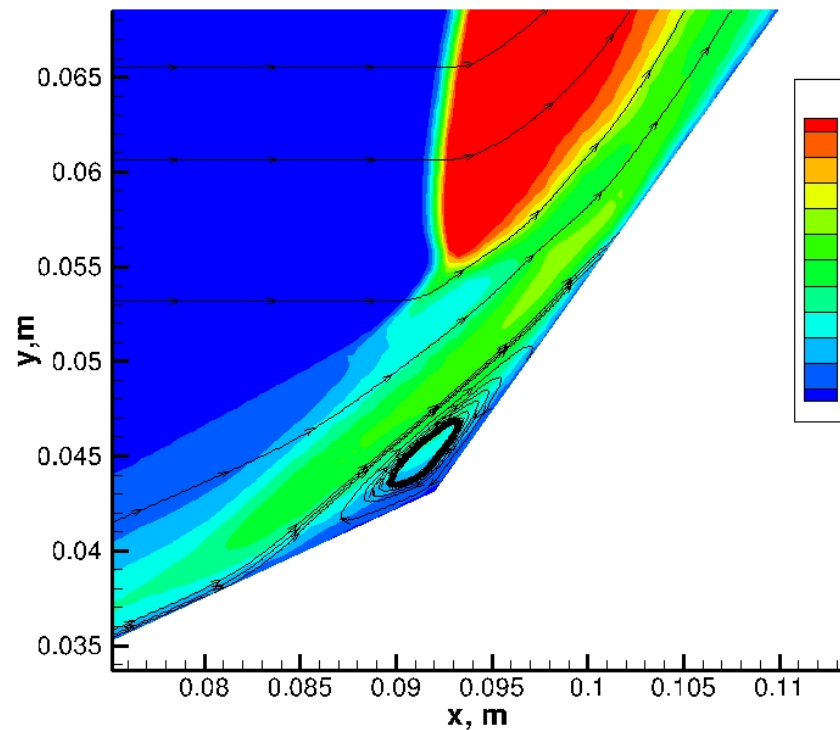
# (1) Double Cone Studies of Moss and Bird\*

Experimental conditions performed for Mach 15.6 nitrogen flow about a 25-/55-deg bi-conic model

Freestream Parameters :	
Temperature, $K$	42.6
Number Density, $m^3$	$3.779 \times 10^{21}$
Speed, $m/s$	2073
Density, $kg/m^3$	$1.757 \times 10^{-4}$
Pressure, $Pa$	2.23
Mach number	15.6
Reynolds number	$1.37467 \times 10^5$
Knudsen number	$1.7 \times 10^{-4}$

