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# Direct Molecular Simulation of Nonequilibrium Flows

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Thomas E. Schwartzentruer

**Aerospace Engineering and Mechanics**  
**University of Minnesota**

AFOSR Young Investigator Program  
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# Direct Molecular Simulation

- Nearing the point where we can directly simulate high-speed (thermochemical) nonequilibrium flows with quantum mechanics

Flows consist of many collisions, each involving 2-6 atoms

Collisions are modeled with quantum mechanics by Physicists and Chemists

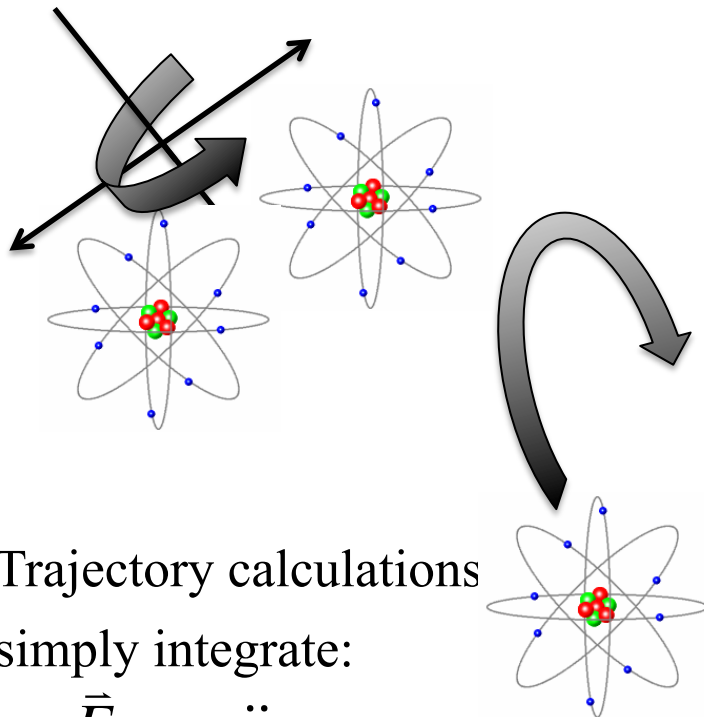


- Large-scale computing and the nature of dilute gases will enable the direct simulation of practical flows

# Current Use of Computational Chemistry

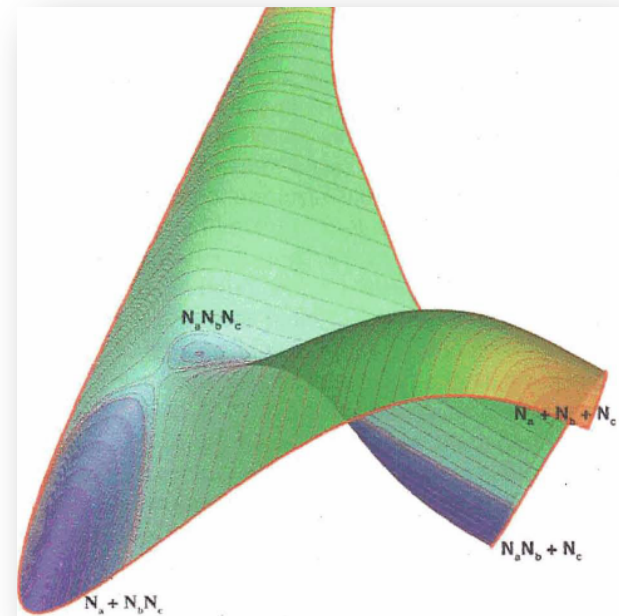


1. Quantum mechanical (QM) energy calculations
2. Fit a potential energy surface (PES)



Trajectory calculations  
simply integrate:

$$\vec{F}_i = m_i \ddot{\vec{r}}_i$$



Analytical function that inputs atomic  
positions and returns atomic forces

# Current Use of Computational Chemistry

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1. Quantum mechanical (QM) energy calculations
2. Fit a potential energy surface (PES)

Create cross-section-based thermochemical models...

3. Employ DSMC or CFD to obtain shock-layer flow solution





# Current Use of Computational Chemistry



1. Quantum mechanical (QM) energy calculations
2. Fit a potential energy surface (PES)

- perform millions/billions of trajectories
- compute state-state cross-sections (thousands)
- typically bin cross-sections (separate rotation, vibration, electronic, and possibly group states)
- implement in state-resolved DSMC or in master-equation CFD code (equipartition/detailed balance)
- thermally average cross-sections to form reduced-order rate models for DSMC and CFD

3. Employ DSMC or CFD to obtain shock-layer flow solution



# Direct Molecular Simulation



1. Quantum mechanical (QM) energy calculations
2. Fit a potential energy surface (PES)

2.1 Pure Molecular Dynamics (all-atom)

2.2 Event-Driven MD (accel. all-atom)

2.3 Trajectory-based DSMC (accel. subset of atoms)

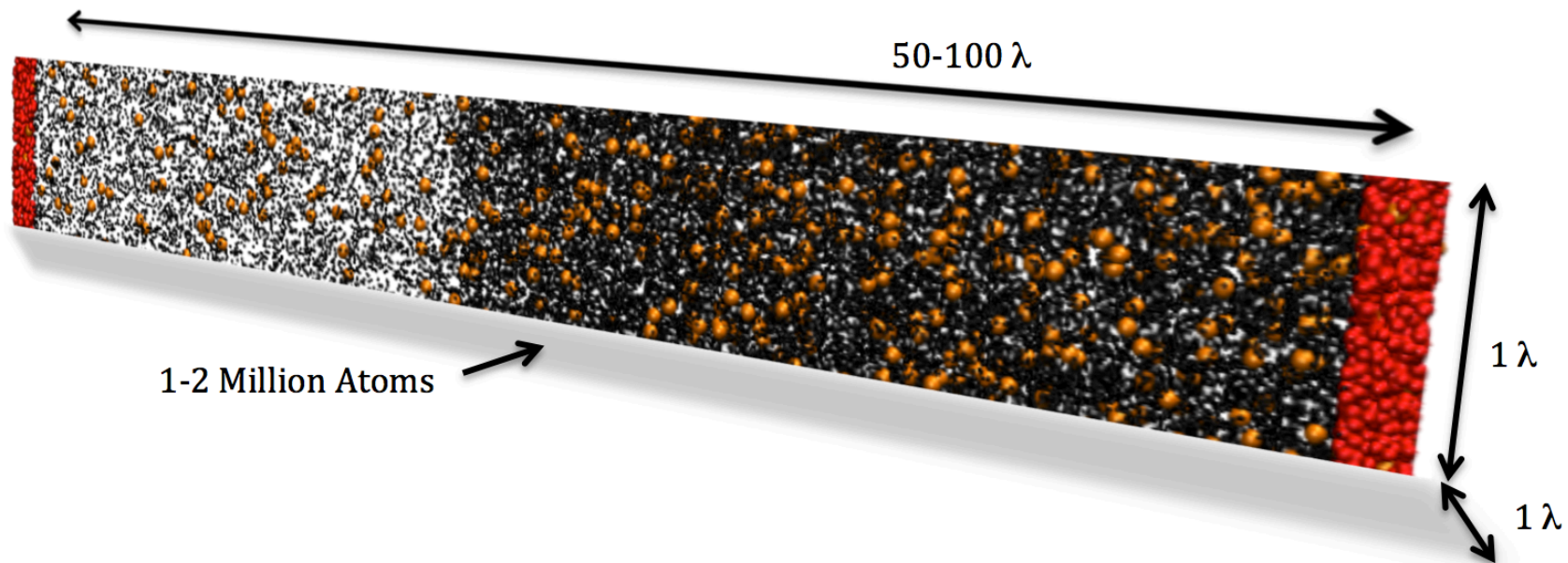
2.4 Direct molecular simulation of shock-layer flow

3. Employ DSMC or CFD to obtain shock-layer flow solution

# All-Atom Molecular Dynamics for Shock Waves



- Pure MD, millions of atoms, millions of timesteps, millions of collisions
- No adjustable parameters, ex. LJ-potential for Argon, Helium, Xenon, and nitrogen (vibrational ground state) are non-negotiable
- Can use freely-available LAMMPS MD code from Sandia



# Pure Argon



Valentini, and Schwartzentruber, "Large-scale Molecular Dynamics Simulations of Normal Shock Waves in Dilute Argon", *Physics of Fluids*, 21, 066101, pp. 1-9, 2009.

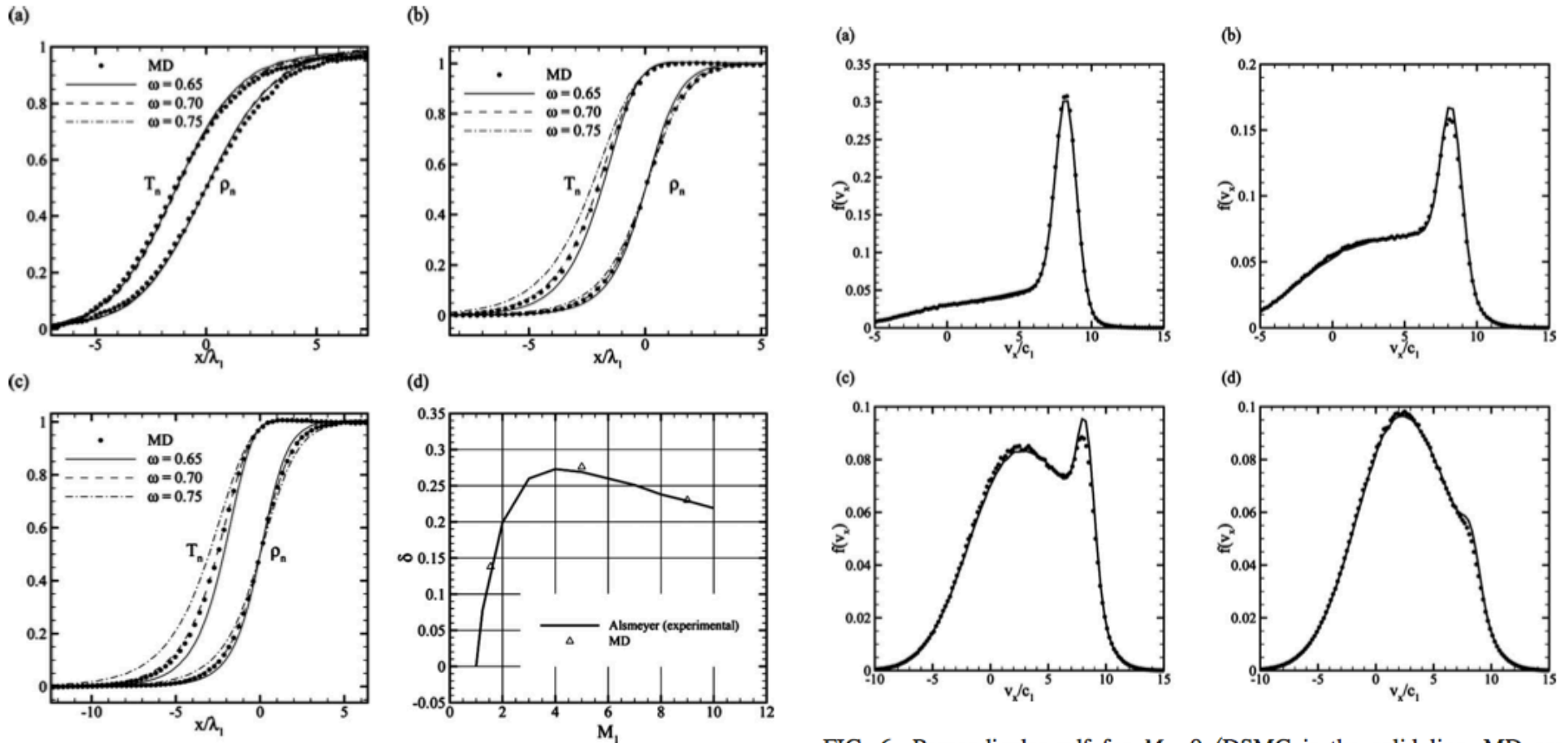


FIG. 3. Comparison between MD and DSMC temperature and density profiles for (a)  $M_1=1.55$ , (b)  $M_1=5$ , (c)  $M_1=9$ ; (d) reciprocal shock thickness.