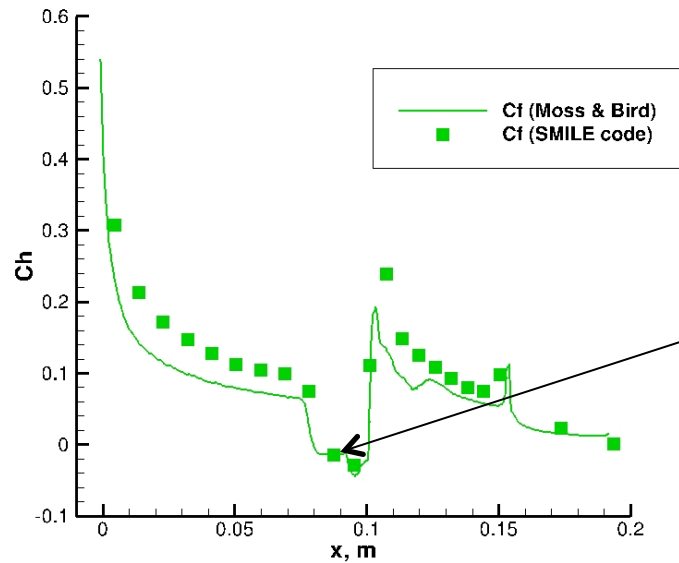
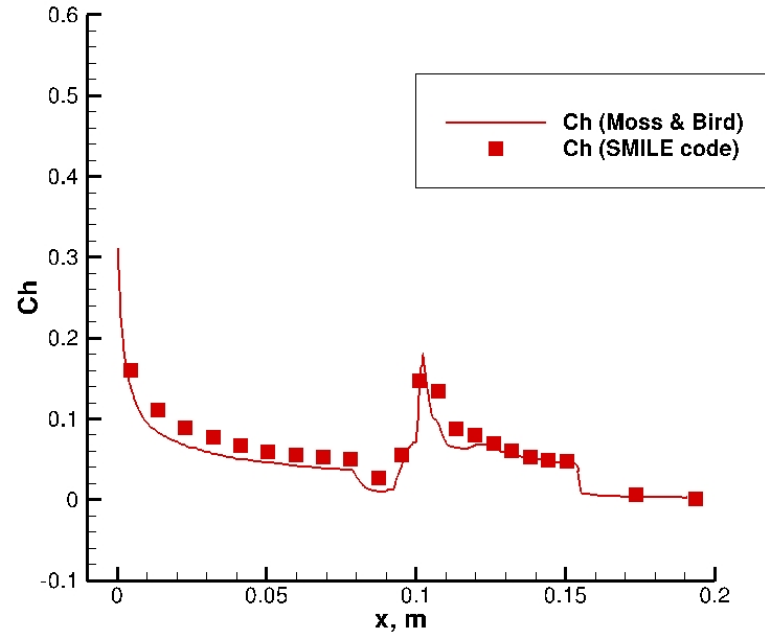
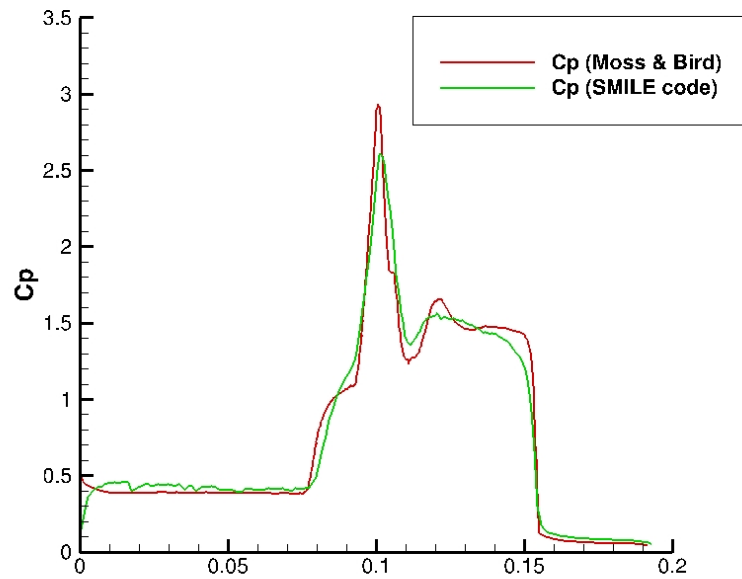
**\*Moss, J. N. and Bird, G. A., "Direct Simulation Monte Carlo of Hypersonic Flows with Shock Interactions," *AIAA Journal*, Vol. 43, No. 12, 2005, pp. 2565-2573.**

## Double Cone Temperature and Pressure Contours



- Physics is dominated by presence of separation zone and
- Sharp leading edge.

# Comparison of Surface Profiles – Double Cone Configuration



- Separation zone well modeled.



## **(2) HET Mach 7 Nitrogen Flows**

- **Computational study of the complex shock interactions resulting from the hypersonic flow about a double wedge configuration presented in the paper AIAA 2012-0284 by A.B. Swantek and J. M. Austin.**
- **Stagnation enthalpies from 2-8 MJ/kg, about a 30-/55-deg double wedge model.**
- **Computations are carried using two-dimensional/axisymmetric Direct Simulation Monte Carlo simulations.**



## Summary of 2 HET Freestream Conditions

Freestream Parameters	M 7_8 (High Enthalpy)	M 7_2 (Low Enthalpy)
Mach number	7.14	7.11
Static Temperature, K	710	191
Static Pressure, kPA	0.78	0.39
Velocity, m/s	3812	1972
Density, kg/m <sup>3</sup>	0.0037	0.0069
Number Density, /m <sup>3</sup>	$7.96 \times 10^{22}$	$1.48 \times 10^{23}$
Stagnation Enthalpy, MJ/kg	8.0	2.1
Unit Reynolds number, /m	$0.4156 \times 10^6$	$1.0653 \times 10^6$
Knudsen number	$4.0256 \times 10^{-4}$	$1.5742 \times 10^{-4}$



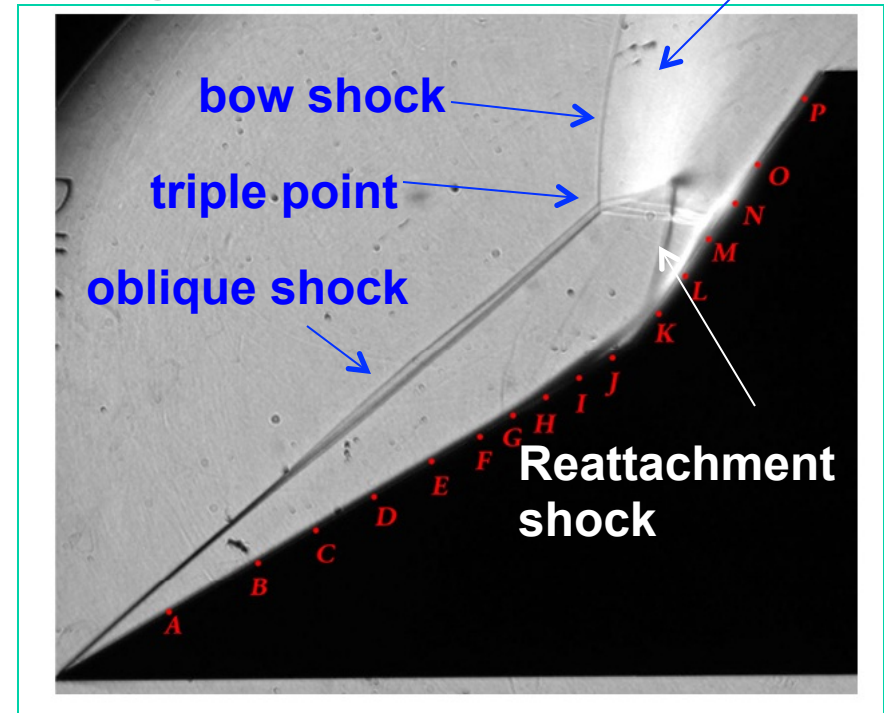
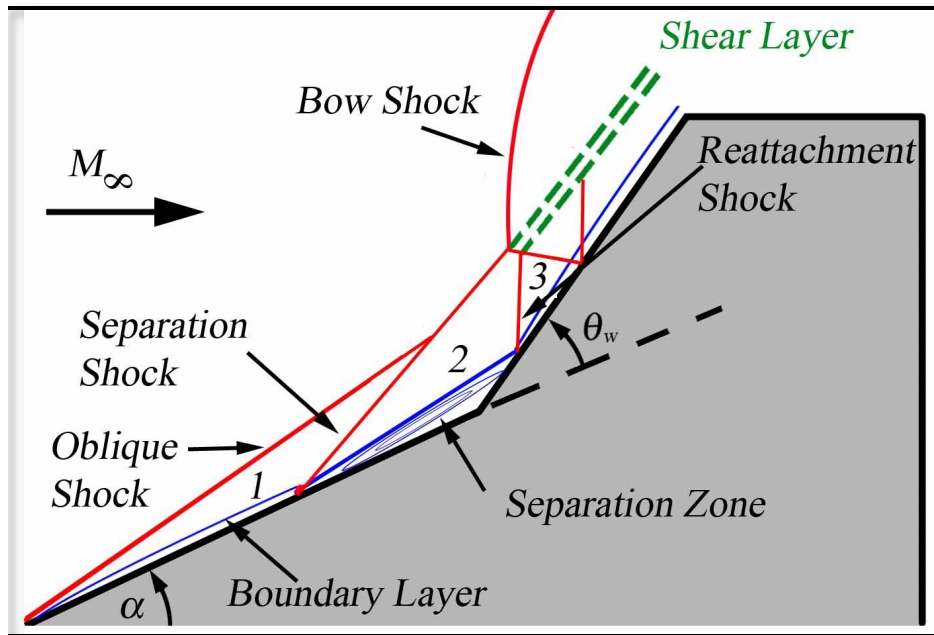


# Summary of Numerical Parameters Used in the DSMC Calculations

	Case	Number of Processors used	Time Step (s)	PFnum	Number of Collisional Cells
High Enthalpy	1	32	$2.0 \times 10^{-7}$	$1.0 \times 10^{14}$	450x350
	2	32	$2.0 \times 10^{-8}$	$3.0 \times 10^{13}$	1800x1600
	3	32	$1.0 \times 10^{-9}$	$3.0 \times 10^{13}$	1800x1600
Low Enthalpy	1	32	$1.0 \times 10^{-9}$	$3.0 \times 10^{13}$	1800x1600
	2	32	$1.0 \times 10^{-9}$	$1.0 \times 10^{13}$	3600x3200