FIG. 6. Perpendicular vdf for  $M_1=9$  (DSMC is the solid line, MD are circles). (a)  $\rho_n=0.148$  (DSMC) and  $\rho_n=0.144$  (MD), (b)  $\rho_n=0.330$  (DSMC) and  $\rho_n=0.348$  (MD), (c)  $\rho_n=0.540$  (DSMC) and  $\rho_n=0.561$  (MD), and (d)  $\rho_n=0.743$  (DSMC) and  $\rho_n=0.762$  (MD).

# Xenon-Helium and Argon-Helium Mixtures



Valentini, Tump, Zhang, and Schwartzentruber, “Molecular dynamics simulations of shock waves in mixtures of noble gases”, *under review*, ***Journal of Thermophysics and Heat Transfer***, Feb. 2012.

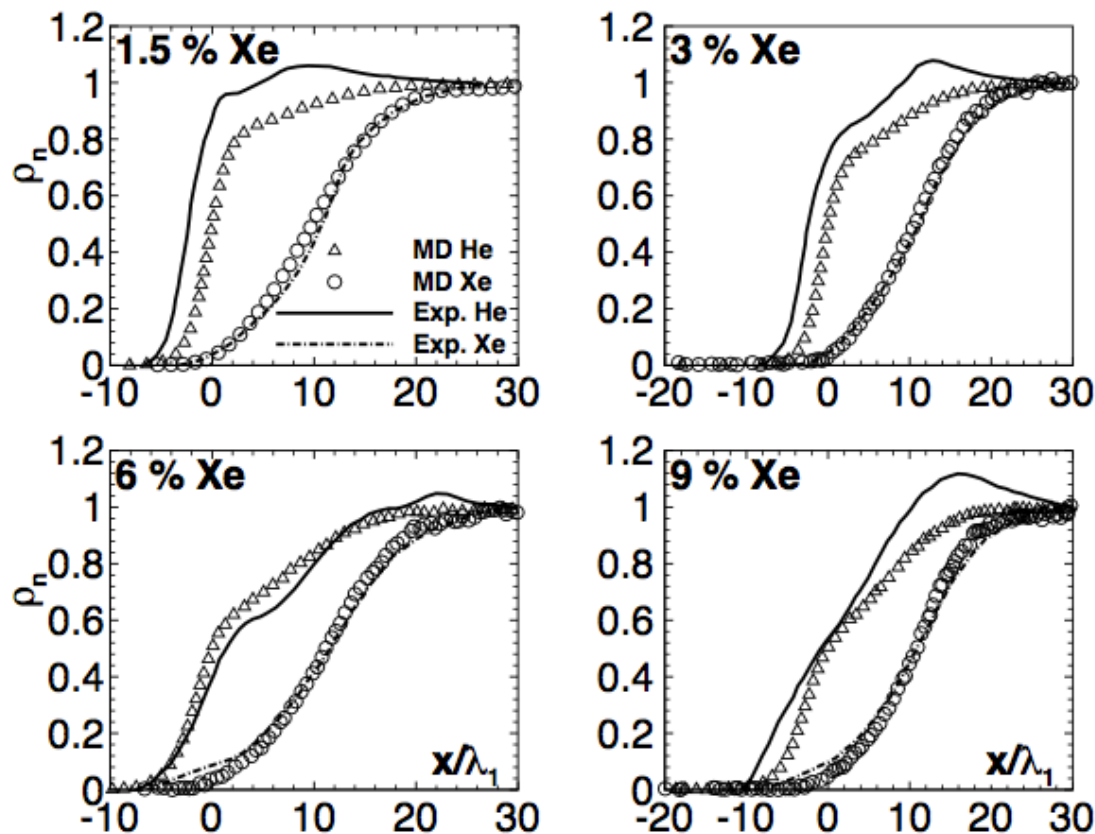
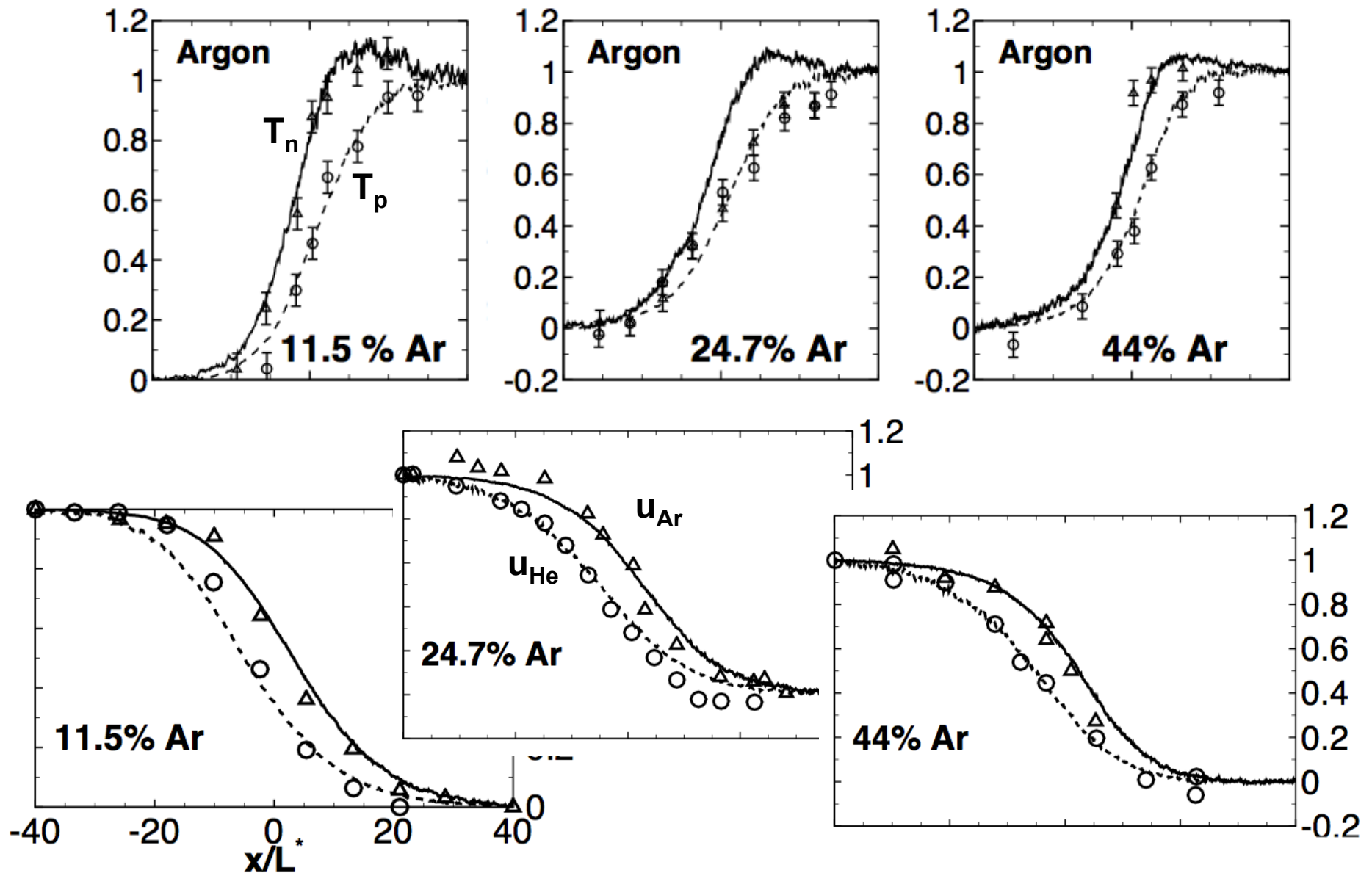


Figure 3: Species normalized density profiles obtained with MD and compared to the experimental measurements of Gmurczyk and co-workers.<sup>19</sup>  $\lambda_1$  values are listed in Tab. 2 for each case.

# Xenon-Helium and Argon-Helium Mixtures

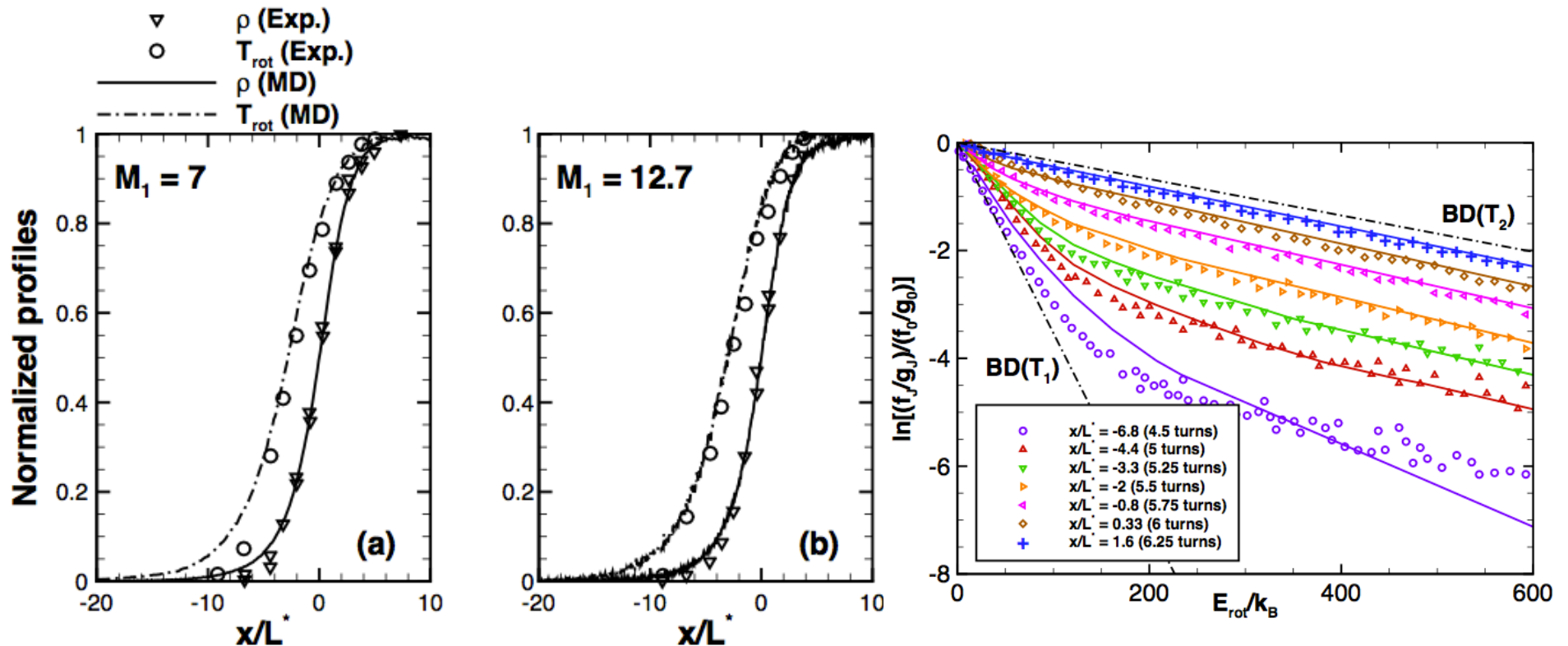




# Diatomic Nitrogen



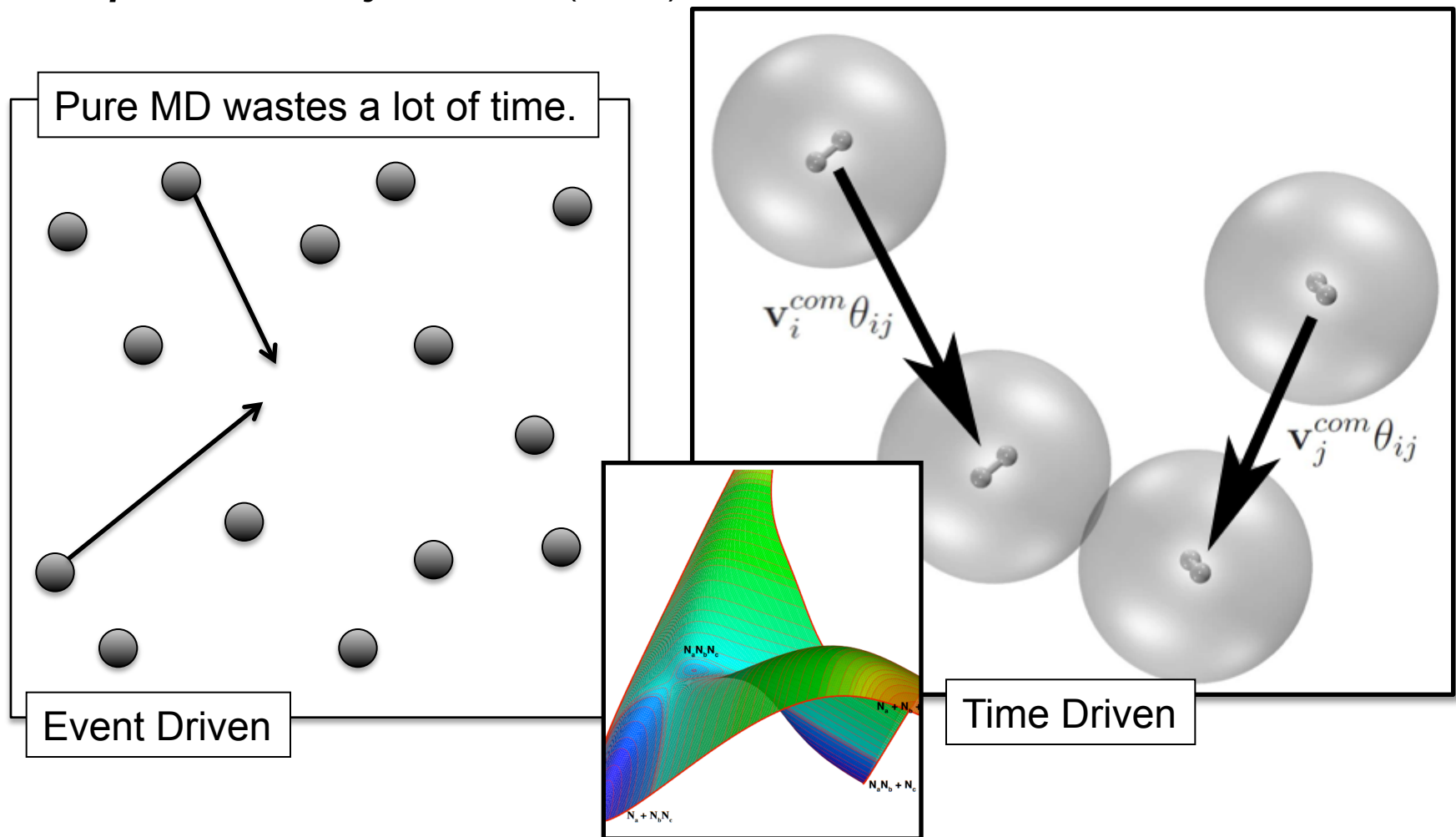
Valentini, Zhang, and Schwartzentruber, “Molecular dynamics simulation of rotational relaxation in nitrogen: implications for rotational collision number models”, *under review, Physics of Fluids*, May, 2012.





# Combined Event-Driven / Time-Driven MD

Valentini and Schwartzentruber “A Combined Event-Driven/Time-Driven Molecular Dynamics Algorithm for the Simulation of Shock Waves in Rarefied Gases”, *Journal of Computational Physics*, 228 (2009) 8766-8778.







# Combined Event-Driven / Time-Driven MD

Valentini and Schwartzentruber “A Combined Event-Driven/Time-Driven Molecular Dynamics Algorithm for the Simulation of Shock Waves in Rarefied Gases”, ***Journal of Computational Physics***, 228 (2009) 8766-8778.

- ED/TD MD algorithm detects and advances simulation to impending interactions, while accurately integrating each interaction using conventional Time-Driven (TD) MD.
- Multi-body interactions are also detected and simulated.
- Recently extended to polyatomic molecules including chemical reactions
- For example, the time of an impending collision is:

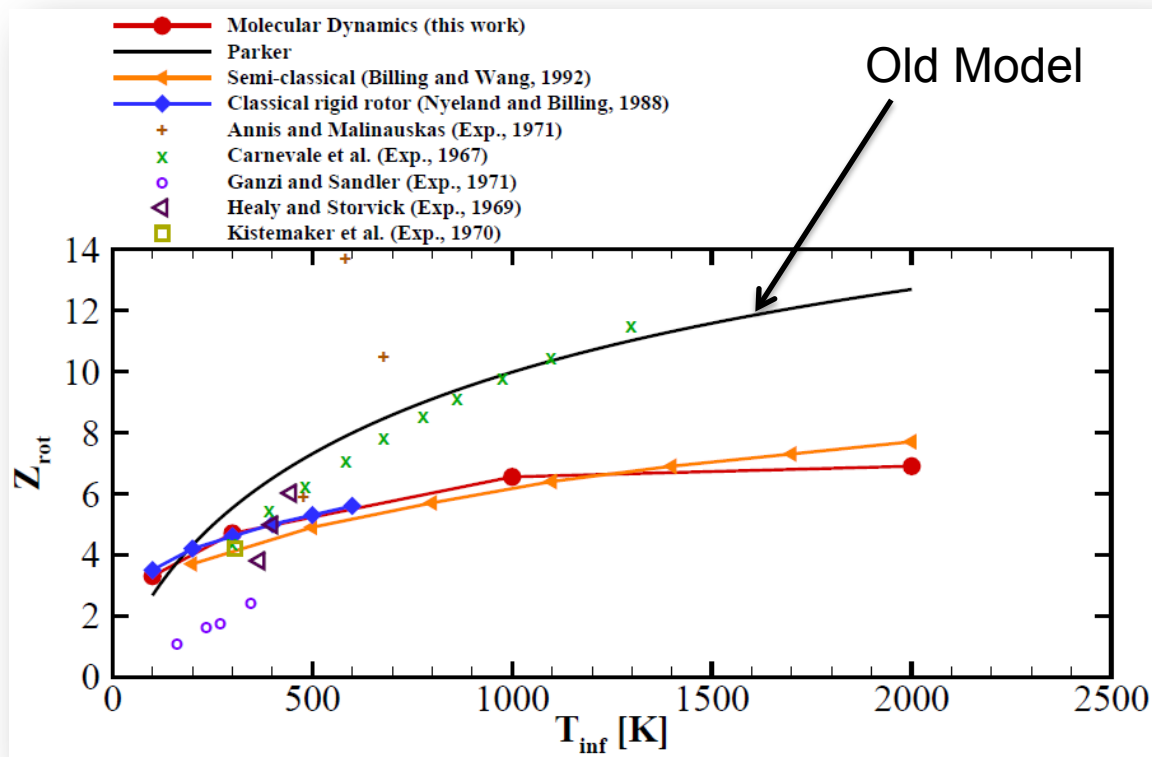
$$\theta_{ij} = \frac{(-\mathbf{v}_{ij} \cdot \mathbf{r}_{ij}) \pm \sqrt{(\mathbf{v}_{ij} \cdot \mathbf{r}_{ij})^2 - \mathbf{v}_{ij} \cdot \mathbf{v}_{ij}(\mathbf{r}_{ij} \cdot \mathbf{r}_{ij} - r_c^2)}}{(\mathbf{v}_{ij} \cdot \mathbf{v}_{ij})}$$

- Pure MD shocks: ~128 cores for 4 days
- ED/TD MD shocks: 1 core for 10 days (~50x faster - **exactly** the same result)

# A New Rotational Nonequilibrium Model



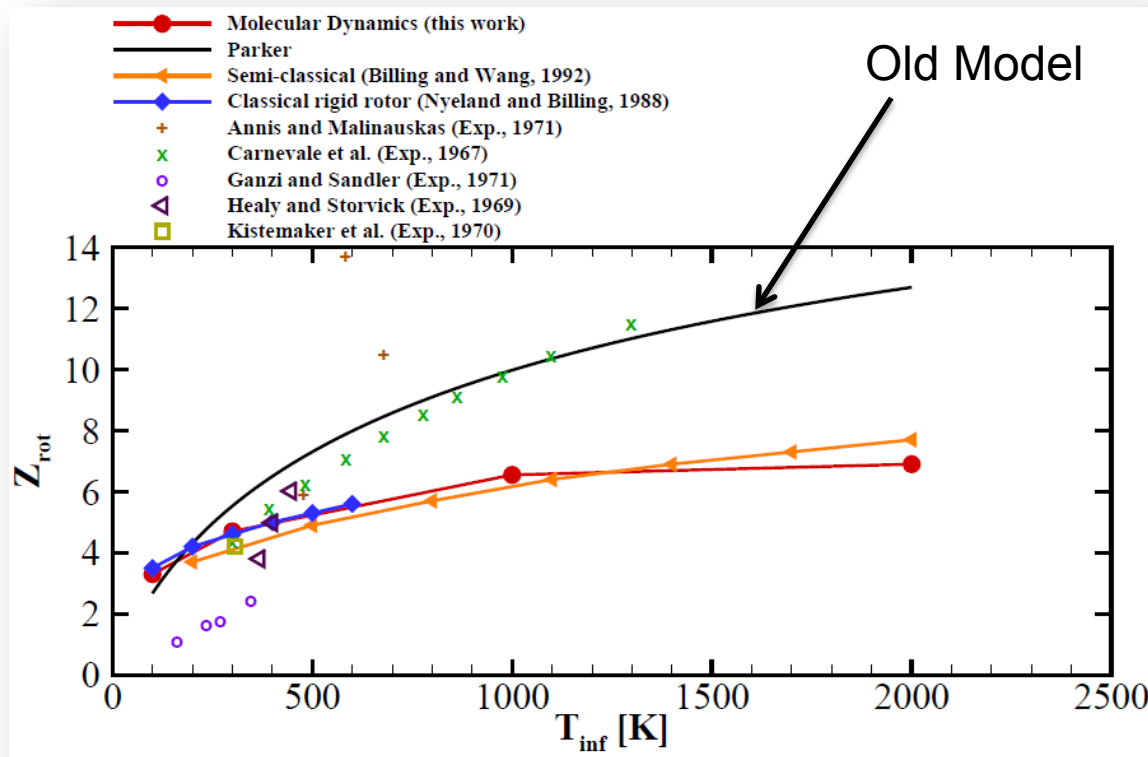
- Current DSMC codes use either  $Z_{\text{rot}}=5=\text{constant}$  or  $Z_{\text{rot}}(T)$  – Parker
- Parker model fit to single experimental data set (experiments vary widely)



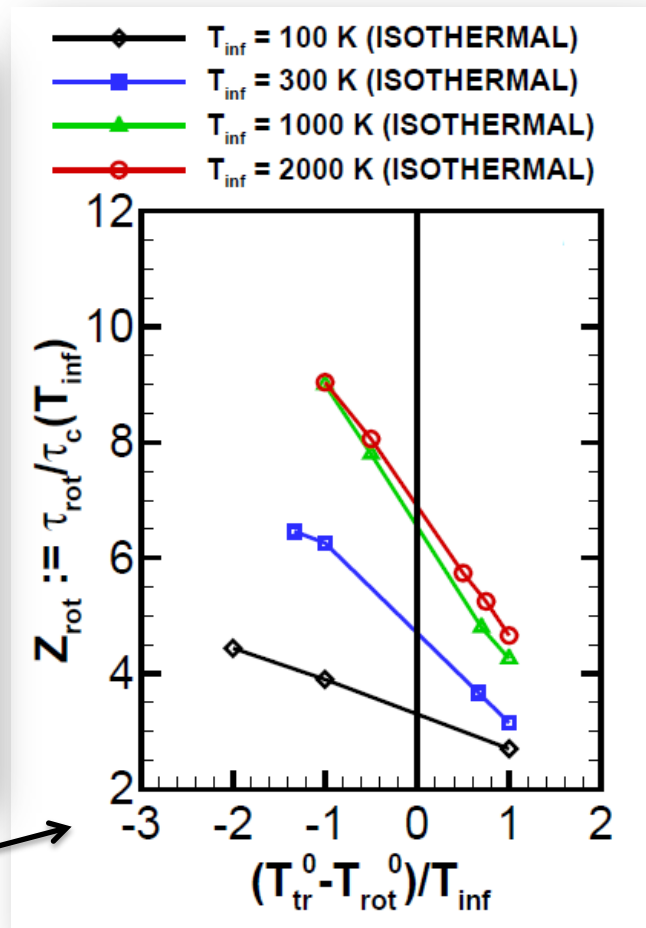
# A New Rotational Nonequilibrium Model



- Our results clearly show that the rotational relaxation rate strongly depends on the *degree* of nonequilibrium and the *direction* to nonequilibrium