**The computational domain from -20 to 70 mm along the x direction and from 0 to 80 mm in the y direction.**

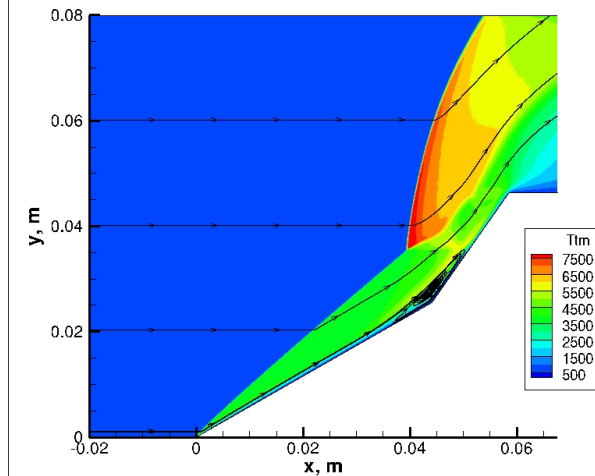
# Strong Shock Interactions – High Enthalpy Case



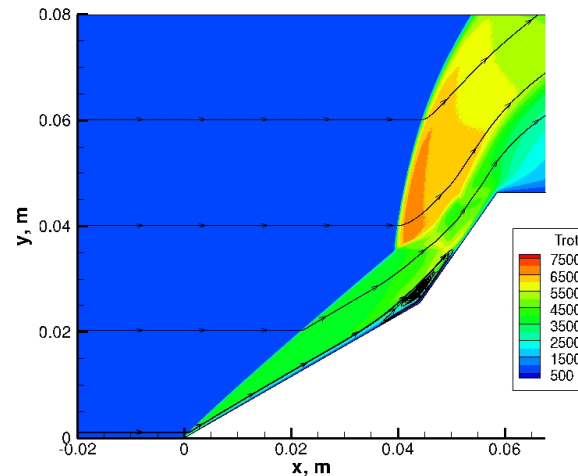
- separation and reattachment shocks
- triple point
- shear layers
- boundary layer interactions
- attached shock from the first cone/wedge interacts with the detached bow shock from the second cone/wedge.