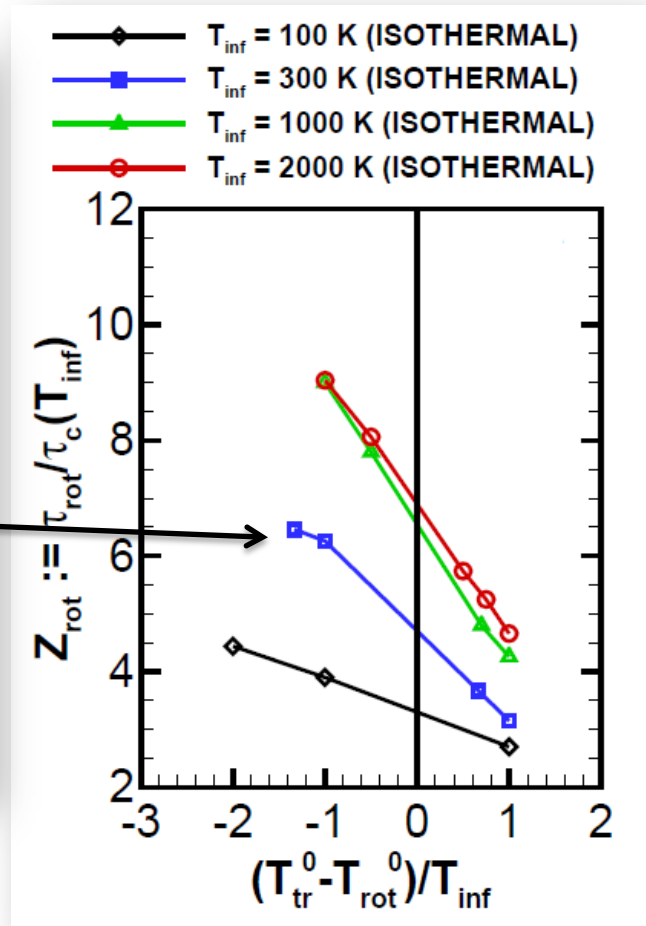
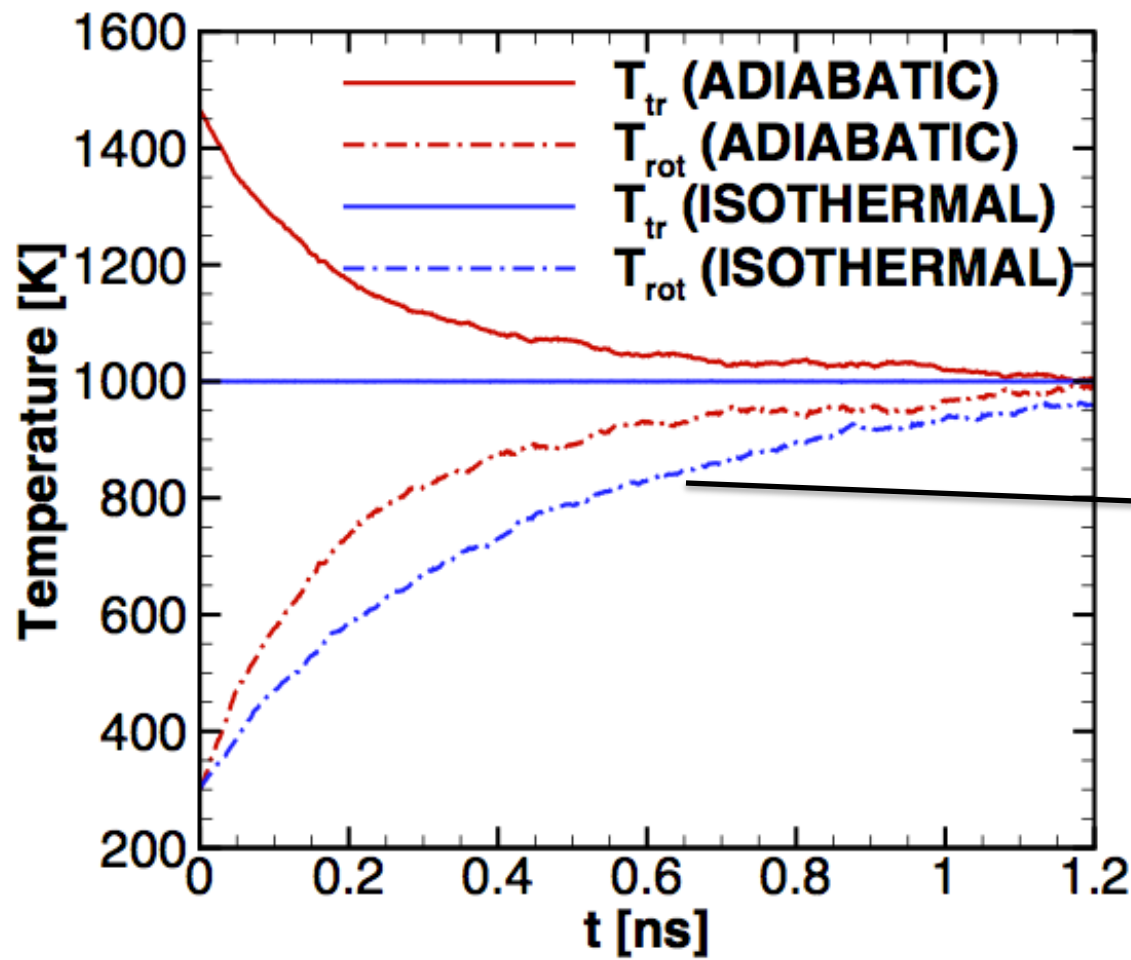
New Model



# A New Rotational Nonequilibrium Model



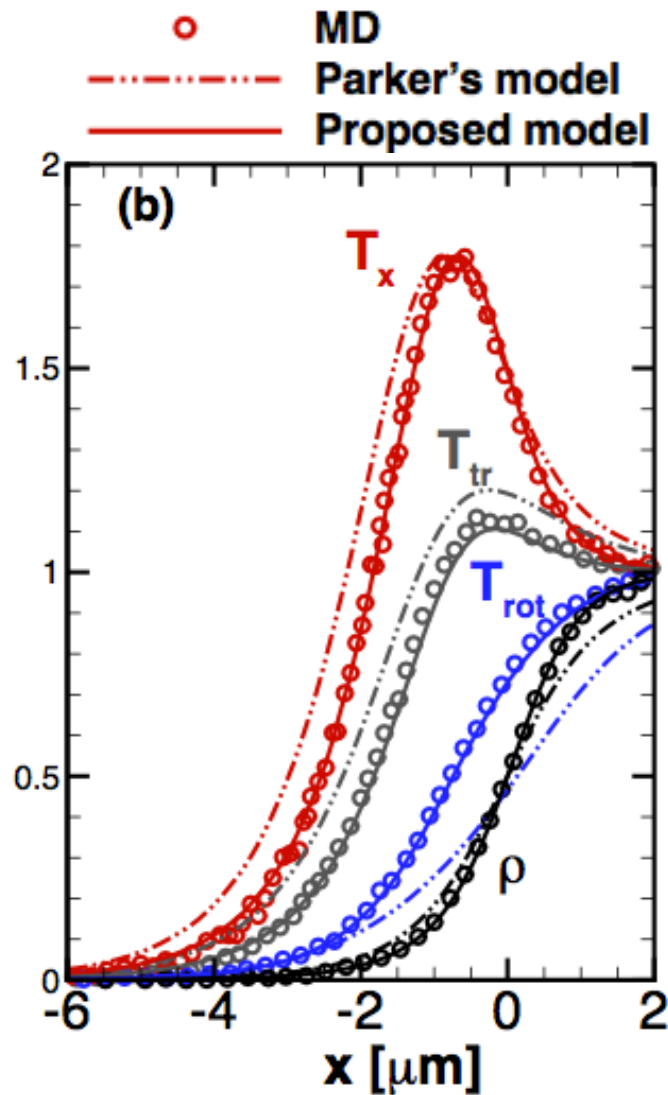
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# New Model Results



Shock:  $T_1=300\text{K}$ ,  $M_1=7$



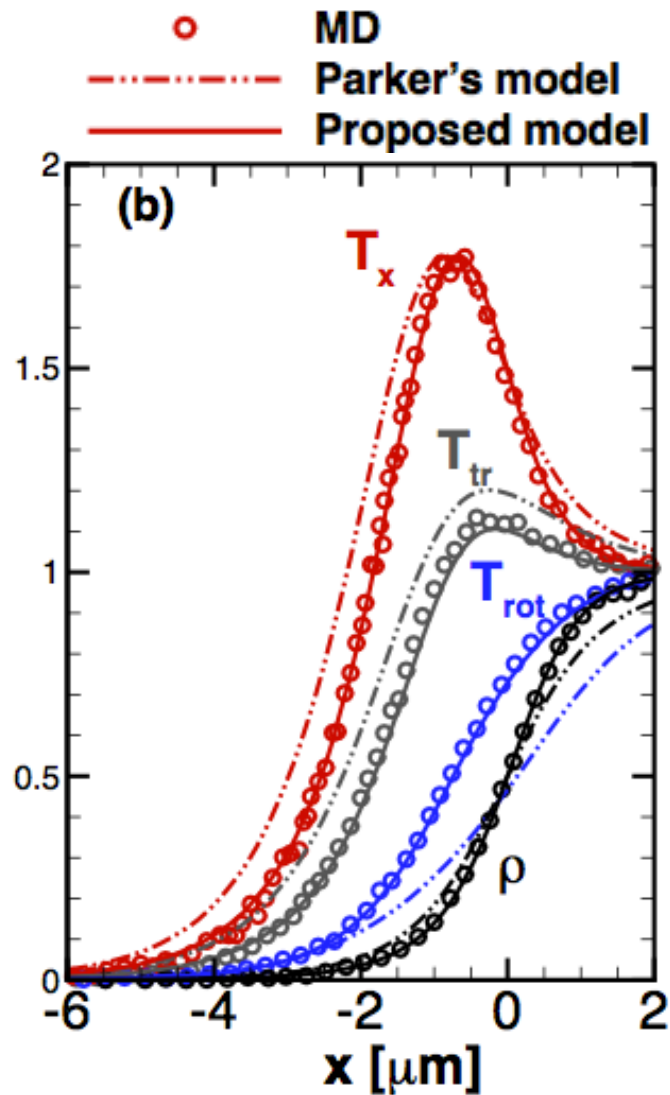
$$Z_{rot}(T_{tr}, T_{rot}) = Z_{rot}^0 \left[ 1 - b_1 \left( 1 - \frac{T_{rot}}{T_{tr}} \right) \right]$$

$$Z_{rot}^0(T_{tr}) = a_1 \left( \frac{T_{tr}}{1 \text{ K}} \right)^{1/4} + \frac{a_2}{\left( \frac{T_{tr}}{1 \text{ K}} \right)^{1/4}} + a_3 \left[ \left( \frac{T_{tr}}{1 \text{ K}} \right) - 1000 \right]$$

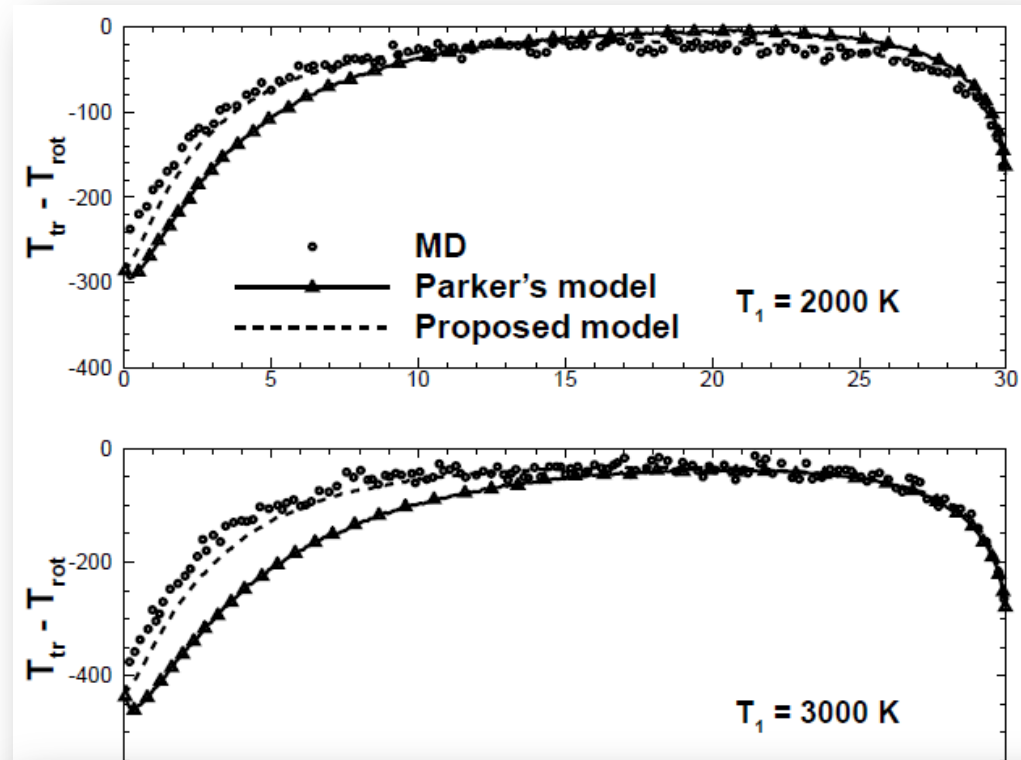
# New Model Results



Shock:  $T_1=300\text{K}$ ,  $M_1=7$



Expansion: Similar temperature range



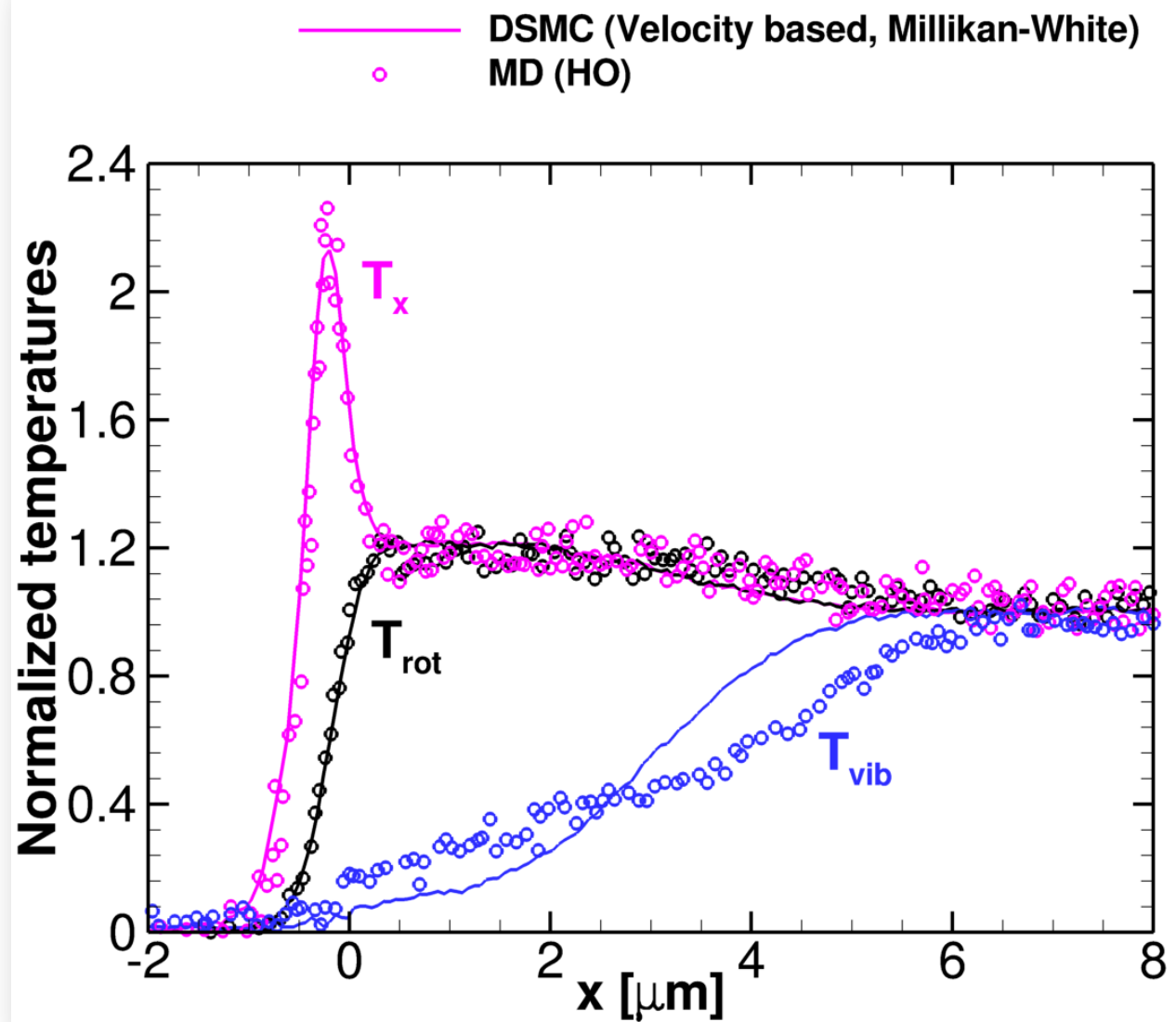
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# Vibrational Nonequilibrium (Preliminary)



- All-atom simulations  
[trans, rot, vib are post-processed]
- $N_2$  harmonic oscillators
- 5 million atoms
- Vibration will require accurate QM-based PES
- EDTD-MD and Trajectory-DSMC are very promising for arbitrary PES

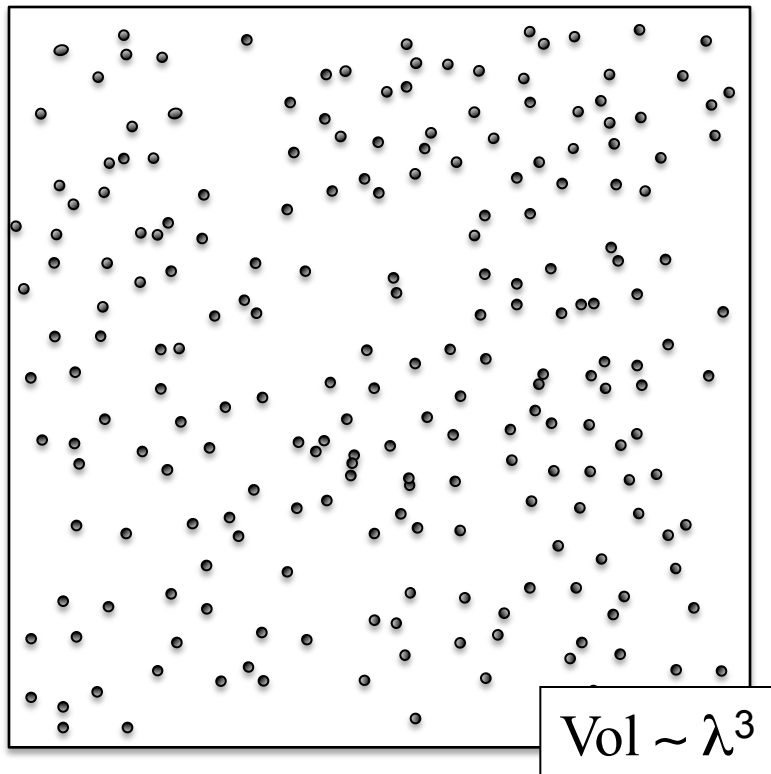


# Direct Simulation of Practical Flows



## Molecular Dynamics

- Simulate every atom in real system
  - Thousands – Millions per  $\lambda^3$
- Femtosecond ( $10^{-15}$  s) timesteps



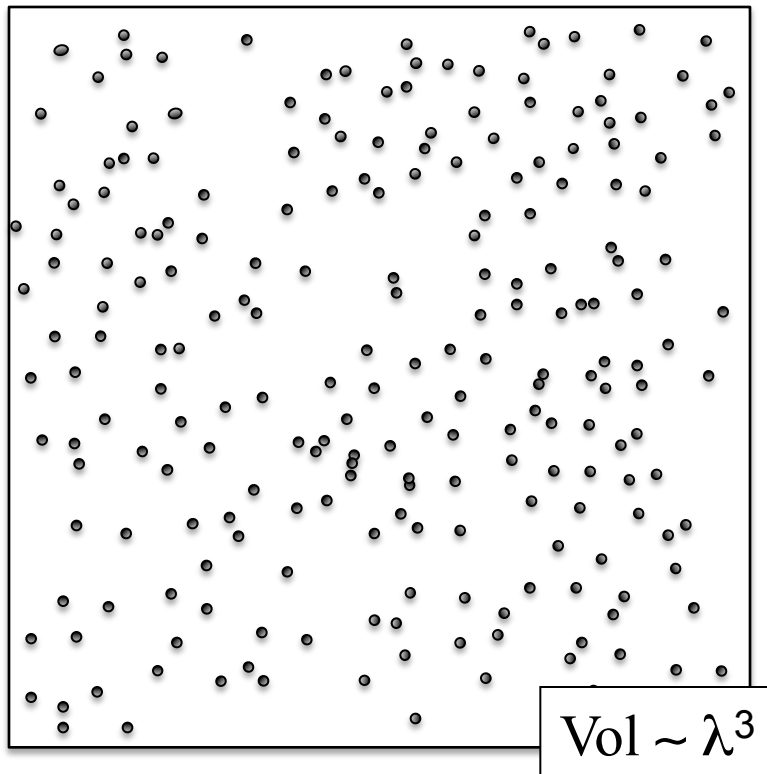




# Direct Simulation of Practical Flows

## Molecular Dynamics

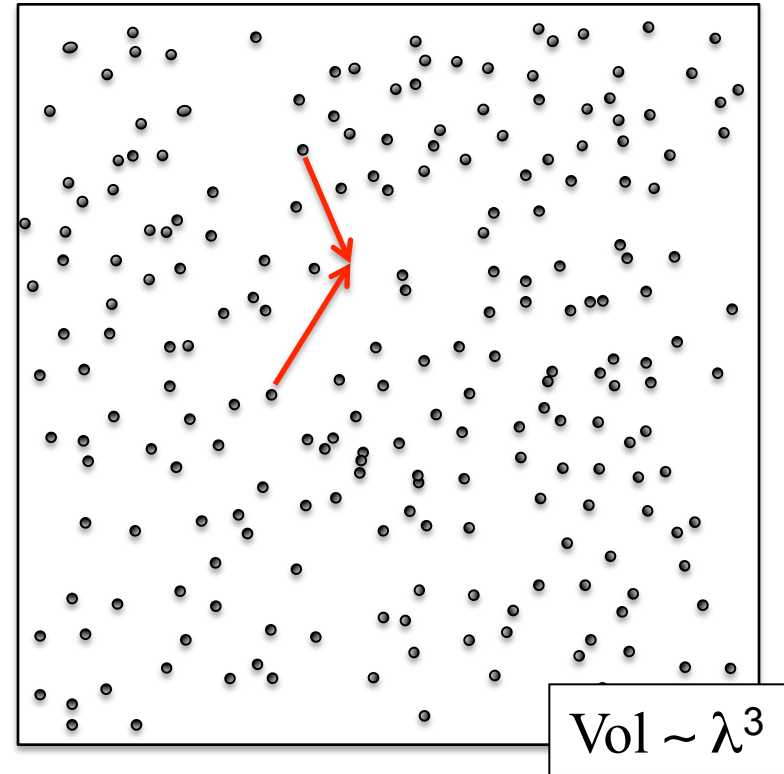
- Simulate every atom in real system
  - Thousands – Millions per  $\lambda^3$
- Femtosecond ( $10^{-15}$  s) timesteps



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## Event-Driven Time-Driven MD