## High Enthalpy Case 3 – DSMC Temperatures

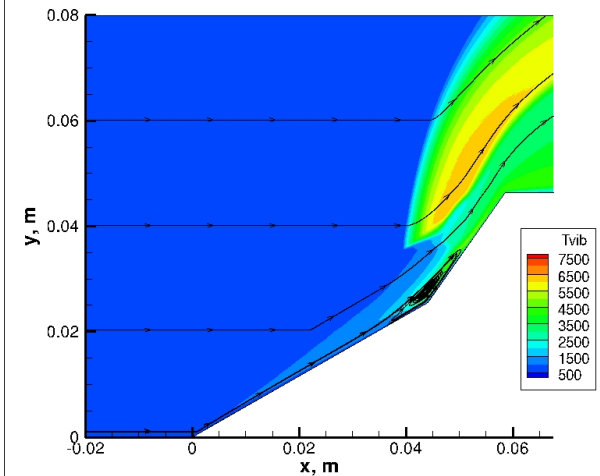
Translational  
Temperature



Rotational  
Temperature

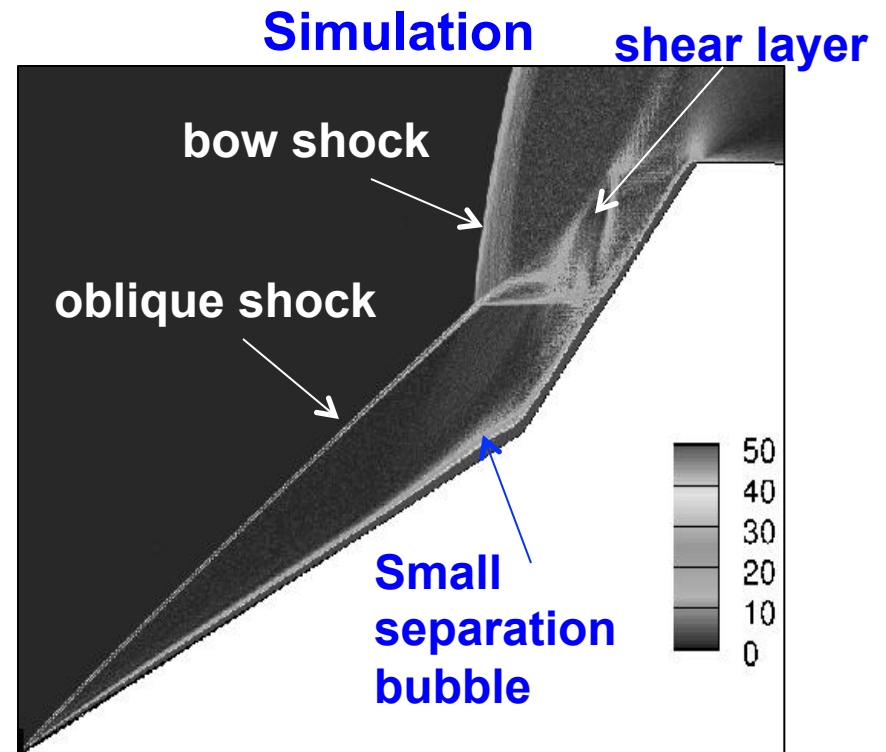
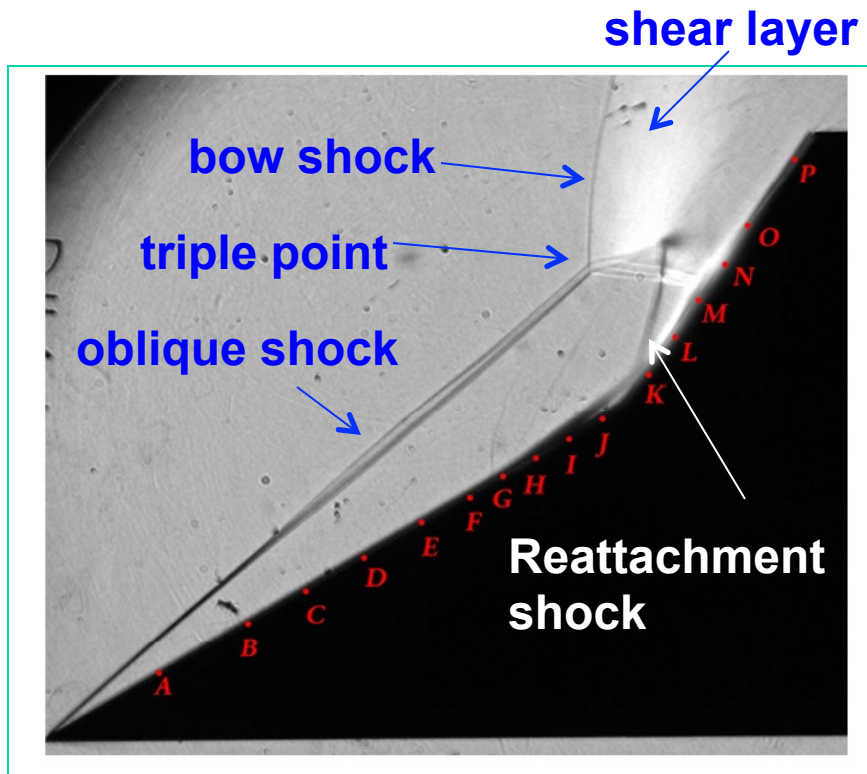