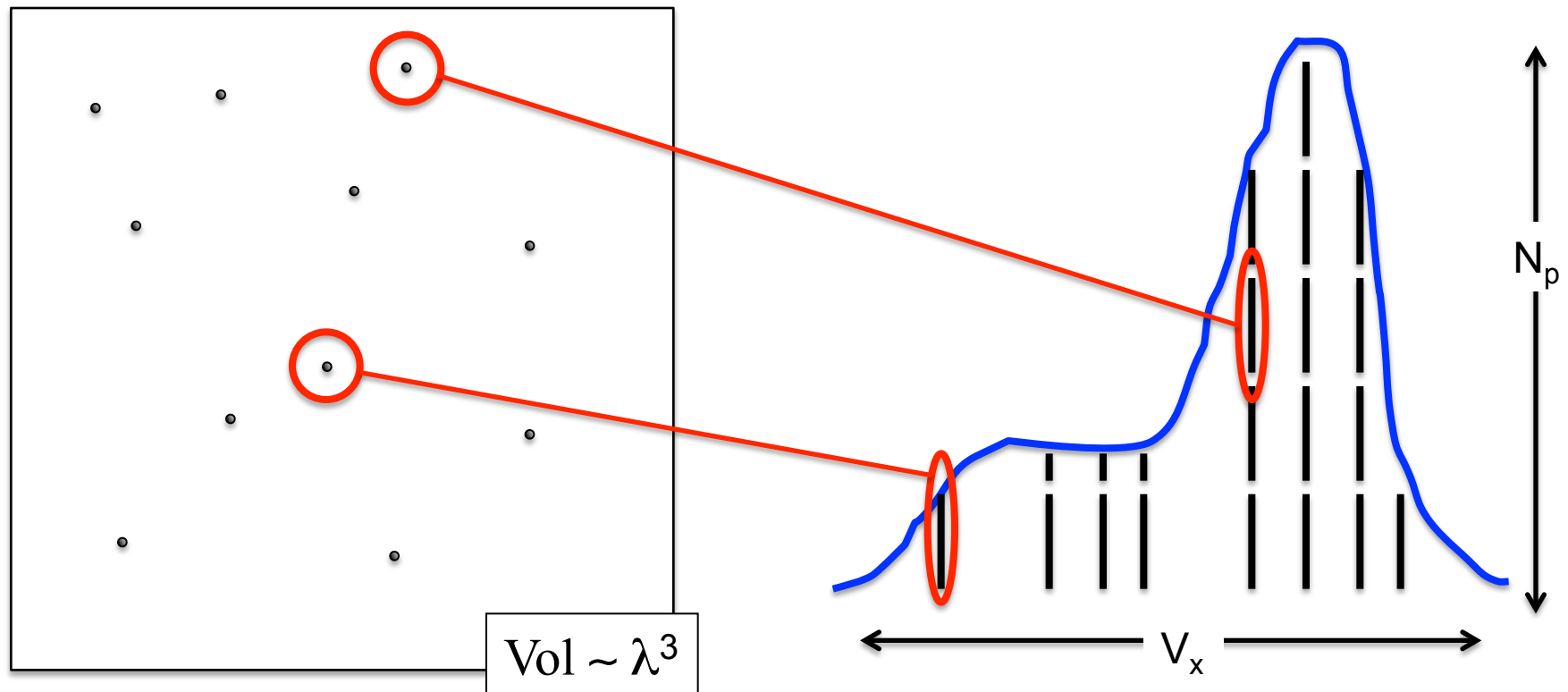
- Simulate every atom in real system
  - Thousands – Millions per  $\lambda^3$
- Timesteps  $\sim \tau_c$  (mean-coll-time)





# Direct Simulation of Practical Flows

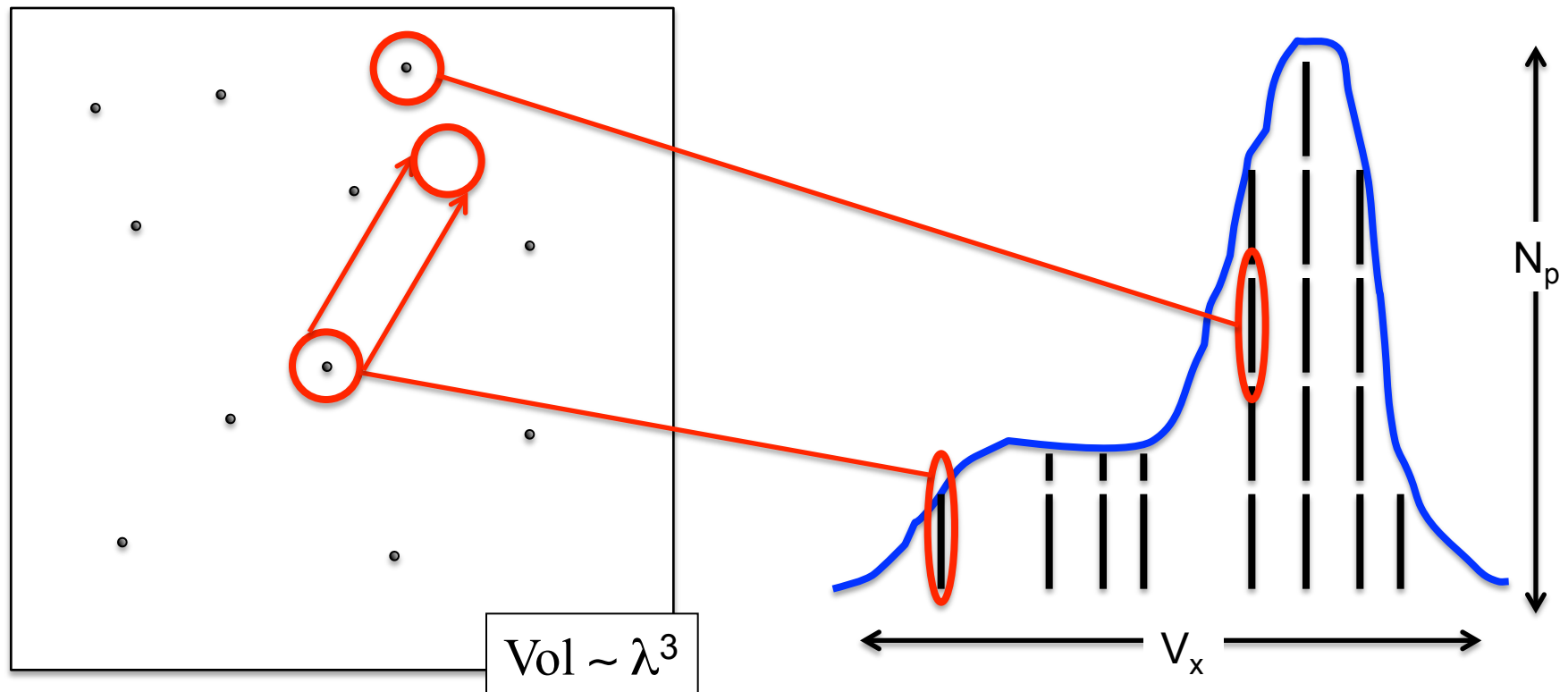
- One can obtain precisely the same statistics with far fewer molecules. This is what DSMC does.





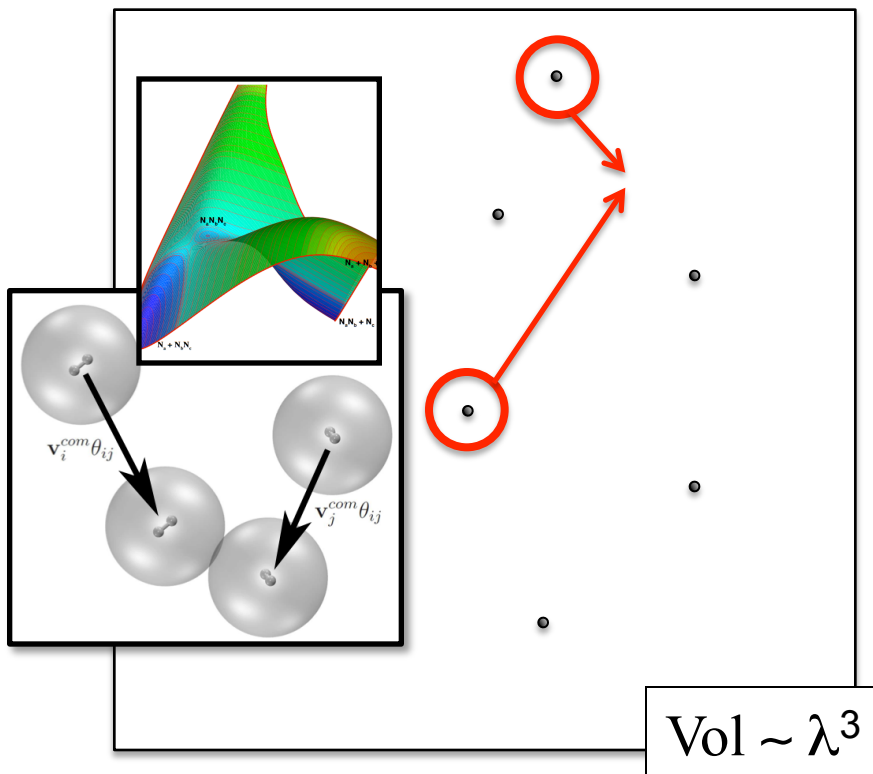
# Direct Simulation of Practical Flows

- One can obtain precisely the same statistics with far fewer molecules. This is what DSMC does.
- But now, what is the collision rate between simulator-molecules?
- For hard-spheres, the precise collision rate is easily determined (MD=DSMC)



# Direct Simulation of Practical Flows

- For real gases, DSMC attempts to model the true cross-section (and also employs probabilistic models for post-collision properties).
- However, an alternative is to integrate collisions directly within DSMC (**“Trajectory-based DSMC”**) [only  $\sim 100\times$  slower than DSMC]

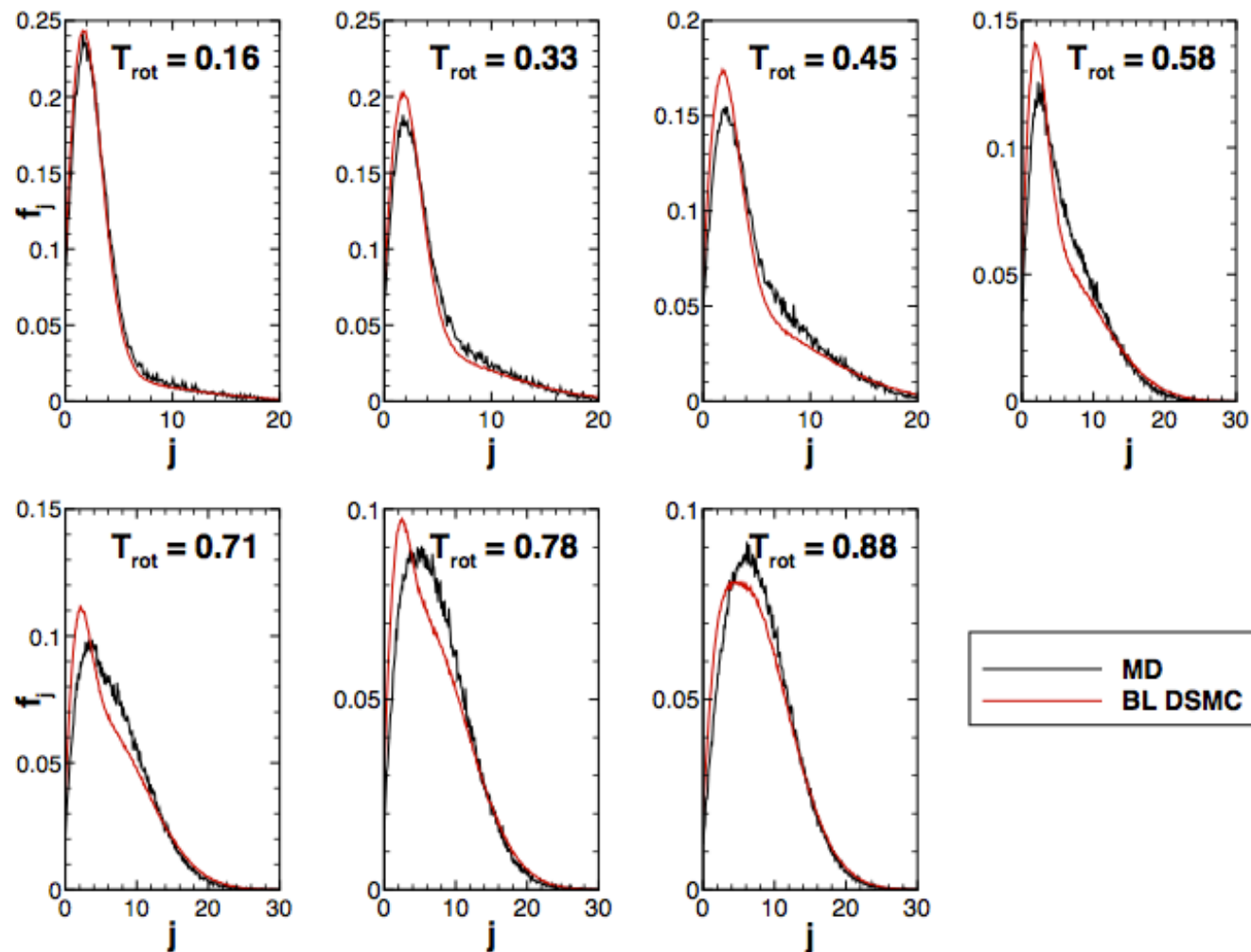


- Carefully match the HS cross-section with the impact parameter variation used for the collision calculations
- Simply make the HS cross-section conservatively large, and it will be the PES that determines the collision rate (and also post-collision states)
- We are working on 3-body collision rates for recombination.