Vibrational  
Temperature



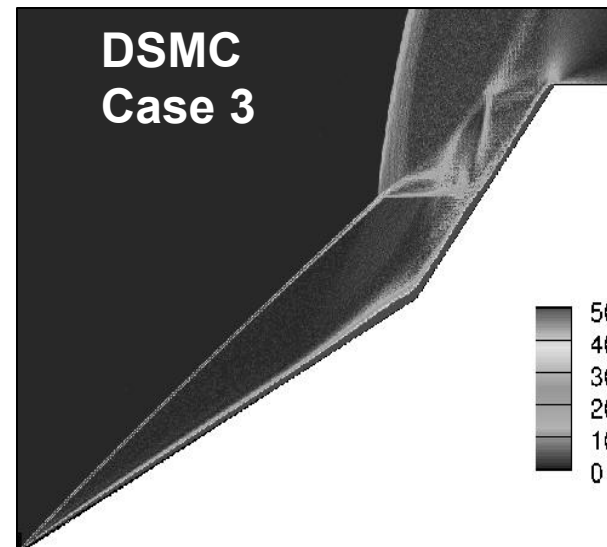
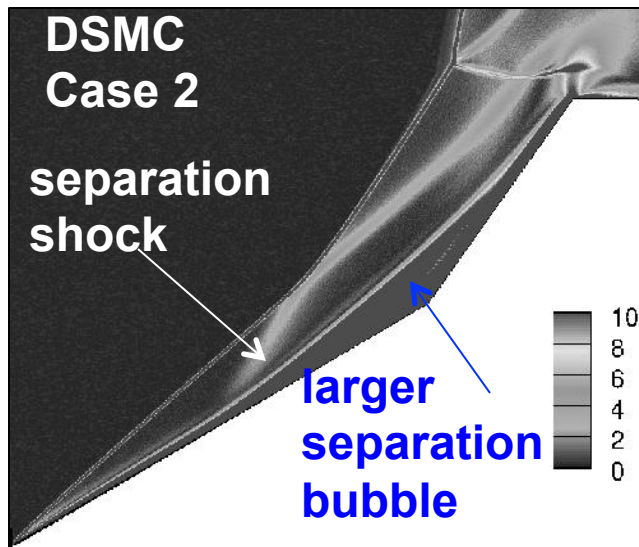
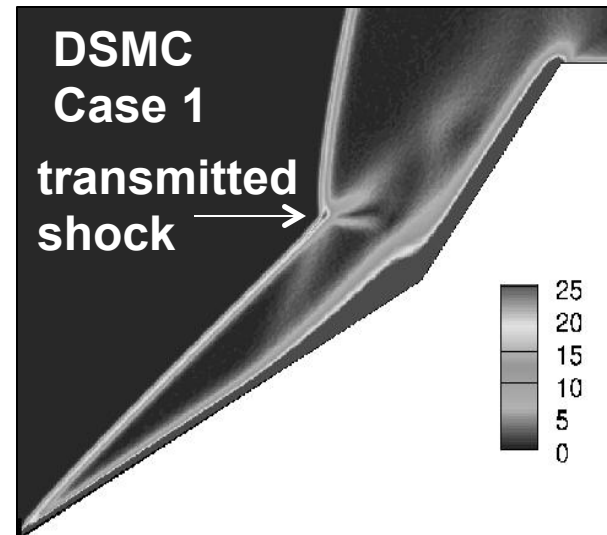
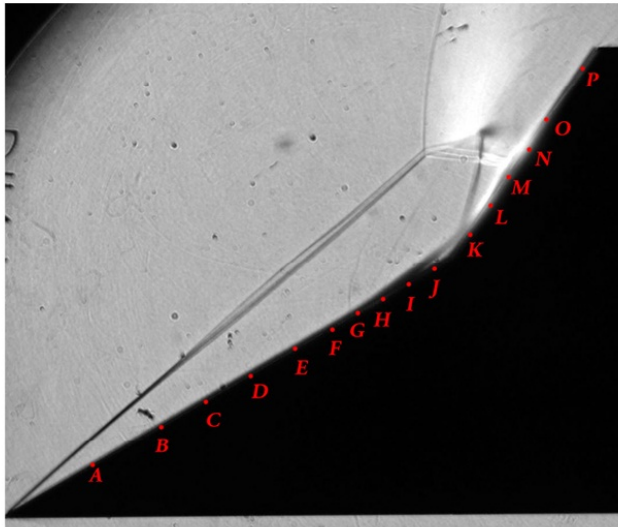
- Characteristic separation bubble seen,
- $T \sim T_{rot}$ ,  $T_{vib}$  out of equilibrium even for continuum-like flow,
- Need to assess separation bubble structure on T-V relaxation models.