# Standard DSMC vs. Pure MD



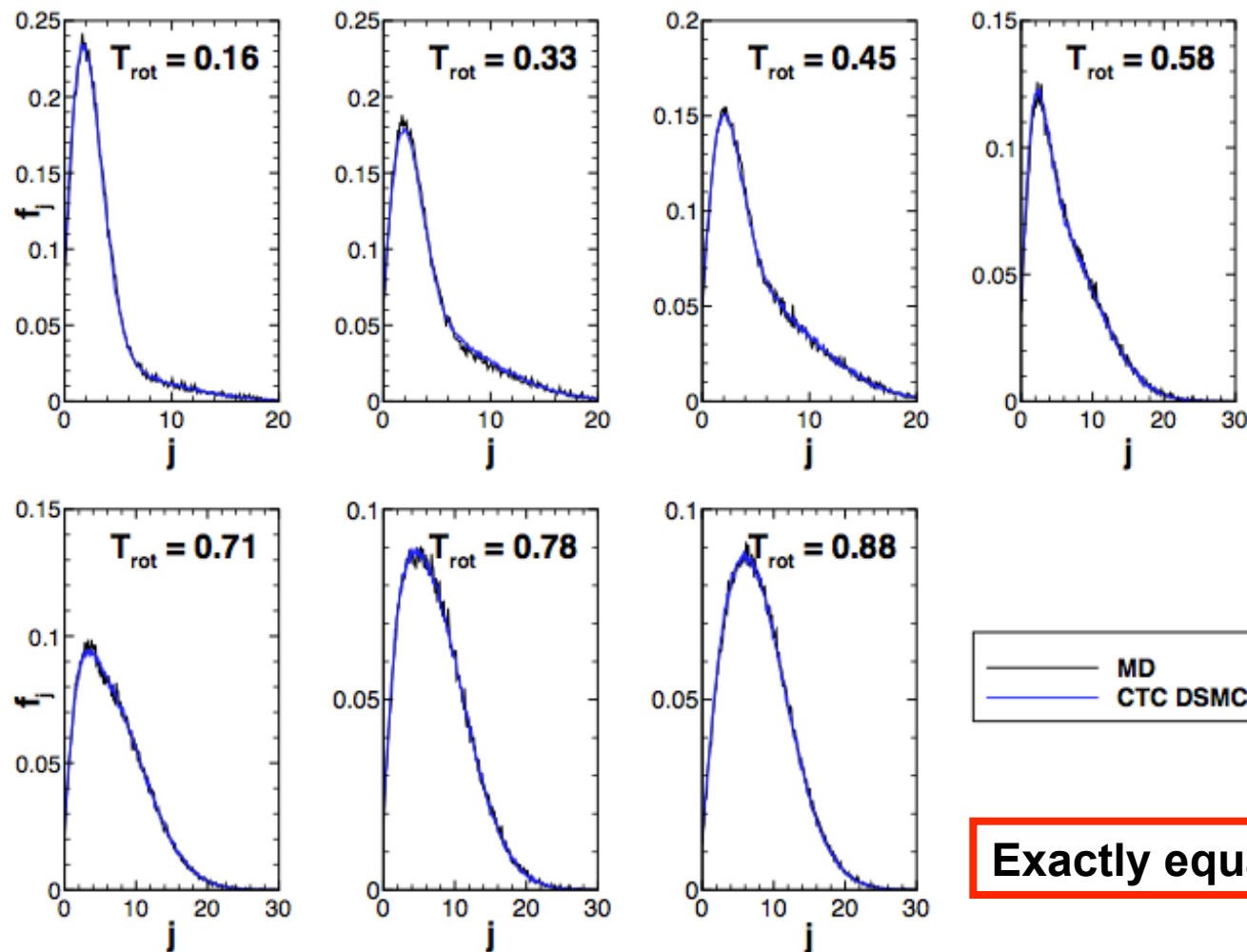
- Rotational level distribution functions within shock wave.



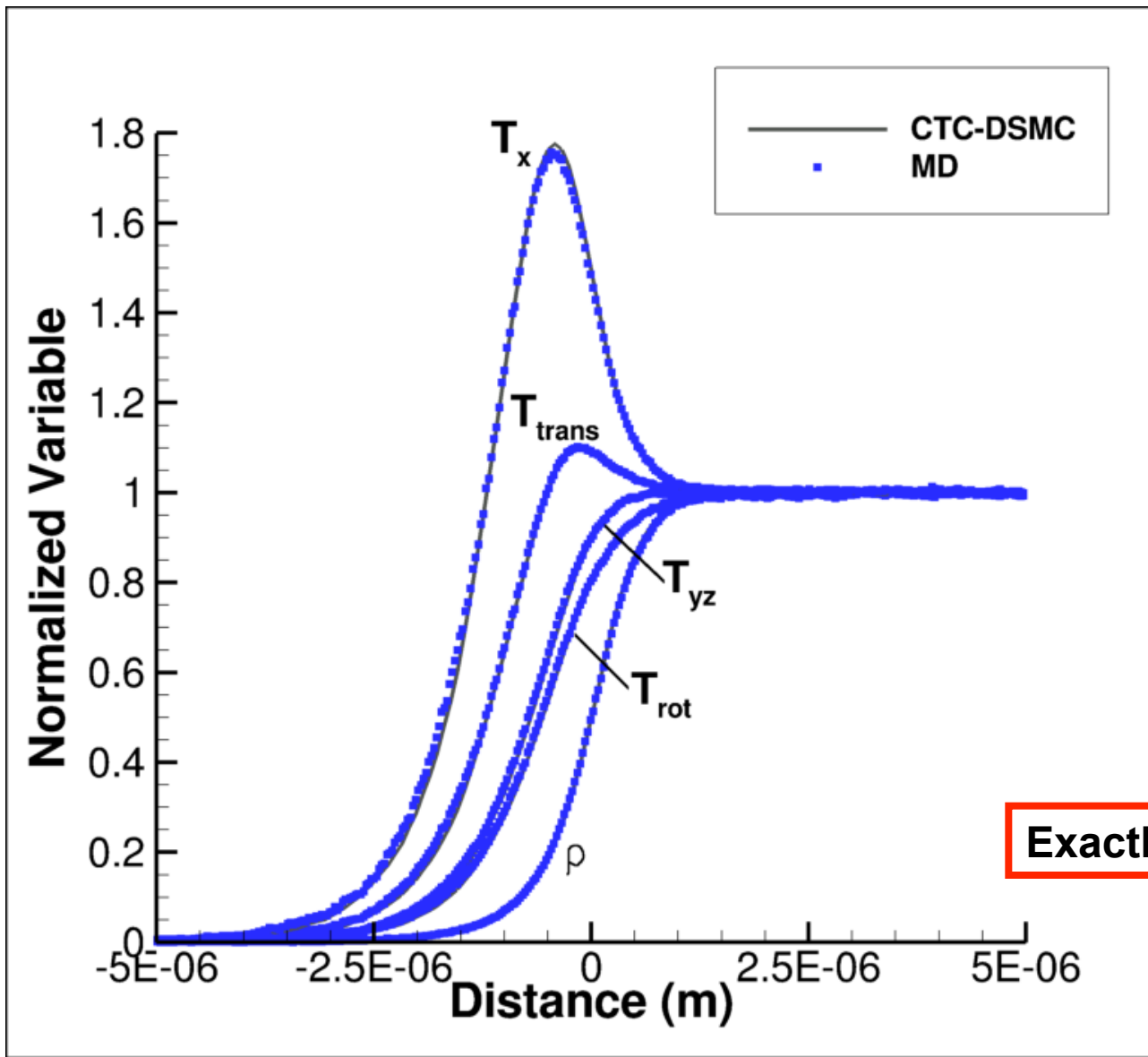
# Trajectory-DSMC vs. Pure MD



- Rotational level distribution functions within shock wave.



# Trajectory-DSMC vs. Pure MD



Exactly equal to pure MD.

# Trajectory-DSMC New Insights

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- Inherently enables the use of **multiple PES** for different species and potentially for different collision energies (LJ  $\rightarrow$  pure QM in theory)



# Trajectory-DSMC New Insights



- Inherently enables the use of **multiple PES** for different species and potentially for different collision energies (LJ  $\rightarrow$  pure QM in theory).
- >99% CPU time spent integrating collisions (DSMC move/sort/geom <1%). Thus perfectly suited for **GPU acceleration** (CPU handles move/sort/geom)
- Trajectory-DSMC  $\sim 100x$  more expensive than DSMC, but 2 weeks of GPU coding has found **speed-up of 10x per GPU!**
- Current nodes have 8 core-CPU's and 4 GPU's (= 50 core-CPU node...)

Method	Speedup vs. Serial	Speedup/GPU
Serial	1x	-
OpenMP	7.14x	-
OpenMP + 1 GPU	-	-
OpenMP + 2 GPU	33.24	13.05
OpenMP + 4 GPU	50.58	10.86

# Trajectory-DSMC New Insights



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- We achieve GPU load-balancing by relative collision velocity (high speed collisions are actually faster)
- Stagnation line simulations using new surfaces within a year ( $N_2+N_2$ ,  $O_2+O_2$ ,  $N_2+O_2$  – Truhlar UMN Chemistry and possibly  $N_2+N$  – NASA?)

# Summary and Conclusions

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- 1) Pure Molecular Dynamics of normal shock waves is possible
- 2) MD simulations have been validated with all available experimental data for Ar, Ar-He, Xe-He, and N<sub>2</sub>(rot) shock waves
- 3) New internal energy relaxation physics were found for N<sub>2</sub> rotational excitation/relaxation (ground vibrational state)
  - weaker temperature dependence than prior models
  - strong dependence on direction and degree of nonequilibrium
- 4) Demonstrated how a reduced-order model for DSMC/CFD can be constructed based on MD results (and we recommend its use)
- 5) Preliminary results show that trajectory-based DSMC exactly reproduces pure MD results at a cost ~100x slower than DSMC. However, trajectory-DSMC is perfectly suited for GPU acceleration with realistic 50x speedup on existing architectures.

# Challenges and Open Questions

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- 1) Can we implement trajectory-DSMC such that 3-body collision rate is determined only by the PES (and exactly equals MD)?
- 2) Can we achieve GPU scalability ( $>10\times$  per GPU) for complex PES?
- 3) **How do we go about model reduction for vibration, and rot-vib-diss coupling? What precisely should we look for?**
- 4) Chemistry is not entirely in our control... requires real collaboration. Will these PES agree with experiment for dissociating flows? What if they don't?
- 5) Experimental validation. Currently many CFD/DSMC and now MD calculations match the same experimental data sets (density/pressure traces). No way of distinguishing models. We need new data with hydrodynamic, internal energy state, and species fractions (even at a few points in a shock or expansion flow).

# Acknowledgments

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- University of Minnesota researchers:
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  - Paul Norman
  - Chonglin Zhang
  - Savio Poovathingal
  - Byron Edgar

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# Questions?

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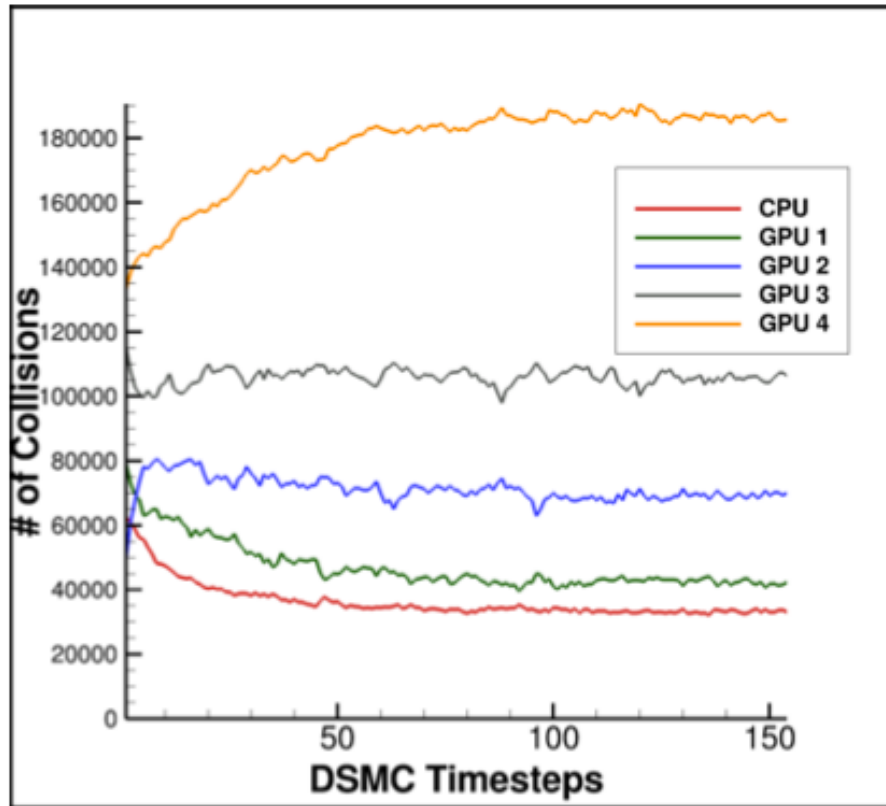
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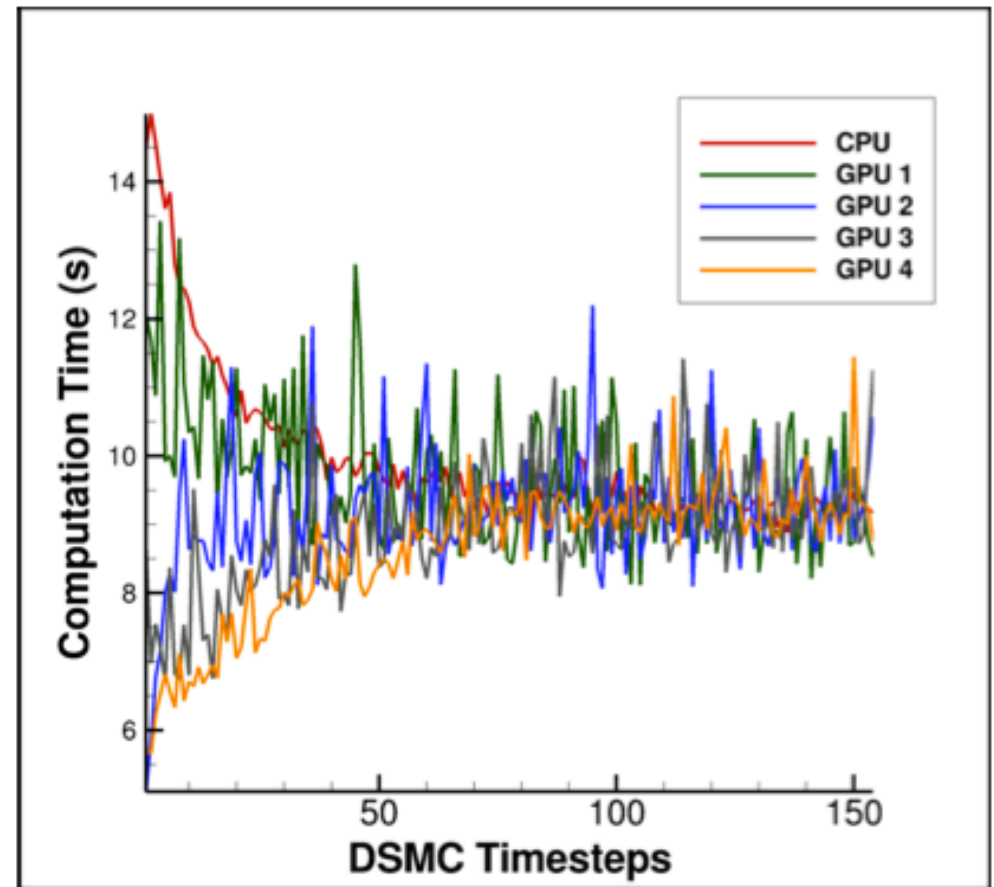
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# GPU Load Balancing



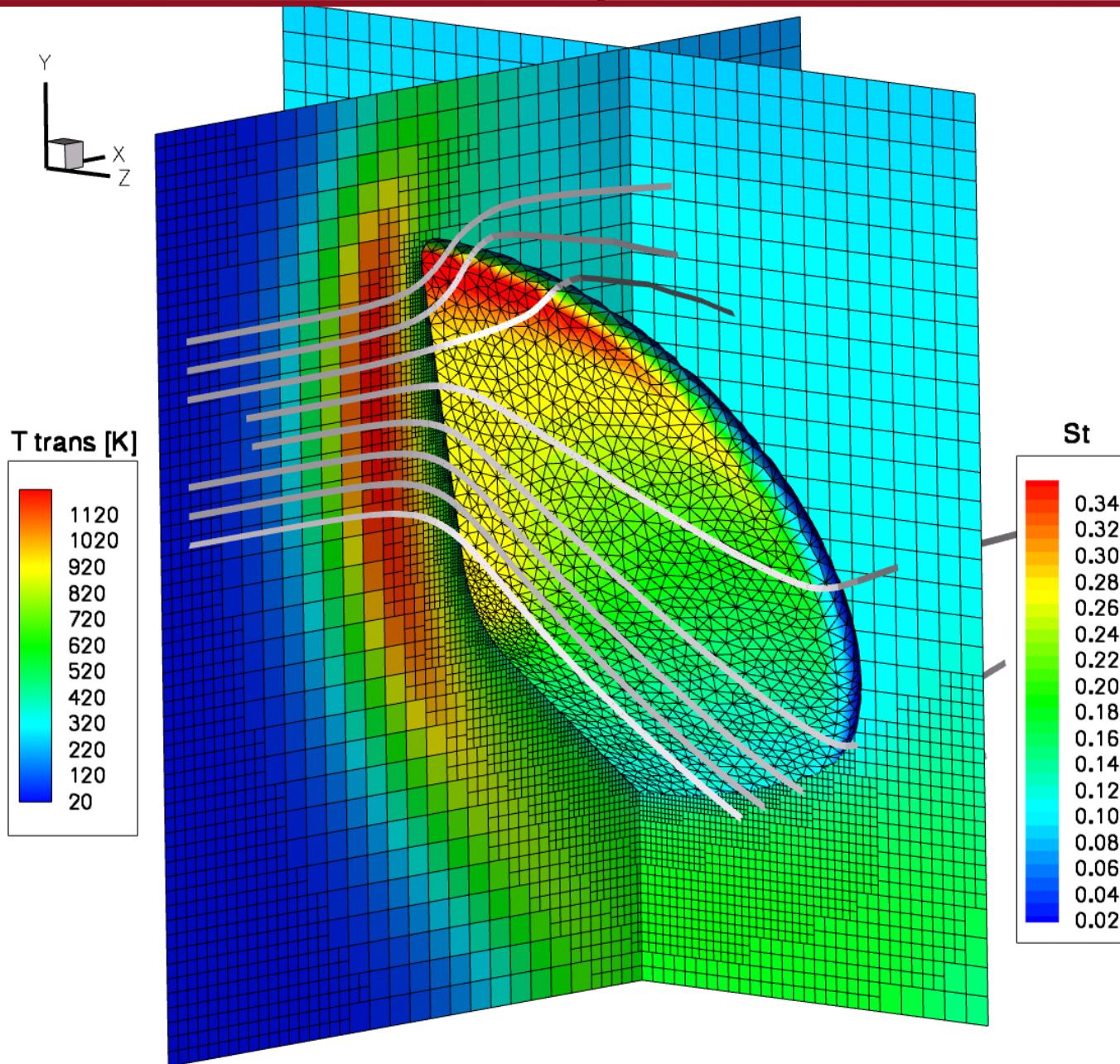
(a) Number of collisions vs. DSMC timestep



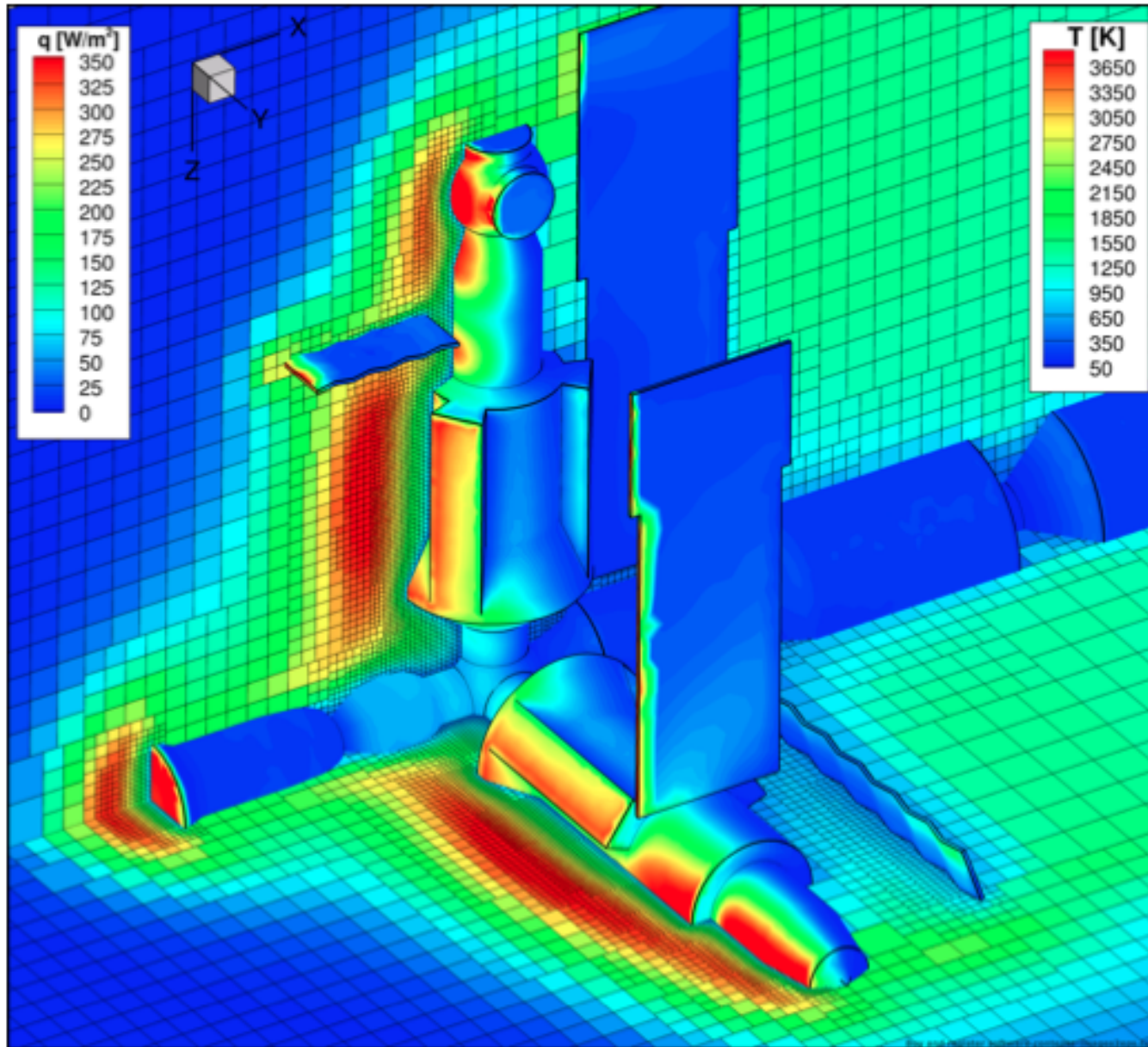
(c) Computational time vs. DSMC timestep



# DSMC Solution for Planetary Probe



# DSMC Solution for MIR Space Station







# Micro and Nanoscale Flows

- $\lambda$  and  $\tau$  are constant so  $\Delta x$  and  $\Delta t$  are uniform
- Low  $T$ , so no gas-phase vibration/dissociation chemistry
- High thermal fluctuations compared to bulk flow velocity (large scatter)
- Requires subsonic (or far-field) boundary conditions and large domain sizes
- *Real* fluctuations in gas flow are present; nano-clusters may be “random walkers”