# Comparison of Shock Structure - High Enthalpy Case

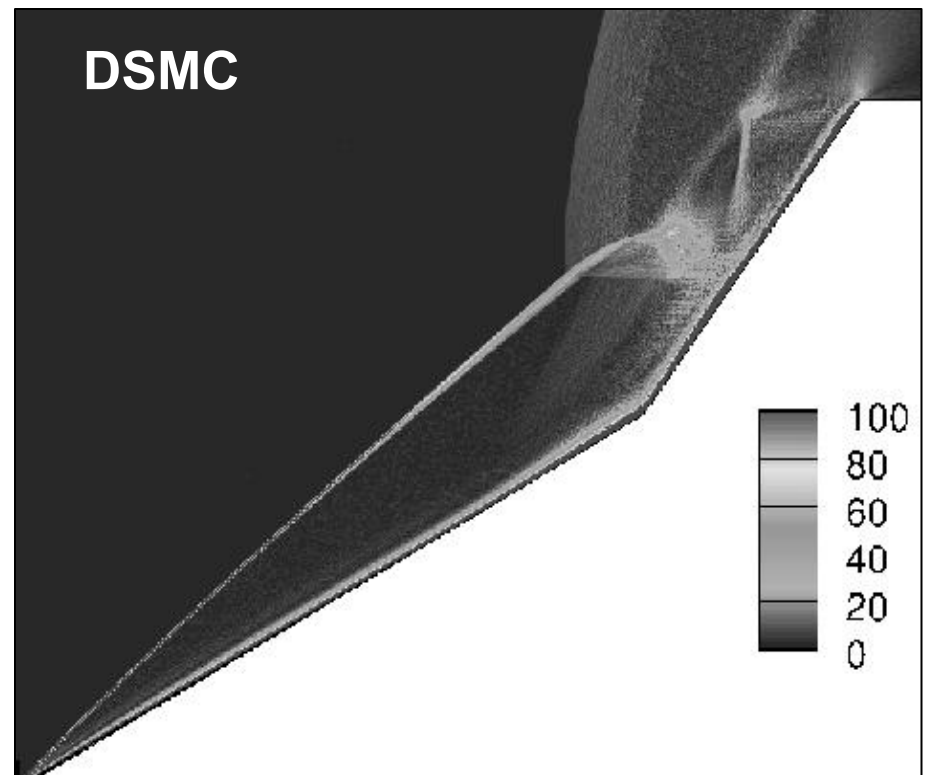
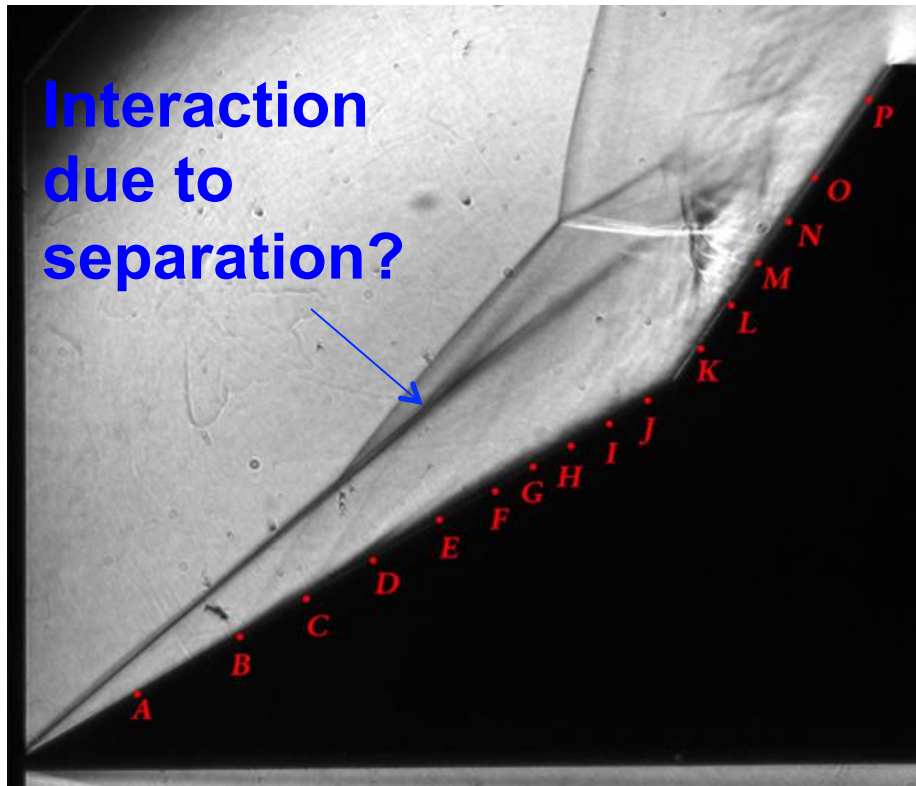


- Reasonable, but, not perfect structure agreement.
- Affect of razor-sharp leading edge on downstream structure?

# Shock Structure Dependence on Numerical Parameters – High Enthalpy Case



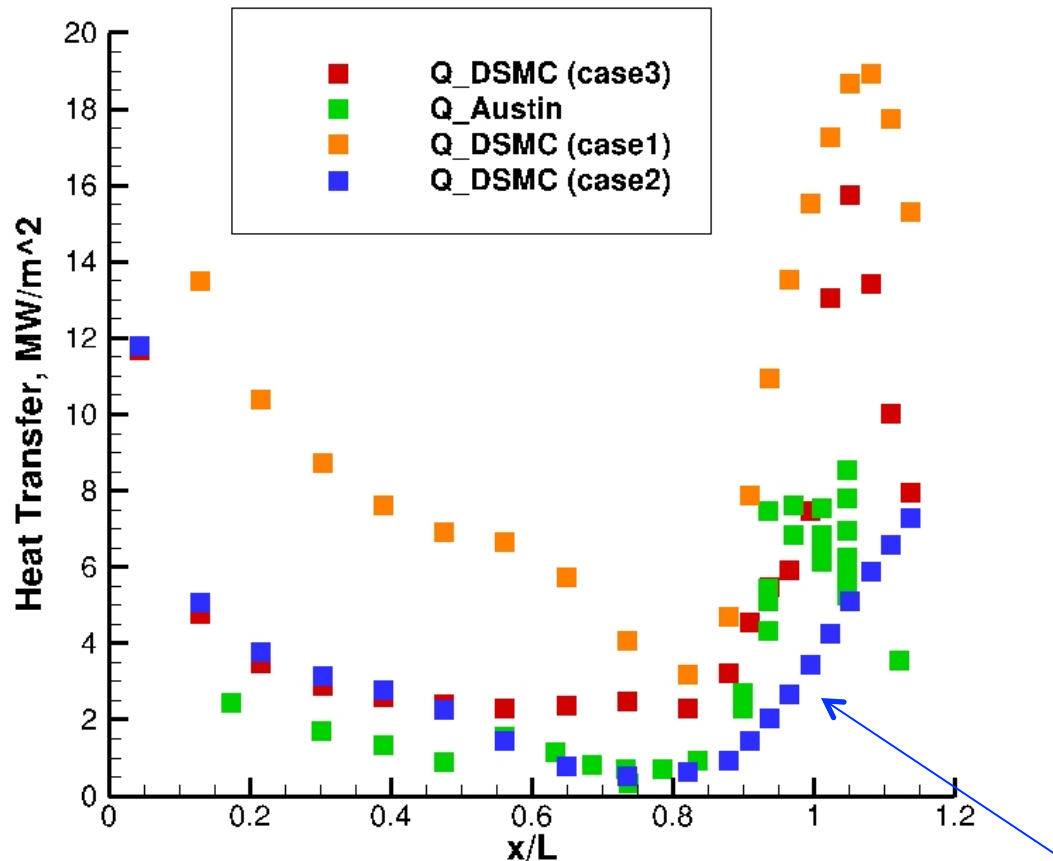
## Comparison of Shock Structure - Low Enthalpy Case



- Different flow features such as the oblique-bow shock interaction, separation shock, separation region, and triple point.
- The experiment seems to have a larger separation region resulting in different flow features.
- Not as confident yet in convergence of numerical parameters.



# Comparison of Heat Transfer – High Enthalpy Case



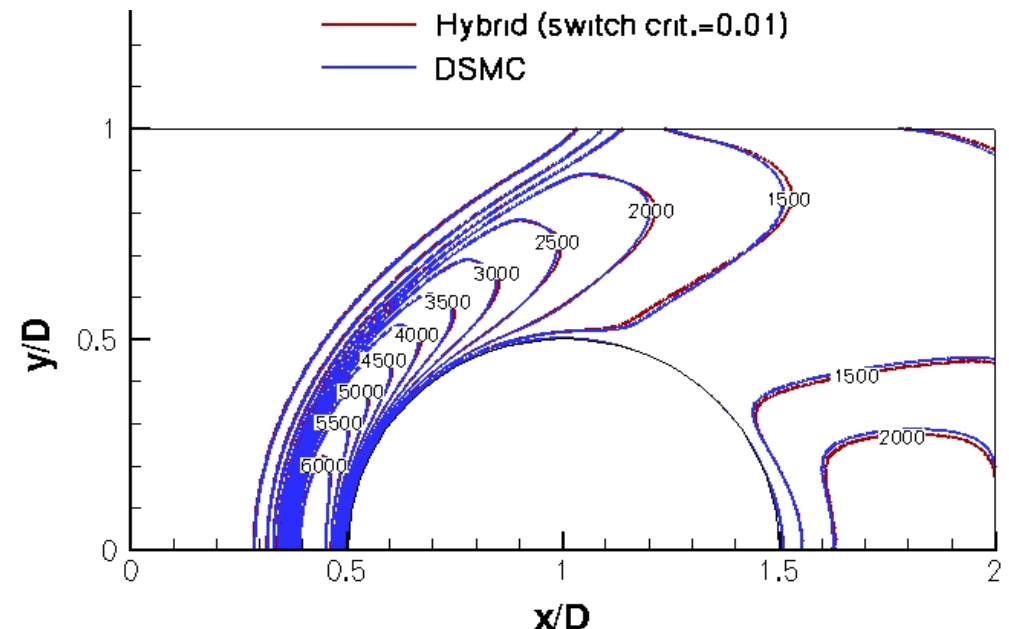
- **DSMC Case 2** seems to capture similar trends, ie., jump at the hing ( $x/L = 0.8$ ).
- But DSMC Case 2 had “wrong” shock structure.
- Separation bubble too large.

# Outstanding Scientific Issues

- Nonequilibrium thermochemical models still are incomplete and unvalidated (in both particle and continuum approaches). Need more data and less code-to-code comparisons.
- Need to characterize and quantify facilities for non-equilibrium gas dynamic calculations.

- **Particle-particle hybrid schemes:**

- What is our criteria for detecting equilibrium break down?
- Will the ES-BGK approach be sufficiently general to include internal energy?
- Can we apply it to shock-shock interactions?
- Can we handle unsteady flows?







## ***Acknowledgments***

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